


DC Power Transmission Systems
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Lecture – 27

Extinction angle: Commutation margin angle for normal inverter operation of 6 pulse LCC

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Extinction Angle $\gamma = \pi - \alpha - u = \beta - u$

$$V_d = \frac{V_{d0}}{2} [-\cos(\gamma + u) - \cos \gamma]$$


$$I_d = I_s [-\cos(\gamma + u) + \cos \gamma] \quad \checkmark$$

$$V_{di} = -V_d$$

$$V_{di} = \frac{V_{d0}}{2} [\cos(\gamma + u) + \cos \gamma] = \frac{V_{d0}}{2} \left[\cos \gamma + \cos \gamma - \frac{I_d}{I_s} \right]$$

$$V_{di} = V_{d0} \cos \gamma - \frac{V_{d0} I_d}{2 I_s} = V_{d0} \cos \gamma - R_c I_d$$

For normal inverter operation $120^\circ < \alpha < 180^\circ$
 $0 < u < 60^\circ$



So, we defined a quantity called Extinction angle denoted by gamma. The definition is 180 degrees or pi minus alpha u, it is also equal to beta minus u. So, can you please let me know we got the expression for Vd in terms of a gamma and u and V d o.

Student: (Refer Time: 00:56).

So, did we get this equation V_d equal to $V_{do} \sqrt{2} \cos \gamma + u \cos \gamma$. Then did we relate I_d $I_s \gamma$ and u ?

Student: (Refer Time: 01:17).

So, we go to this relation: I_s is equal to $-\cos \gamma + u \cos \gamma$.

Student: (Refer Time: 01:30).

Then we defined a quantity V_{di} which is equal to $-V_d$. Now, this is a notation which is used for inverter operation V_{di} . So, that subscript i is for a inverter. So, for inverter the DC side voltage has an average value which is negative. So, we take the negative of that, so, that we get a positive value. So, V_{di} is a quantity I mean which is used only for inverter, it is a positive value ok.

So, if you look at V_{di} , so, V_{di} is equal to $-V_d$. So, from the first equation, I can write this as $V_{do} \sqrt{2} \cos \gamma + u \cos \gamma$. Now, what I do is I write this as $V_{do} \sqrt{2} \cos \gamma + u \cos \gamma$, I use a previous equation. I used the previous equation which relates I_d $I_s \gamma$ and u . So, if I use this equation, I get an expression for $\cos \gamma + u$ it is nothing, but $\cos \gamma - I_d / I_s$. So, from this equation, $\cos \gamma + u$ is $\cos \gamma - I_d / I_s$ ok.

So, this is equal to. So, finally, we get as V_{di} as $V_{do} \sqrt{2} \cos \gamma + \cos \gamma V_{do} \cos \gamma - V_{do} I_d / I_s$. So, I write this as $V_{do} \cos \gamma - V_{do} I_d / I_s$. So, you recall we had defined a quantity called r_c denoted by r_c which is nothing, but V_{do} / I_s . So, I can write this as $R_c I_d$.

So, R_c is the equivalent commutation resistance which is defined as the ratio of V_{do} to I_s ok. So, that relates a $V_{di} = V_{do} \cos \gamma - R_c I_d$. Now, why we need this definition γ ? There is a purpose for all the definitions. See if you look at the previous definitions α is a

straightforward thing I mean it was the delay angle. Why was beta required? What is the definition of beta? $180 - \alpha$. Now, what did we need that definition? Now, that was because if you look at the commutation margin angle, the commutation margin angle is more relevant for inverter.

So, if you take the case of u equal to 0 or l equal to 0, the simplest case the ideal case of l equal to 0; say we studied that case only for the sake of starting with the simplified case, so that we do not jump directly to complications in practice there is a non-zero l . So, when l is 0 what is the commutation margin angle? There is one more notation ψ commutation margin angle, the duration for which the voltage across a valve is negative after it stops conducting. So, that should have some minimum value. So, that ψ was equal to. So, for inverter operation.

Student: $180 - \alpha$ (Refer Time: 05:55).

So, its $180 - \alpha$ that is nothing, but beta. So, the purpose for defining beta was it is nothing, but the commutation margin angle; beta is nothing, but the commutation angle for inverter operation. So, for inverter operation, the commutation margin angle is relevant. Say for a rectifier operation actually it is not. So, say for α less than 60 degrees you get actually a rectifier operation, for which the commutation margin angle is not equal to beta; only for inverter operation it is. In fact, for any value of α greater than 60, the commutation margin angle is actual equal to beta ok.

So, that was the purpose. Now, we see that the new definition extinction angle also happens to be the commutation margin angle for normal operation. So, here also what is a relevant is inverter operation. So, we normally get the commutation margin angle almost close to the minimum required. Say the commutation margin angle should not go below a certain value. So, there is some threshold value. So, it can go near only for inverter operation.

So if I consider normal inverter operation; for normal inverter operation, see normal means what happens in practice normally. See abnormal means due to some fault or I mean due to some unforeseen situation you can have an inverter operation which is not normal, but most of


the time it is normal. So, for normal inverter operation what we have is alpha; see I did not say what is the range of alpha for normal inverter operation, ok.

So, I am just making a statement, we will look at more details of what should be alpha for inverter operation. Now, it is not as simple as the case of l equal to 0. So, for l equal to 0 there was only alpha was the only angle. So, if alpha is less than 90, it is rectifier operation greater than 90 inverter operation.

Now, it is not just alpha there is also a u . So, it is not straightforward, but what I would say is I am not talking about the range of alpha for inverter operation, I am just saying the range of alpha for normal inverter operation. So, it is actually greater than 120 degrees and less than 180 degrees.

Of course, it is much less than 180 degrees, its I mean it cannot go near 180, but what I am trying to say is the maximum value is of course, less than 180. Now, let us see what is the commutation margin angle for normal inverter operation and of course, we also have u ; u is an angle which is between 0 and 60 degrees. So, let us see why we define a quantity called extinction angle gamma.

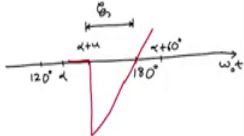
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Normal Inverter Operation

$\alpha > 120^\circ$
 Valve 1 stops conducting at $\alpha + u$
 $0 < u < 60^\circ$
 Up to $\alpha + u$, voltage across valve 1 = 0
 For $\alpha + u < \omega t < \alpha + 60^\circ$, voltage across valve 1
 $= e_a - e_b$
 $= -\sqrt{2} V \sin(\omega t)$
 Negative to positive zero crossing
 is at $\omega t = 180^\circ$
 $\therefore \alpha + u$ should be less than 180°
 Since $\alpha > 120^\circ$, $\alpha + 60^\circ > 180^\circ$

Voltage across
valve 1



$\delta = 180^\circ - (\alpha + u)$
 For normal inverter operation,
 $\delta = \gamma$



So, if I consider normal inverter operation, so for normal inverter operation alpha is greater than 120 degrees. So, if I take the voltage across say valve 1, so, valve 1 stops conducting at alpha plus u, where u is the overlap angle and u is greater than 0 and less than 60 degrees. So, it actually means that up to alpha plus u voltage across valve 1 is 0.

So, what happens after alpha plus u? So, if I consider a omega o t greater than alpha plus u and less than alpha plus 60 degrees, so, in this duration what is the voltage across valve 1? This is the duration immediately after valve 1 stops conducting, so, voltage across valve 1. So, this voltage is e a minus e b. So, e a minus e b is a line voltage, so it is equal to minus root 2 V sine omega o t. So, this voltage across valve 1 has a negative to positive 0 crossing at omega o t equal to 180 degrees. So, the negative to positive 0 crossing of this voltage across valve 1 is at omega o t equal to 180 degrees.

So, this actually gives the reason for $\alpha + \mu$ to be less than 180 degrees. So, otherwise the voltage across valve 1 will not be negative after it stops conducting. So, therefore, $\alpha + \mu$ should be less than 180 degrees. Of course, if I try to plot the voltage across valve 1. So, let me plot this voltage across valve 1; voltage across valve 1. So, if I take the voltage across valve 1 up to $\alpha + \mu$ this voltage is 0. So, let me show a few values of ωt suppose this is say 120 degrees.

So, α should be greater than 120 degrees and this is 180 degrees. Now, since α is greater than 120 degrees, $\alpha + 60$ degrees is greater than 180 degrees, so that means, I consider this range of ωt between all $\alpha + \mu$ and $\alpha + 60$ degrees. So, $\alpha + 60$ degrees is actually greater than 180 degrees. So, $\alpha + \mu$ is between 120 and 180 degrees. So, for the sake of having a minimum value of the commutation margin angle, I should have $\alpha + \mu$ less than 180 degrees.

So, if I plot the voltage across valve 1, so, up to $\alpha + \mu$. Suppose, I show α here then $\alpha + 60$ degrees is greater than 180 degrees because α is assumed to be greater than 120 degrees which is true for normal inverter operation. So, this is $\alpha + 60$ degrees. So, at some instant $\alpha + \mu$ valve 1 stops conducting.

So, the voltage across valve 1 is 0 up to $\alpha + \mu$ then the voltage across valve 1 is minus $\sqrt{2} V \sin \omega t$. So, it is a wave form like this. So, this wave form is applicable up to $\alpha + 60$ degrees. So, if you look at the commutation margin angle that is the duration for which the voltage across valve 1 is negative after it stops conducting. So, this duration is the commutation margin angle ψ .

So, if we look at the commutation margin angle ψ then we can see that this is equal to 180 degrees minus $\alpha + \mu$ now which is nothing, but the angle that we have defined as a γ extinction angle which is given by 180 degrees minus $\alpha + \mu$. So, we see that whenever we have normal inverter operation the commutation margin angle is γ . So, that is the purpose of defining this quantity γ and is called extinction angle. So, for normal inverter operation the commutation margin angle ψ is equal to γ .

