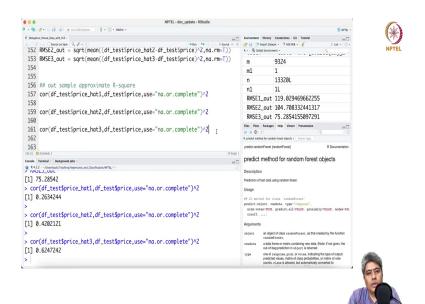
Predictive Analytics - Regression and Classification Prof. Sourish Das Department of Mathematics Chennai Mathematical Institute

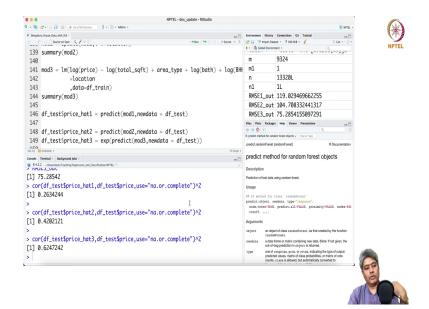
Lecture - 56 Hands on with R : More Prediction of Bangalore House Price

Hello all. In this video, we are going to continue on the Bangalore House Price Data Analysis using R. So, in this particular video, we will whatever we have done in along with that, we will do few more models, and trying to understand some of the way we split the dataset is actually called a static random stratified sampling strategy and we will try to understand what is it doing.

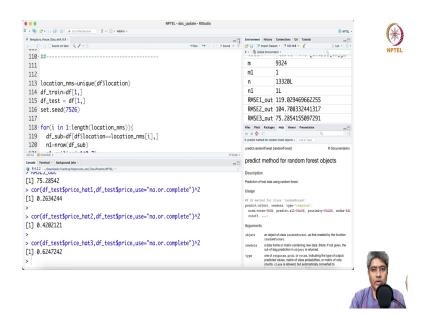
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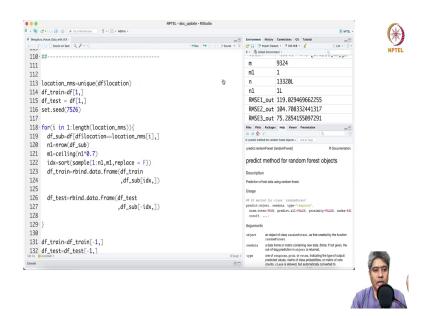


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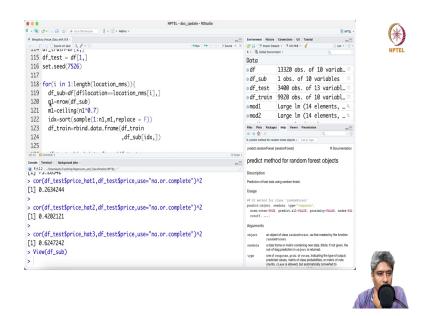
So, here in the we can let me first talk about the strategy of splitting the data by location.

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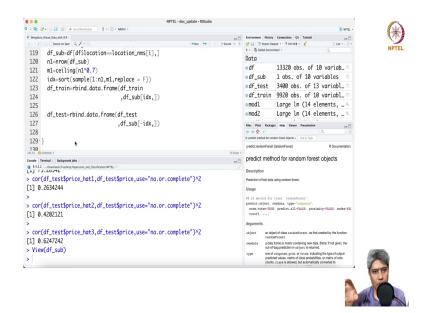
So, here you remember that we put the we call the locations, unique locations and put them in location names. Then, we just created a space holder for train and test, I set the seed and then for each location, we created a sub dataset here.

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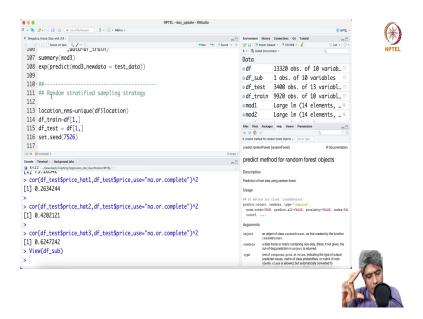


And then we took the n1 and we put it in the ceiling, and then we draw the sample and in that sample, we just put it in the idx and then test and then we just append that in the test. So, therefore, each location we created a sub dataset and then for each location, whatever the sample we have, we just split it into 2 and into 30, 70 way into train and test dataset.

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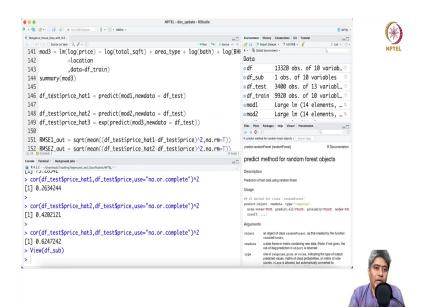


Now, this strategy is known as random stratified sampling strategy. The idea is imagine you want to draw sample all over the India. You can either draw simple random sample with replacement. In that case, what might happen that you made quite a few samples from big states like Maharashtra, Tamil Nadu, or you know Uttar Pradesh, but there are some small state like Sikkim, Goa, ok. In those states, you may not find even a single sample.

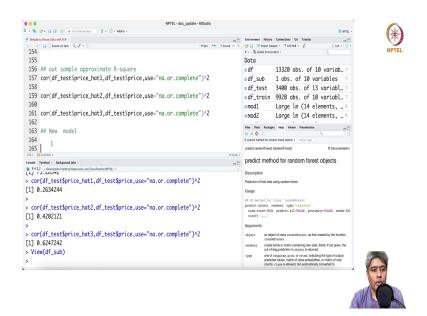
In this, this is not a very good strategy because you want you want representative of from each sample. Similarly, here each location, for each location, I want a representation. So, that is exactly what we are doing. This strategy is called random stratified sampling strategy and because of that, we avoid the issue of inconsistent modeling. Now, our model is consistent across all locations.

So, you can apply this strategy when you will handle state level data or any location or any data where which will have a some kind of categorical variable or too many categorical or categorical variable with quite a few locations. It is good to stratify the samples using or random draw the samples using stratified sampling strategy.

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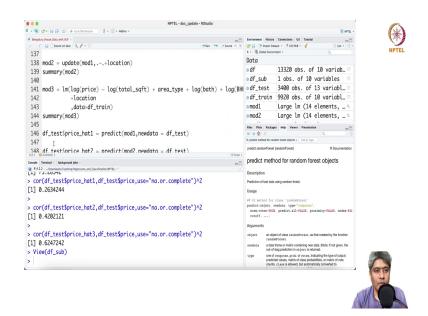


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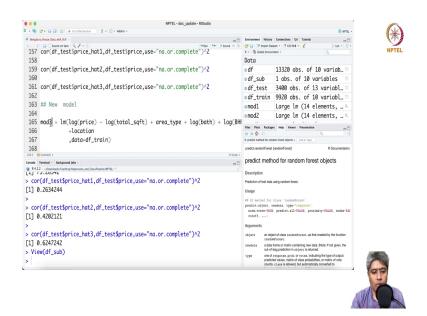
So, that is why we avoided all those problems and we able to move on to new models. So, let us try to fit a new model. So, new model.

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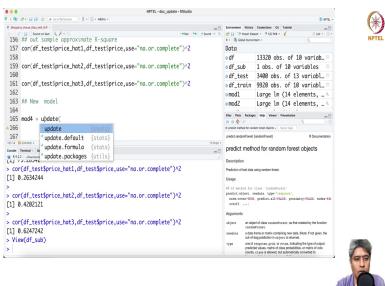
So, this was our best model. So, for the third model was the best model. And can we add few more thing in the best model?

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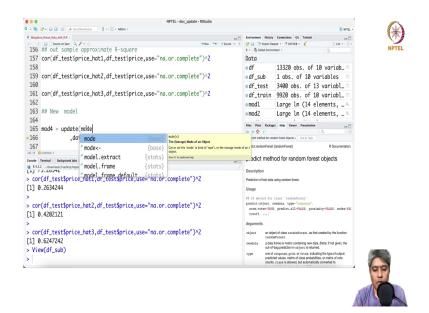
So, mod 4; oops mod 4 and maybe what we will do, we will just update the first, we do not want to again run the model 3.

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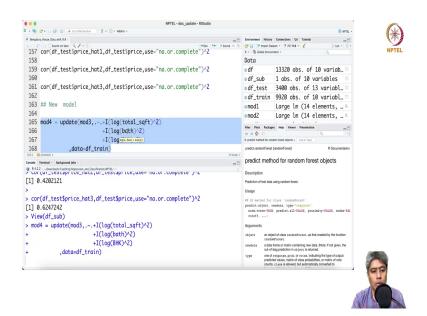


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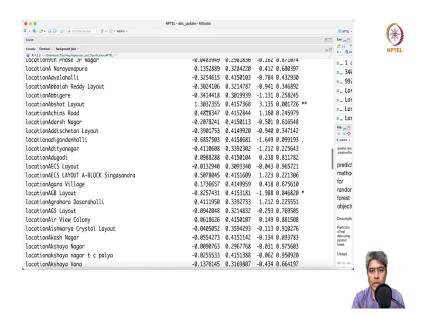
So, we will just mod 3.

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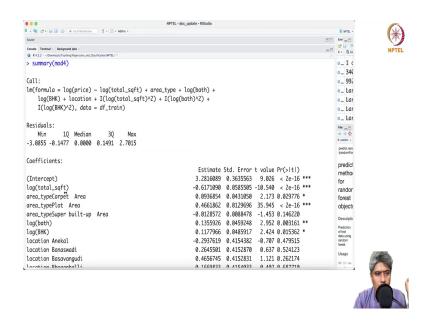
We will just tick that and whatever we have along with this, maybe we put a squared term of this, a square term of that plus I log of bath square plus I log of BHK square. So, I just want this. It takes a little time. Yeah, it is done. So, I just put a summary of mod4, model 4th model, ok. It is similar to 83 percent.

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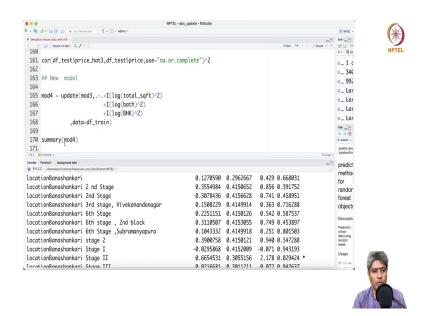
Not much. Let me just little bit increase the place. If we can just emit more space. Yeah. And see a shot layout Ambedkar Colony, AGB Layout, ok. These are like a shot layout, ok. 8th Block Jayanagar as in. Anyway, we will see what we have here. (Refer Time: 07:31). So, then these third stage. So, what we are seeing here, ok.

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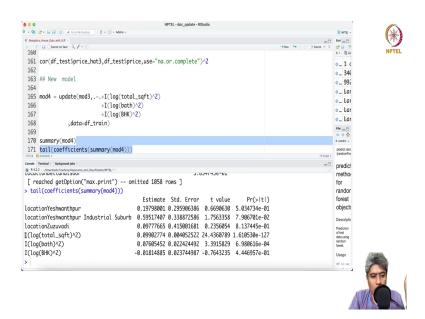
There is some issue. It has square terms, but we are not seeing the square terms, ok. Maybe they have added the square terms at the end. So, but they are not ending it here.

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So, what we will do instead of that, we will just say coefficients mod 4, ok; it is just, ok. It is just coeff with this and this (Refer Time: 08:29), ok. And maybe I will just say tail of this tail or yeah. So, you can see at the end, the it is added these parameters.

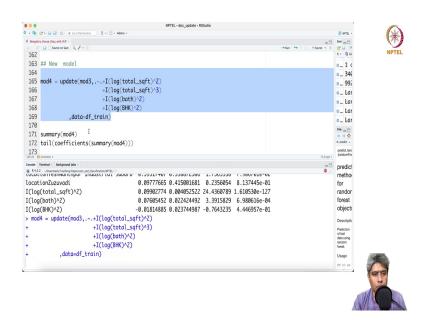
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So, you can see that the t value for log total square feet square is very high. Log bath square is also very high. And log BHK square does not have much effect. t value is very small. So, square quadratic effect for bath in log scale and total square feet in log scale does have a quite significant effect. Looks like.

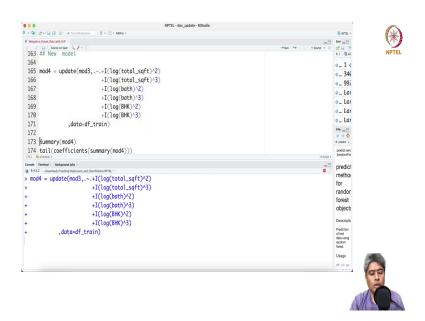
(Refer Time: 09:16); what we can do is you can keep adding more and more samples, more and more things, so maybe you can try one more. Total square feet cube. I just, ok.

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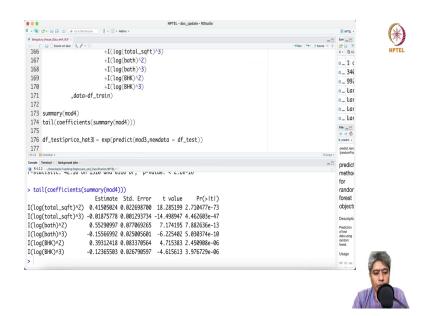
4 and then we just see this. Yeah, both square and cube does have effect looks like. Bath square does have a effect. So, What about bath cube, and BHK cube?

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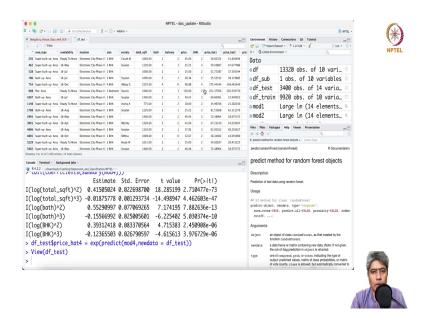
Let us run this, ok. So, if I just add the end. So, BHK square and BHK cube both are now effective. Bath square and bath cube is also effective. And square fit square and square fit cube are also effective. So, we can keep doing it. But let us see if we by doing this, by adding this predictors, engineer predictors if we really adding any value or not.

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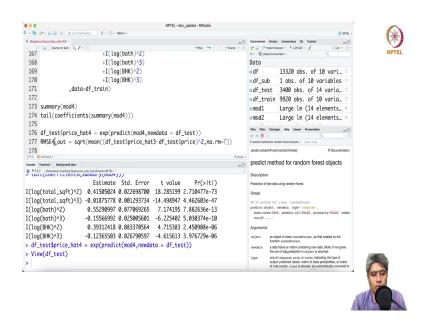
So, let us try model this test, ok, alright.

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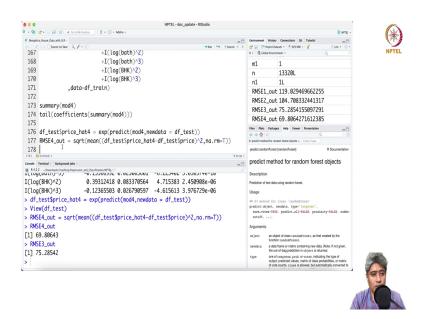
And then this is df test, this is price hat. And looks like it is doing fine, yeah. So, we will see and then let us write.

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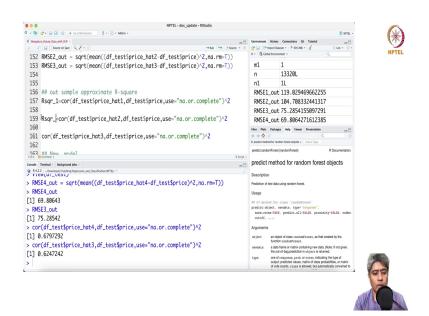
RMSE 4 out, this is 4, hat 4 and 69 whereas, RMSE 3 output 75. So, adding these adding these numbers adding these features actually helped a bit. So, you can see feature engineering is helping. So, these are out of sample remember that. These are out of the sample RMSE, root mean square error.

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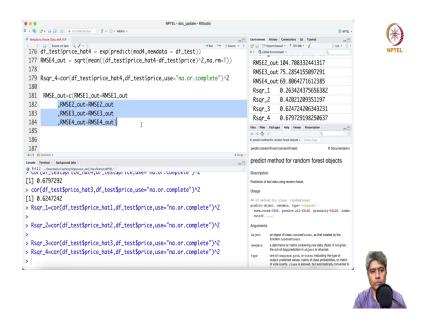
So, probably this is a good thing to have and 4 (Refer Time: 13:26). So, let me take my 4 and 0.679 whereas, my this is 62; this is even pushed further 70 percent. So, model 4 is so far best, right. So, I can just put it there R, to R square 1.

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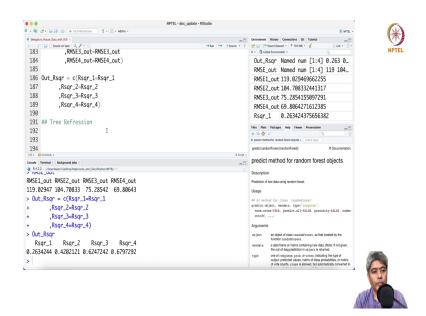
These are obviously out sample R square 2, 3 and this is 4, right. And so, we can see (Refer Time: 14:44) 1, 1, 2, 2.

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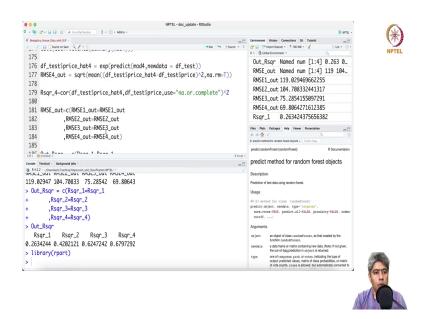
So, clearly RMSE has dropped over on, 4th model is much better. And out of the sample 4th model is this, and then R square 4 equal to R square 3, R square 2 equal to R square 2, R square 1 equal to R square, right.

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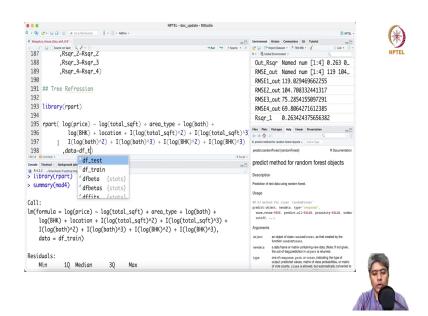
And sample R square, R square is this. So, it has gone up to 70 percent 67, 68 percent 67.9 is the maximum out of the sample R square that we can found. So, what we now we can try? We can also try implement tree regression, tree regression, ok. So, tree regression is way we can do that library R part, ok, R part, ok.

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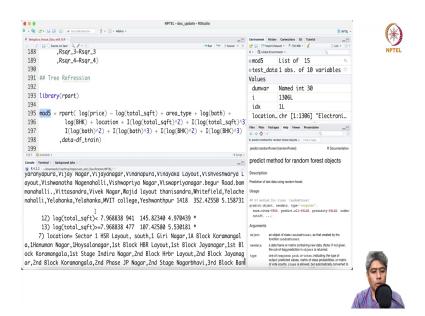
And then, then model4 dot mod4. So, what we can do is essentially I can just fit R part and then I just run it. So, this is the formula, right, ok. So, y naught data equal to df train.

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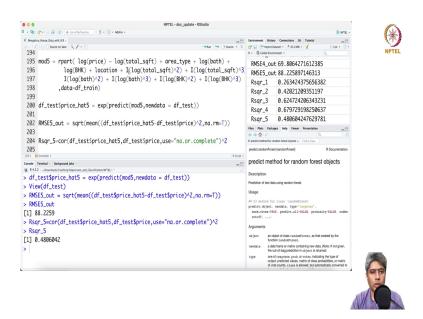
Well, this is mod3, no mod5. I hope this will be ok. This has given me something.

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And then alright, quite complicated.

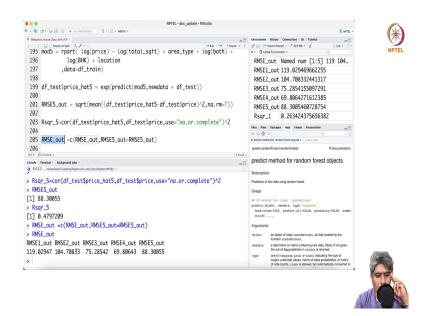
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Let us now try to; let us use it as a black box. First is, we have to predict the model 5 as a black box let us see how it is doing, ok, looks like it is doing ok. And then RMSE 5 and RMSE square, RMSE 5 out this and this 88; RMSE 5 as this, alright. So, this is some what not doing so, when the regression tree or what you can do you know what, you just drop this, if you just drop this engineered feature and let us see what it does in the. So, RMSE (Refer Time: 20:50) similar not much.

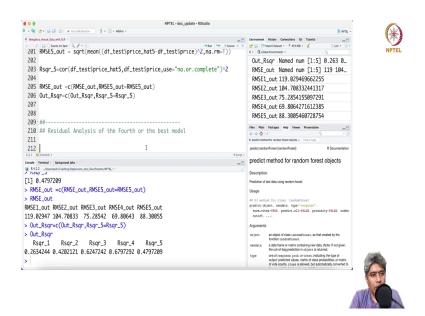
So, whether you put the engineer feature or not tree regression, tree is doing slightly worse than I would say the RMSE out is, RMSE out in out comma is equal to out, RMSE out. So, now, so we can see that it is some doing somewhere between third model and the second model.

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And R square 5 is been out (Refer Time: 21:40) R square 5 equal to Rsqr 5.

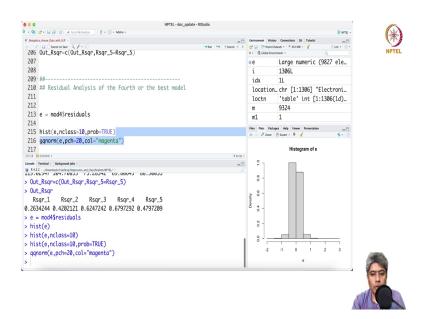
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So, out of R square is also here also it is doing somewhere in between second model and third model. So far the third 4th model is the best model that we have find. Now, since 4th model is the best model what we will do we will try to do some residual analysis of the 4th model, ok, residual analysis of the 4th of the best model. So, you can if you want to take a break you can pause the video, you can take a break and come back and see it because now we are going to turn a bit, ok.

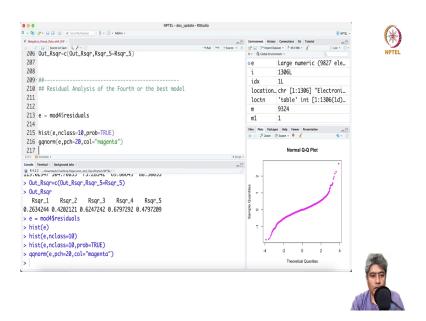
Alright, I hope you have taken your break and let us try to do the residual analysis of 4th model of the best model. And we hope that our 4th model has done reasonable job in terms of the fitting the; you know now here is the residuals.

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So, let me just take it as e, ok. Now, first thing probably what we will do, I will just put hist equal to e. Let us see how the histogram looks like. Looks like its normal n class equal to 10 if I just do that, I do not know, alright. Probability equals to true. And then what we do is we can try to do q q norm as e and then pch equal to 20 colour equal to say magento, ok.

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That is not very good. So, that means, definitely the qq line lwd equal to 20 2. So that means, this error is heavily heavy tail distribution, error has definitely a heavy tail distribution. Though it is behaved like a bell shaped, it as doing reasonably bell shape, but it is definitely a as a heavy tail distribution on both sides, ok. On both sides there is some quite a bit of underestimation and overestimations are happening.

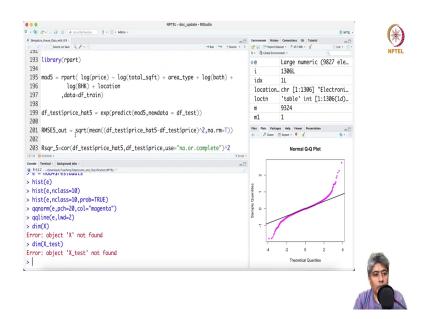
So, in this case I mean effectively if your prediction is doing well, probably you do not want to be your it should be fine. But at the same time if it is heavy tail; that means, you should be aware that there are cases where it is either doing heavy underestimation or heavy over-estimation. So, that means, these are the points where this probably happened heavy over-estimations and these are the places where heavy underestimations have happened, right.

So, in this case, what can we do? I mean you have to be if you take it as with a pinch of salt then you say that, ok I am fine with this, right. And or you trying to put more features and you try to figure out if you can tame this underestimation or overestimations.

So, one way to put this underestimation and overestimation under control is put more and more new features which probably affect the price you brought those into the in your analysis. Just not location and bathrooms and how many BHKs, and you know all the only and total square feet area types. These are the only 5 variables effectively we have used. But other than that you should use other variables also, if you have available.

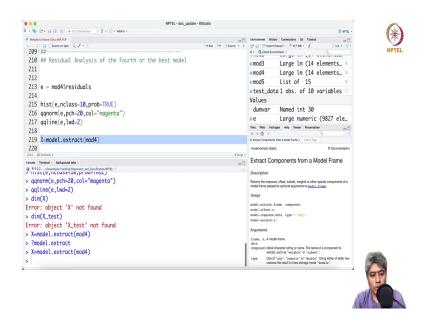
Now, for example, ready to move. You can try to add those variables as well. So, now if you want to still do the you know analysis, say whether if you are interested in doing inference statistical inference, so statistical inference will probably in this analysis will be valid. You can ask me why, because the sample size even in the training sample you have 9000 samples whereas, your dimension of your x is so maybe x test; wait a minute.

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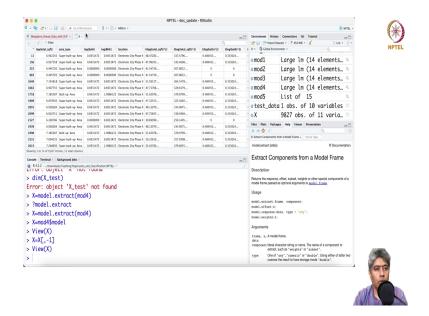
So, what you can do is sorry now what I have to do probably, I will tell you exactly what will be the model. So, model4, mod4, model dot extract, model dot extract, extract, model4, x and so, model dot extract and mod4. That is it, ok.

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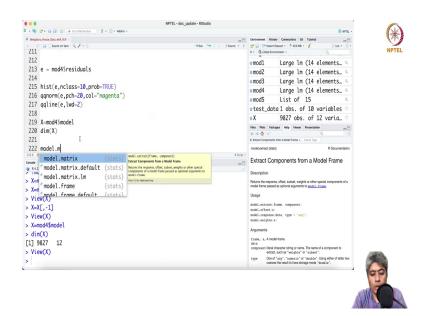
Or, one way of doing it is simply mod4 dollar model, if you do that. And so, first then is equal to x comma minus 1.

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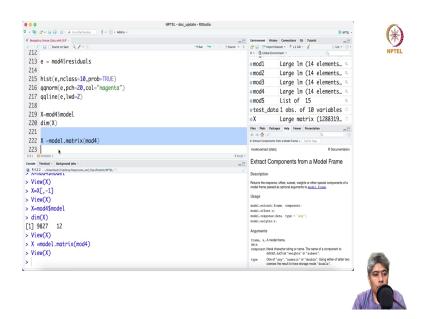
So, the number of actually dimension of x, just run it, so 12. So, you have 9827 training samples that you are using that model 4 have used and there are only 12 parameters.

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But if you put all locations, ok; that is where you need the locations fine, alright. So, model dot matrix mod 4, I think if you just say x; and now if you are saying that we have intercept log square feet area type, and then you are getting all the locations dummy variables.

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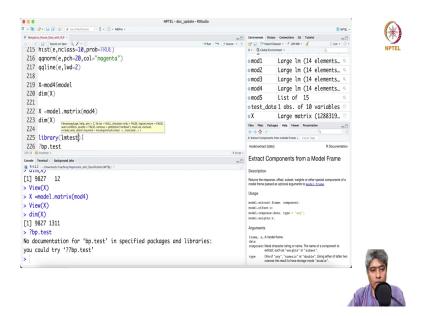


And then, if you put dimension of x, then what you will get is, ok 9827 samples and 1311 columns you are fitting it is a dimension. So, it is just 2th n x 10th a bit of a high dimension I would say, but not bad. So, you have about for each parameter you have about 10 samples. So, not bad, I would not say not bad.

So, probably, probably central limit theorem will kick in and you will be able to do the analysis reasonably, ok. I do not think you will be facing much of a trouble in this case. So, this the testing of hypothesis for the coefficients are not valid this argument probably will not be, I mean is ok, not be correct, but you can probably say reasonably that central limit theorem probably will kick in and your testing of hypothesis based on these coefficient of t value and should be fine.

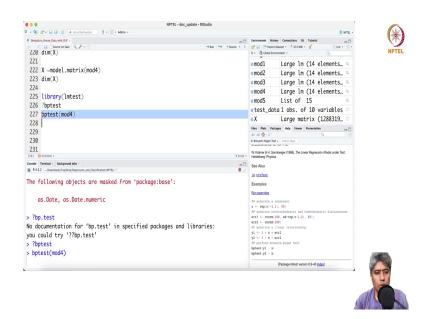
But you have to be careful that there are certain cases where you are doing quite a bit of underestimation and overestimations. So, one thing one should do that you should do Breusch Pagan test bp test, right, bp test, ok.

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Now, I think this will come under library. I am not, if am not making, a mistake I think it is under library lm test I think bp test. Yes, Breusch Pagan test, lm test, correct, correct, ok.

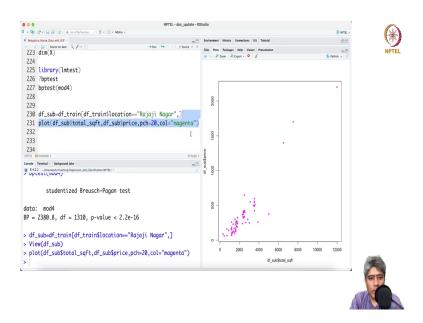
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So, may be what I will just do that I will just make a mod4. So, it takes times in general, ok. So, even Breusch Pagan test is rejecting so that means, there is quite bit of heterogeneity is there, heterogeneity is there. So, let us try to see how the heterogeneities are there. Let me see. The location the coefficients. What we can do is very simple is, let us take few places like say Rajaji Nagar or something, right.

So, let us take this kind of places and we can try to take a df sub create a sub value and let us try to understand. So, this in these area where these are the values that we have.

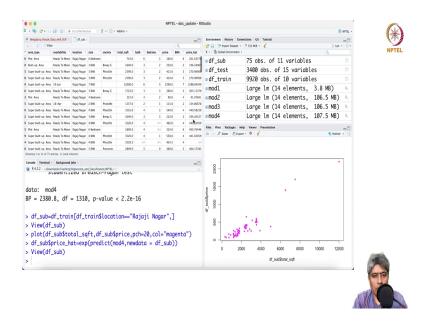
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And for these values df sub s what we will have is, we can plot the df sub dollar square feet comma df sub dollar price df sub equal 20 and color equal to magenta. So, this is pretty much data that we have. And then if we; so, this is the data that we have. So, this is the total square feet and this is the data. And now, if we do a df sub in the df sub dollar price hat, equal to exp.

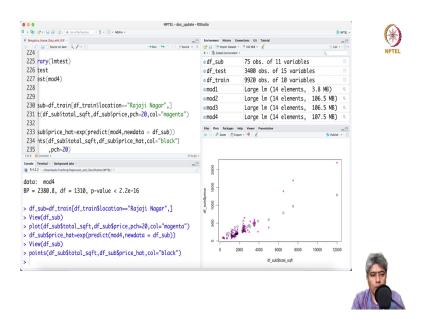
What we can do is mod 4, let us take mod 4 and new predicator which we have to first credit mod 4 comma new data equal to df sub, just for Rajaji Nagar, we are doing the prediction for Rajaji Nagar in this case, ok. So, let us see df sub. So, now, I have price, predicted price for these values.

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So, most of the places I have values there are few cases where I do not have values like NA. So, I have NA is here, so which I cannot do much. And then what I can do is essentially points; I can plot is essentially this comma df price hat is color equal to black, alright. Let us try to get that pch equal to 20.

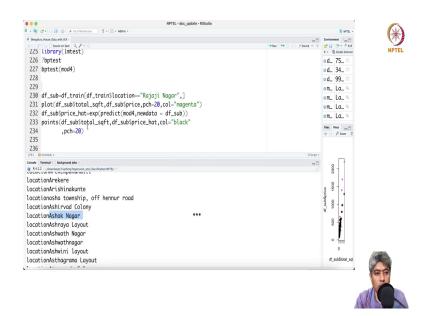
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So, this is where we are doing and these are the points, this model missing these points, you can see that the large points this point is underestimating, clearly underestimating, ok. And that is why we are seeing for different here it is trying to do very good, because we have all the values and all these things, but here clearly it is bit of underestimating.

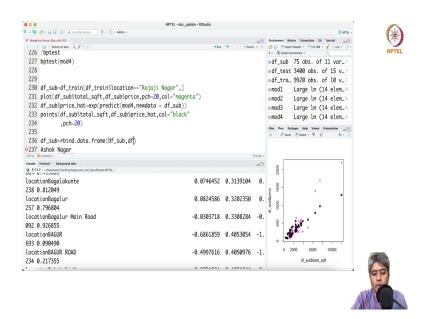
So, now similarly, if we just go and take another area. So, we did for say other than Rajaji Nagar. Here I think we have the Rajaji Nagar, alright.

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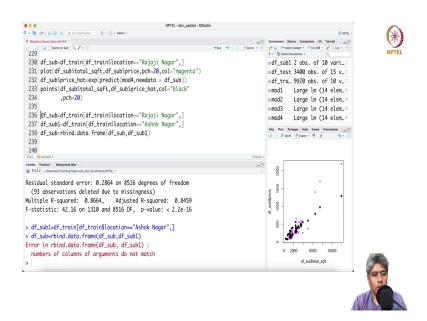
Let us try to take summary mod 4. And what is this? Ok, Ashok Nagar. Let us see how this happens, ok. Now, what am going to is very interesting; that we are going to be a bit of interesting thing. I am going to create a data set which is R going dot data dot frame with df sub and df sub 1.

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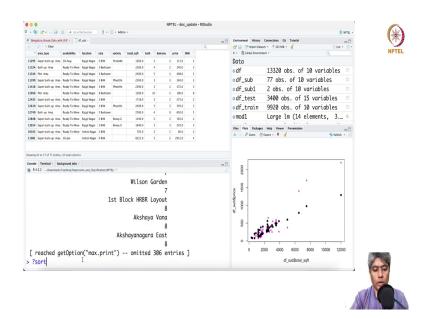
Now, you can tell me what is df sub 1. I have no I do not have any df sub 1, but I am going to make 1; that is df train and here and instead of Ashok Nagar. This is at Ashok Nagar. So, df sub 1 will have, right, ok, alright. So, ok I will do this, ok. Let me just do this guy.

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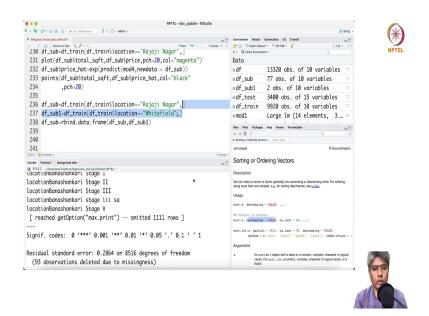
Run it once more and now it is fine. Now, if you look into the df sub, it has first Rajaji Nagar datas and then two Ashok Nagar, ok. That is where the problem probably, ok. So, what I will do is df dollar location, table, and sort; wait a minute sort descending is equal to true. Descending equal to true.

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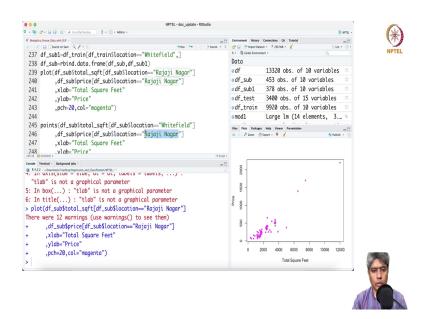
First, I do not know why it is not happening. So, I can, I want few more data set actually. I want a location with a little bit more data set.

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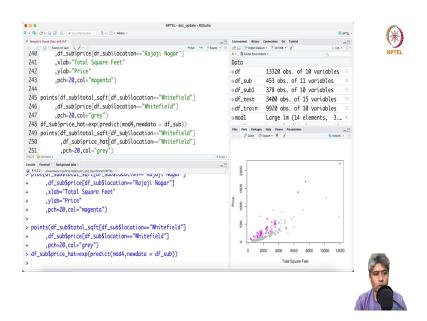
Summary equal to data, mod 4, maybe white field alright. So, maybe white field, ok. So, I have first Rajaji Nagar, then I have a bunch of white field, ok. Now, what I am going to do is first plot all the Rajaji Nagar cases; df sub (Refer Time: 43:51), ok. So, I have to put some x label to do this, total square feet square feet, and t lab equal to price, ok. Otherwise it is taking (Refer Time: 44:35), ok. So, I got that, alright. And then, I am going to put these points, points. And it is going to be white field, ok.

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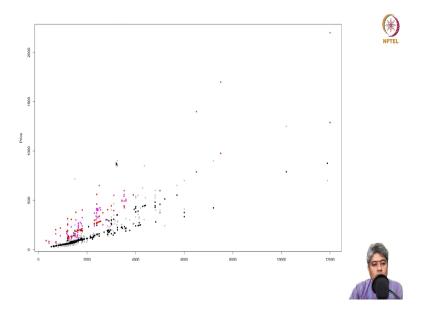
So, this is a bit of a different issue or grey. I think I can put a grey that will be probably better number, ok. Now, if you do the prediction, now if you do the prediction, and first, we are going to put the points, bunch of points for instead of price, 50 price hat.

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But instead of grey using black, and ok. And here you have bunch of red and Instead of this, you just see Rajaji Nagar set. So, let me just zoom it. So, the magenta is the actual numbers.

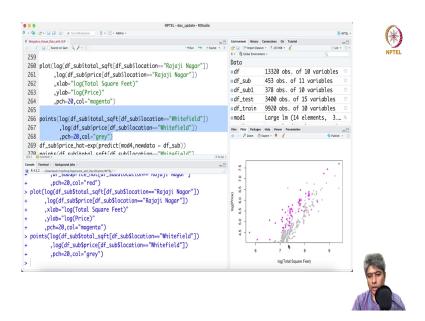
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And you can see that rates are the actual the predictions. And then there is quite a bit of underestimations are happening. Whereas, the model here, it is doing pretty good in terms of you can see this, it is actually able to pick this, you know this kind of log linear behavior to an extent, right. It is quite great, actually in that sense.

And then we can try to put the same thing using maybe. Another plot I will just create out of it with log linear. Since, these are all long linear, I will try to put it in log linear scale. So, log of this and log of price in log scale total square feet log scale log of price. So, if you just plot this, so you can see that this is better and then if you just plot log of this and log of that; this is also, to an extent.

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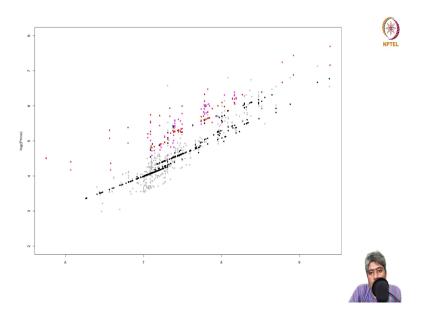


But so, but I need to, I think quite a few are actually down. So, maybe I will just increase the y limit, c from maybe from 2 to 8. I will just get 2 to 8. You can see systematically, the price on the white field is like, lower than the Rajaji Nagar. You can I mean, clearly this is the Rajaji Nagar. These points are in Rajaji Nagar. And whereas, these points are in the white field. Now, white field also when it, when the size of the house increases that time in terms of total square feet, the gap they are kind of overlapping.

At the, but at when the size of the flat in terms of total square feet decreases that time you can see there is a clear cut premium that you are paying for the Rajaji Nagar compared to Whitefield. For a large house, larger house this premium on gap is not that much. The slope is slightly different.

Whereas, now you do this thing and then we have to plot this in the clock still remember that. So, now, this is the; this is the predicted values of for the Whitefield. These are the predicted values of the Whitefield. So, Whitefield does reasonably, ok.

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And if you just do this for the Rajaji Nagar with red now if you see that clearly the Rajaji Nagar's are the red points. And for the Rajaji Nagar the points are bit higher on the side, ok whereas, clearly they are on an average it is higher compared to the Whitefield. So, it is much more clear when you plot it in the log scale.

So, and that means, whenever you are doing modeling the housing price, in fact, any economic activity any economic activity which related to price, my strong and strong recommendation is always work with log price. And along the other variable with the log price, the feature of the economic activity also, like square feet in this case square feet

number of bathroom number of you know bedrooms, these are all part of the square feets and features, so take the log transformations.

The log transformations works in economics works amazingly while, beautiful because everything in economics sort of works; there is called economies of skill the economies of skill happens in the exponential scale. So, when it becomes; so, that is one of the reason you know if you can afford you should when if somebody is investing they say that you know you try to invest in larger apartment perhaps.

Because your appreciation will be better. People sometimes say that that because of the economies of skill. So, economies of skill gets captured in the log transformations. So, and we can see that visualization also clearly explain that. So, with this I will stop here. I will hope you enjoyed these particular weeks, complete week on the complete hands-on. One way to learn regression and classification using hands-on data analysis only.

I would recommend you try other models, try to apply more engineering, feature engineered features try to do some stepwise variable selections maybe Lasso, Ridge regression, try to check the multi-collinearity. I have not done any of those yet. So, if you do that on the; so far model fold looks like the best.

Try to apply all those advanced technique that we I have taught you maybe random forest on the top of this. I believe that will give you a very good results. You can improve the accuracy a much better. You can reduce the heaviness of the residual that is overestimations and under estimation to a great extent. And I hope you will enjoy this data analysis to a great extent.

So, I am going to share this code on NPTEL platform. Please download this code and try to run on your side, and check if you are able to reproduce these results. And then, try to improve these results using more feature engineer, engineered features more step-by selections very and then try to look into the variance inflation factor, maybe Ridge correction, Lasso correction you can try. All these will help you to improve the you know prediction accuracy of the model.

I hope you enjoyed it.

Thank you very much.

See you in the next week.