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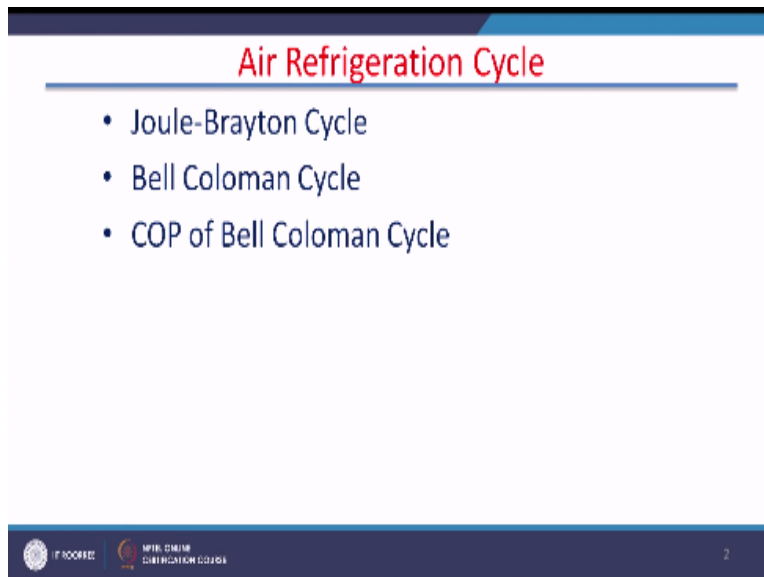
Refrigeration and Air-conditioning

**Lecture-03
Air Refrigeration Cycle**

**with
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Department of Mechanical and Industrial Engineering
Indian Institute of Technology, Roorkee**

I welcome you all in the course on Refrigeration and air conditioning today we will cover the air refrigeration cycle in today's lecture we will be covering Joule Brayton cycle Brayton cycle.



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Air Refrigeration Cycle

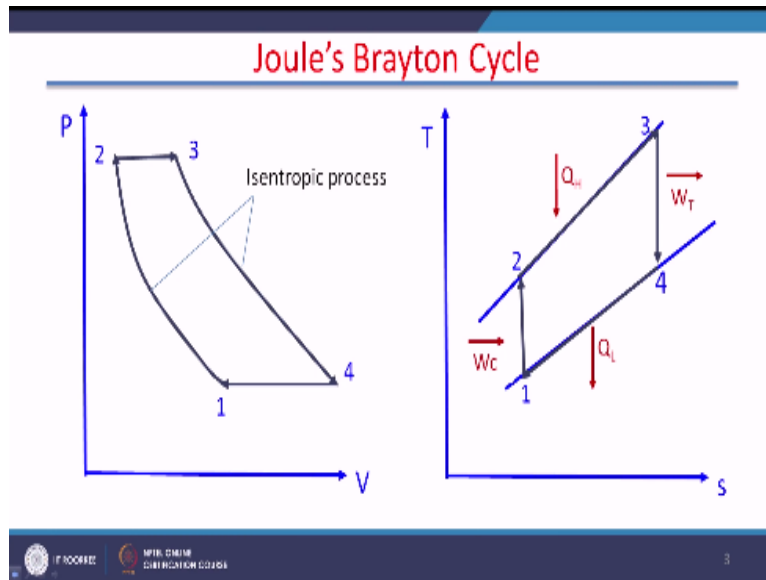
- Joule-Brayton Cycle
- Bell Coloman Cycle
- COP of Bell Coloman Cycle

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And we will try to find COP of bell Coloman cycle the starting with the Joule Britain cycle I actually Joule Barayton cycle is a years ended cycle for power generation and this cycle is being

used for the power generation in gas turbine it is one specific application in gas turbine and in this cycle there are two isentropic processes.

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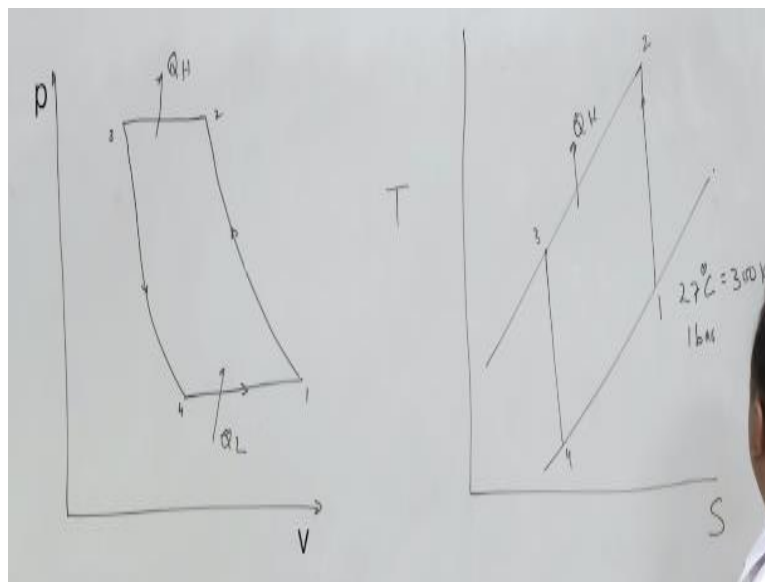
And where two constant pressure processes so this cycle is depicted here on pressure volume diagram and at the same time this cycle also depicted here on temperature entropy diagram now in this cycle first here is a working fluid and the first air is compressed from state 1 to state 2 through a compressor at state constant pressure heat addition takes place normally in the gas turbine separate compression chamber in that compression chamber the heat addition takes place but since it is a gas turbine cycle it is assumed that throughout the cycle air is fluid so from state one to state 2.

Compression air takes place is state 2 to state 3 constant pressure heat addition takes place constant pressure heat addition to air takes place and when the state 3 is attained the expansion of air takes and we attain the state 4 during this process the output the net output of the cycle is the area of PV diagram under 1, 2, 3, 4 this cycle can also be shown on temperature entropy diagram process 1 to 2 is isentropic compression where work is done by the compressor on the gas on the air process 2 to 3 is constant pressure heat addition process 3 to 4 is output of turbine or

expansion of hot air take place and process 4 to 1 is the cooling process or if it is open cycle then at state 4 the air is thrown to the surroundings now if you reverse this cycle if you reverse this cycle reverse means instead of expansion process 3 to 4 compression in process 3 to 4 3 takes place compression and then heat rejection then 2 to 1 expansion and 1 to 4 heating the cycle will become something like this now this is reverse Joule Barayton cycle or it is called bell Colaman cycle.

Bell Colaman cycle here refrigeration cycle it is called air refrigeration cycle because in this cycle air is the work king fluid or air is the refrigerator now in this cycle.

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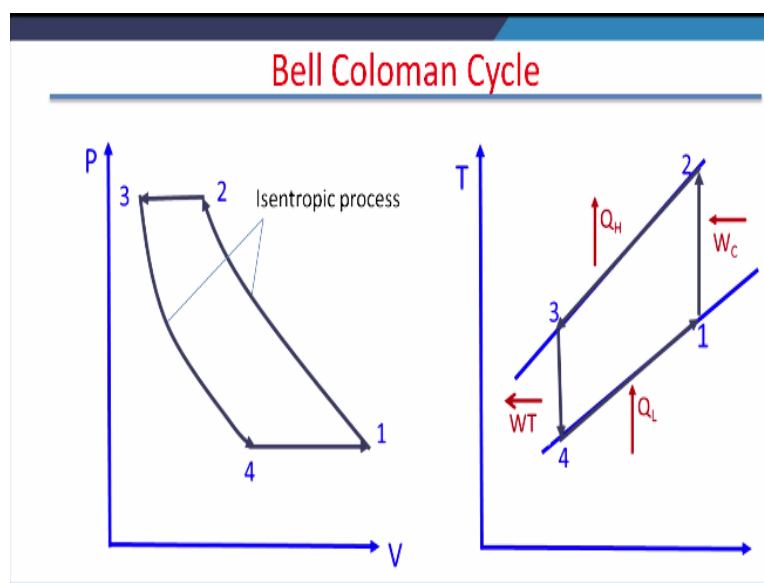


If we show it on the PV diagram first of all compression of air take place from state 1 to state 2 after this compressing the cooling of air take place or heat is removed during this process from the air so the temperature of the air goes down when the state 3 is attained again expansion take place inside an expander it is a turbine or an expander where expansion takes place and these two processes 3 to 4 and 1 to 2 are isotropic process and 4 to 1 process where heat is taken from the surroundings and this process 4 to 1 process is the pulling effect, now if I want to show this same cycle on temperature entropy diagram.

Then the two constant pressure processes constant pressure lines process 1 to 2 isotropic compression where the pressure increases then heat is extracted from the sphere high pressure here so it becomes high pressure low temperature here and heat is taken away from here and we are in state 3 at a state 3 again the expansion takes place and state 4 is reached, now I will give you some numerical values for these states also.

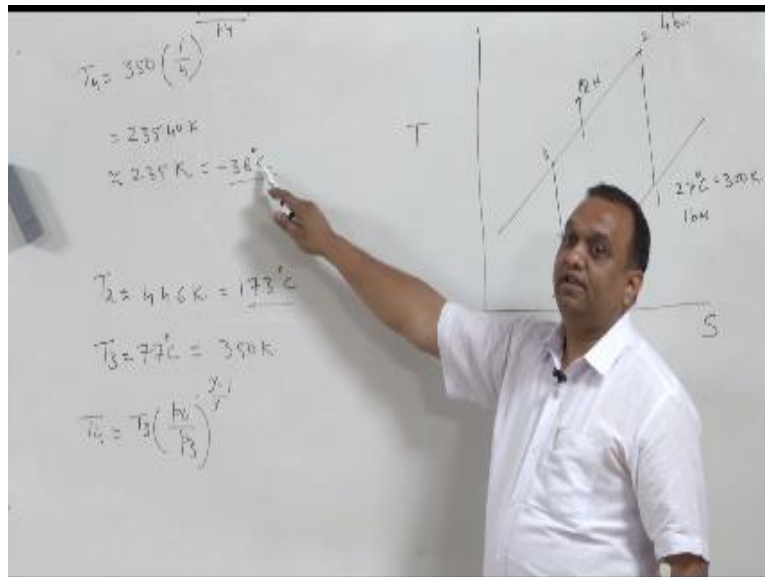
So that you will have a fairly good idea about this cycle now starting from state 1 suppose here is a label at 27°C and one bar pressure so when air is available at 27°C it is equivalent to 300 Kelvin of temperature, suppose this air is compressed in a compressor having compression ratio 4.

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So P_2 with P_1 is 4.

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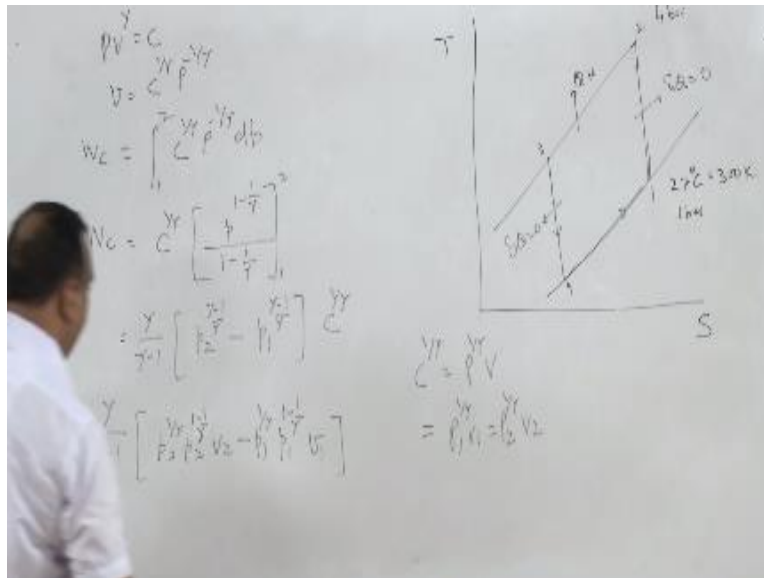
P_2/P_1 , now temperature at state 2 is been to be P_1 multiplied by $(P_2/P_1)^{\gamma-1/\gamma}$ because it is following the process $Pv^\gamma = \text{constant}$ where $\gamma = 1.4$ for air, now if you put the numerical values that T_1 is 300 Kelvin so in order to find T_2 , T_1 is 300 Kelvin, P_2/P_1 is 4, $(4)^{1.4-1/1.4}$ it will turn out to be 4 approximately 446 Kelvin it is exactly it is 445.97 another zoom for 46 Kelvin so 446 Kelvin = 173° Centigrade.

So the temperature of the air is increased where during the compression process 273° C now if I cool this air with the help of surrounding a surrounding in is 27° C, I cool this air to let us say 77° C so it is T_3 is 77° C or 350 Kelvin, temperature of air a level at state 3 is 350 Kelvin and pressure is 4 bar here pressure is 1 bar here pressure is 4 bar, now if I expect this here 2 straight 4 if I expect this here 350 Kelvin here at 4 bar to one bar. Isotropically in that case I am going to get $T_4 = T_3(P_4/P_3)^{1.4-1/1.4}$ and this just a minute is raise to power $\gamma - 1$ over γ now P_3 is 300 $T_4 = T_3$, T_3 is 350k 350 and P_4/P_3 is $1/4$ and 1.

This γ 1.4 – 0.4/1.4 so this will turn out to be 235 approximately 235.44k or let us say 235k or is equal to -38° C so during this cycle during the cycle we have taken outside a compressed it who let and then we have expanded back to the seam pressure 1 bar and the temperature of here had

reduce to -38°C which is very, very low so with the help of this Belcolovin cycle we can get very low temperature in the case of here now after this we will find try to find the performance of the cycle in order to find the performance of the cycle.

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We should how much heat transfer is taking place and how much energy is consumed in compressing that here during the refrigeration process that is 4 to 1 but heat transfer is that is OL is CP this is constant specific heat of here at constant pressure $T_1 - T_4$ this is the refrigeration effect we are getting the cycle now how much work is consumed work assumed is AV of PV diagram or work in compression – work deemed in expansion now compressor work from state 1 to state 2 were several ways of doing it first fall it is a cyclic process so in a cyclic process as per the first law of thermodynamics.

Cyclic integral of $\delta Q =$ cyclic integral of δw here in these two process, process 1 to 2 and 3 to 4 they are isotropic process so heat transfer is 0 only heat transfer is taking place in process 4 to 1 and 2 to 3 so net E transfer $C_p (T_3 - T_2) - C_p (T_4 - T_1)$ and this net heat transfer is also network transfer that is one we have doing it another way is if we use the formula δw is integral of 1 to 2 $V dp$ through this formula also.

We can find the work done because when these processes are not isotropic in that case we cannot use this formula. This formula is applicable only in that is when all the processes are ideal and there is no heat transfer during these two processes. So in order to have a generalized expression let us try to find out work through this formula, work consumed by the compressor through this formula, this work interaction has negative sign an energy is consumed by the compressor it means work interaction is negative in this process.

So negative, negative is positive so for positive so the work of the compressor is state 1 to state 2 $\int V dp$. During the compression if it is isotropic compression or reversible adiabatic compression PV^γ will remain constant or $V=C^{1/\gamma}$ and $P^{-1/\gamma}$ now putting these values of V here will get work of the compressor is equal to integral from 1 to 2 $C^{1/\gamma} P^{-1/\gamma} db$ again the work of compressor is equal to $C^{1/\gamma}$ and if we integrate this will be getting $P_1^{-1/\gamma} \int_{1-1/\gamma}^{1-1/\gamma} 1 \text{ to } 2$ or $\frac{\gamma}{\gamma-1} P_2^{\gamma-1/\gamma} - P_1^{\gamma-1/\gamma}$ multiplied by $C^{1/\gamma}$.

Now $C^{1/\gamma}$ is equal to $P^{1/\gamma}$ into V , now putting this value because now PV now we can always take it as like this $P_1^{1/\gamma} V_1 = P_2^{1/\gamma} V_2$ now putting this value of C here we will be getting $\frac{\gamma}{\gamma-1} P_2^{1/\gamma} P_2^{\gamma-1/\gamma} - P_1^{1/\gamma} P_1^{\gamma-1/\gamma}$ or we can instead of writing like this $\frac{\gamma-1}{\gamma}$ I will write $1-1/\gamma$, $1-1/\gamma$ and V_1 . If you simplify this equation you will be getting work consumed by the compressor is.

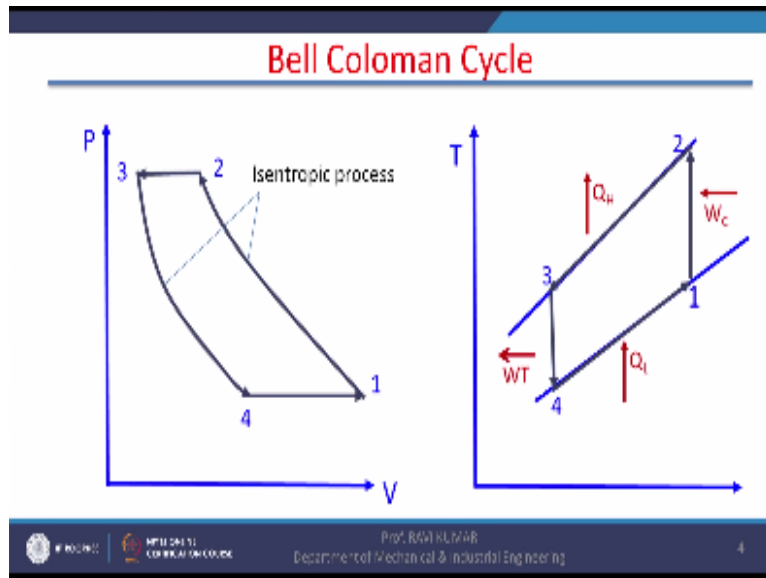
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$\frac{\gamma}{\gamma-1} P_2 V_2 - P_1 V_1$ here it is considered to an ideal gas here so PV can also be replaced by RT so $\frac{\gamma}{\gamma-1} R(T_2 - T_1)$. Now $\frac{\gamma}{\gamma-1} R$ is nothing but C_P , $C_P (T_2 - T_1)$ here there is an interesting observation that adiabatic compression is taking place pressure of the gases raising, okay and work done in this process is $C_P \delta T$, C_P is the heat at a specific heat at constant pressure, it is C_P and there is no constant pressure process here.

So it is only N expression it does not indicate that the pressure is the process is a constant pressure process but this expression is a simple expression for work will like the compressor similarly we can find the work output during process 4 that is work of the turbine or work of the

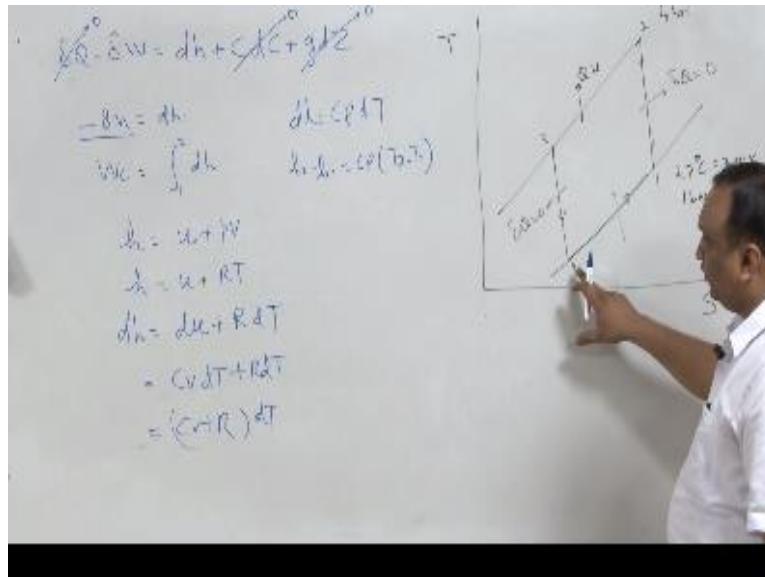
expander it equal to $C_p T_3 - T_4$ and the network is $c_p t_2 - T_1 - C_p T_3 - T_4$ or $C_p T_2 - T_3 - c_p T_1 - T_4$ or heat rejected in this process. And heat take care in this process or cyclic integral of heat.

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Heat transfer there is another way of I have already discuss two ways of idée the network there is another method also if we use the first law of open system first law of open system states.

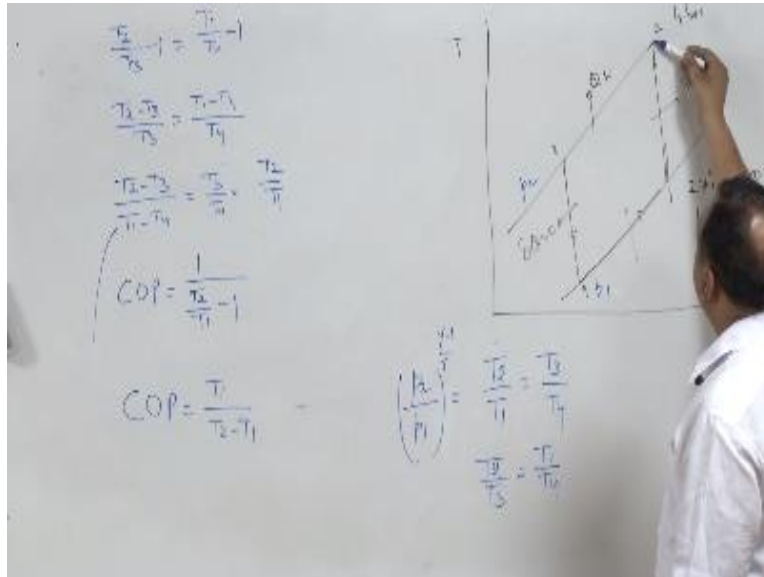
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When in open system $\delta Q - \delta W = dh + cdc + g dz$ now here in this case in case of compressor this changing potential can be consider a 0, to change in kinetic energy is also 0 isentropic process there is no neat transfer, so $-\delta w$ is dh this $-\delta w$ means work is consumed b the compressor, so work of the compressor is integral of 1 to 2 dh as we know net $h =$ inter energy + Pv or $h = u + rt$.

Pv we can always use the relation $Pv = rt$ in case of ideal gas and here is an zoom to be an ideal gas so $dh = du + rdt$ or du is always $c_v dt + dt$ and this is $C_v + r dt$ and this is so $dh = C_p Dt$ or $h_2 - h_1 = c_p t_2 - t_1$ similarly we can drive for this also that work at in a during expansion process, $C_p T_3 \cdot T_4$, and we can again come to the conclusion or we will come to the, same expression as we have attain through the earlier, processes, so we have there alternative methods, to find work during compression. Now COP of this cycle, coefficient of performance of this cycle, because efficiency of any refrigeration cycle is judge by the coefficient of performance, so coefficient of performance is.

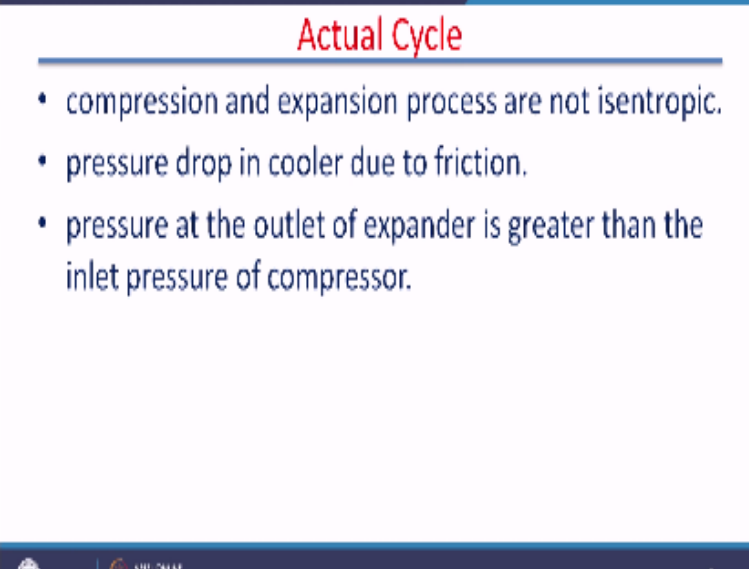
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Heat transfer during the refrigeration process, that is $C_p (T_1 - T_4)$ divided by network consumes, so it is going to be $C_p(T_2 - T_1) - C_p(T_3 - T_4)$, C_p will be cancelled out, and COP, will remain $T_1 - T_4 / T_2 - T_1 - T_3 - T_4$, if we rearrange these terms, $T_1 - T_4 = (T_2 - T_3)(T_1 - T_4)$, or it is equal to $1 / T_2 - T_3 / (T_1 - T_4) - 1$, we can further simplify this, because $(P_2 / P_1)^{\gamma - 1(\gamma)} = P_2 / P_1$, this is also P_2 , and this is P_1 , so $P_2 / P_1 = T_2 / T_1$, this is from ideal gas relation, is equal to T_3 / T_4 .

Now here if you take this relation, or we can further manipulate it like this, $P_2 / P_3 = T_1 / T_4$, so $T_2 / T_3 - 1 = T_1 / T_4 - 1$, $T_2 - T_3 / T_3 = T_1 - T_4 / T_4$, or T_2 / T_1 , this $T_2 - T_3 / T_1 - T_4$ can be substituted here and we can get the value of COP as $1 / T_2 / T_1 - 1$ and final expression for COP as $T_1 / T_2 - T_1$, so for ideal bell callable cycle, we need only two information, temperature after compression, temperature before compression and we can find the COP of the cycle. Actual cycle, now actual cycle, I will depict actual cycle on both on pressure entropy, sorry, this pressure volume and temperature entropy diagram.

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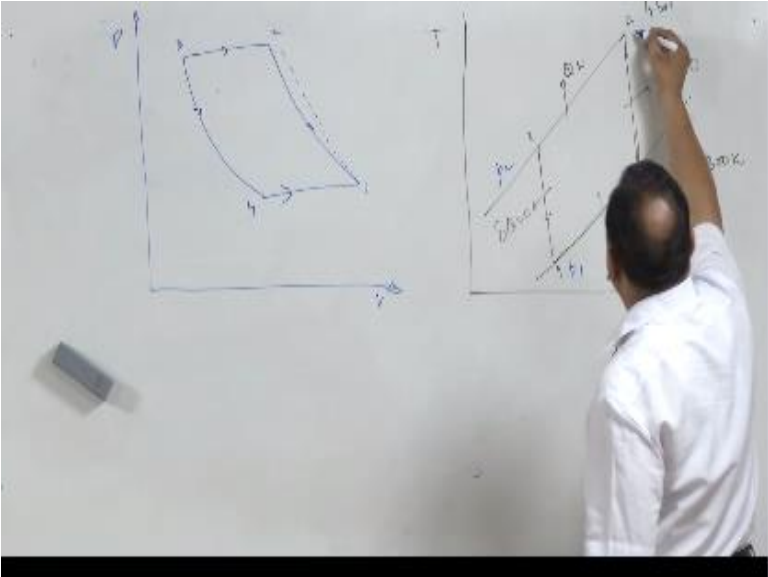


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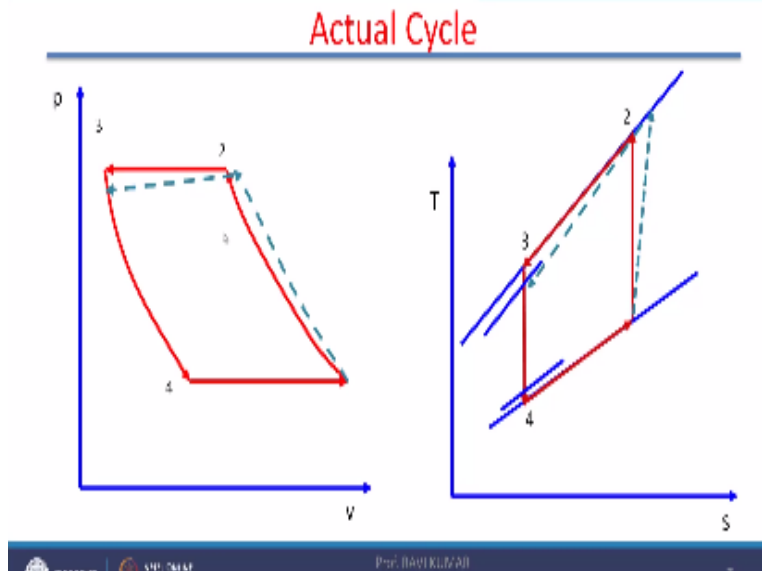
- compression and expansion process are not isentropic.
- pressure drop in cooler due to friction.
- pressure at the outlet of expander is greater than the inlet pressure of compressor.

In the actual cycle, first of all, this is a ideal cycle, 1, 2, 3, 4, pressure and volume. In actual cycle, this is no longer a radiometric process, the process will be something like this, it can be shown here a change in the entropy as there is increase in this process, so it is 2 dash. For cooling also temperature may not remain constant, okay. So temperature, sorry for cooling the pressure may not remain constant, the pressure will fall during the process.

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After that expansion also is not an isentropic process, it is again, there is a change in isentropic, so the expansion something like this 1-2 dash, 3 dash and 4 dash and there is going to be pressure drop in the evaporator or during the heat expansion from the surroundings also. This is actual cycle, so the pressure at the outside of the expander is greater than the pressure of the inner of the compressor. Now with this I end this lecture, In the next class we will take p aircraft refrigeration system.

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