

DC Power Transmission Systems
Prof. Krishna S
Department of Electrical Engineering
Indian Institute of Technology, Madras

Lecture - 11

Analysis of 6 pulse LCC neglecting inductance: Average DC side voltage

(Refer Slide Time: 00:20)

Average DC voltage,

$$V_d = \frac{1}{\pi/3} \int_{\alpha}^{\alpha+60} v_d d(\omega t) = \frac{3}{\pi} \int_{\alpha}^{\alpha+60} (e_{1s} - e_{2c}) d(\omega t) = \frac{3}{\pi} \int_{\alpha}^{\alpha+60} \sqrt{2} V \sin(\omega_s t + 60^\circ) d(\omega_s t) = \frac{3\sqrt{2}}{\pi} V \cos \alpha$$

V_{d0} ← Maximum average DC voltage
 $V_d = \frac{3\sqrt{2}}{\pi} V$
 $V_d = V_{d0} \cos \alpha$

Average power = $V_d I_d$
 If $0 \leq \alpha < 90^\circ$, $V_d > 0$, average power > 0
 Then converter operates as a rectifier

Circuit diagram: A DC voltage source V_d is connected to a load. The current I_d is constant and flows from the positive terminal.

That is the average DC voltage, average DC voltage or average DC side voltage. So, we use a notation for this V uppercase V with a subscript d. Now, can I use the table and try to get a average value of the DC side voltage? If there is 1 cycle and in 1 cycle there are 6 intervals, the waveform of the DC side voltage actually repeats 6 times, is that a result well known to you?

Student: Yes.

So, I use that information. So, I know that there is I mean there are actually 6 intervals in 1 cycle and waveform repeats. So, the frequency of the DC side voltage is 6 times the frequency of the.

Student: AC side.

AC side voltage. So, if I want the average, I need not do an integration over 2π radians, I can just do it over 2π by 6 radians ok. So, what I can do is I will try to take any 1 interval, 1 interval is of duration 60 degrees that is 2π by 6. So, I will just integrate over 1 interval of duration 60 degrees and get the average value. So, 2π by 6 or π by 3, so 1 by π by 3. So, I can take any of the 6 intervals. Now, so the first interval is from α to α plus 60 degrees.

So, if I take the first interval in from the table, I have to just substitute for the instantaneous V_d ok. So, its integral of α to α plus 60 degree of V_d with respect to $\omega_o t$ divided by π by 3, so that is the expression for average DC voltage. So, that is equal to 3 by π integral from α to α plus 60 degrees. V_d from α to α plus 60 degrees, you know the expression for V_d , the instantaneous V_d from α to α plus 60 degree now when we got.

Student: e_b minus e_c .

e_b minus e_c , integrate with respect to $\omega_o t$, $\omega_o t$ is the angle; so or independent variable is angle. So, we are not using time as the independent variable, ω_o is the operating value of angular frequency. See that subscript o is for operating value and ω is the usual angular frequency. So, ω_o is the operating angular frequency.

So, this is equal to 3 by π integral α to α plus 60 degrees and of course, e_b minus e_c is $\sqrt{2} V$. So, from the expressions for e_b and e_c I can get the expression for e_b minus e_c

it is $\sin \omega t$ plus phase angle which is, so e_b is having a phase angle of 30, e_c is having a phase angle of minus 90, so minus e_c will have a phase angle of.

Student: (Refer Time: 03:40).

Plus.

Student: (Refer Time: 03:43).

Now, can I straight away; see I am can I straight away write the expression for e_b minus e_c ? So, what is it? Plus.

Student: Plus 60 degrees.

Plus 60 degrees yes. So, I mean this is straight forward integration. So, if you integrate this you get and I will leave it to you to derive this $\frac{3\sqrt{2}}{\pi} V \cos \alpha$ ok. Now, if you recall we had 1 more quantity V_d , do you recall this? This notation V_d there is another subscript o, what is this V_d ?

Student: (Refer Time: 04:31).

Sorry.

Student: Average DC voltage (Refer Time: 04:36).

Yeah maximum, so we use this notation in the context of trying to obtain a general converter circuit ok. So, if you use this notation for maximum average DC voltage. So, what is the maximum average DC voltage in this case? Look at the expression for V_d V_d is the average DC voltage. What is the maximum possible value? So, maximum is obtained by choosing an appropriate value of α ; so, for a particular value of α .

Student: Sir.

If alpha is 0 we get the maximum value. So, that is $3 \sqrt{2} \text{ by } \pi \text{ into } V$ is the maximum average DC voltage. So, that is V_d . So, therefore, I can relate V_d and V_d , V_d is $V_d \cos \alpha$ ok. So, this is something which is applicable for the circuit we considered irrespective of the operation of the converter as a rectifier or an inverter. So, these are not dependent on how the converter operates; whether it operates as a rectifier or an inverter. Now we have to see, when we get rectifier operation and when we do not get rectifier operation or when we get inverter operation? So, when do we get rectifier operation?

Student: (Refer Time: 06:14).

Alpha is.

Student: Less (Refer Time: 06:17).

Less than.

Student: 90.

90. So, you see on the DC side, if you look at the DC side of the converter our assumption is a constant current. So, the DC side has a plus terminal and a minus terminal the voltage across the DC side is V_d . So, I am not drawing the entire circuit diagram, the DC side of the converter has 2 terminals ok, the voltage across the terminals is V_d . And I have a current i_d of course, i_d is positive please note i_d is positive it's a current source is positive so; that means, the converter acts as a rectifier, if the average power is flowing from the AC to DC side, that is the definition of rectifier ok.

So, a converter has distinguishable AC sides and DC side. AC side has 3 terminals, we always work with 3 phase of course, as far as this course is concerned and DC side has 2 terminals. So, if the average power flow is from AC to DC side then we say the converter

acting as a rectifier, if the average power flow is from DC to AC side it is said to operate as an inverter. So, that is the definition. So, if I look at the average power, what is the average power?

Student: (Refer Time: 07:39).

It is nothing, but the average voltage into the current that is the average power current is anyhow constant current is a constant value. Please note this i_d is constant, that is our assumption ok. So, if average power has to be positive then what should be the value of alpha? So, if alpha is greater than or equal to 0. I am sorry if alpha is greater than or equal to 0 and less than 90 degrees, then V_d is positive. Yeah, there are 2 V_d s, one should be careful I hope I am able to differentiate between the instantaneous V_d by using a lowercase v and an uppercase V by for the average value. So, the average value of V_d should be greater than 0, only then the average power is ok.

So, if alpha is between or in fact, even equal to 0 greater than or equal to 0 and less than 90, then V_d is positive and average power is positive, average power is positive. So, then the converter operates as a rectifier, then converter operates as a rectifier. Now, if it is equal to 90, if alpha is 90.

Student: (Refer Time: 09:40) neither.

Its neither a rectifier nor a inverter, there is no power flow both; I mean when V_d is 0 power is 0 ok. Suppose alpha is greater than 90, then we get a negative value of V_d , if alpha is greater than 90 we get a negative value of the average value of the DC side voltage then the power is actually flowing in the other directions then it the converter is said to operate as an inverter.

Now, we will come to that later because, I know that if alpha is greater than 90 it is inverter operation, but I still do not know for the timing being up to what value of alpha I can go. So, I will come to that a bit later. So, inverter operation will be considered just shortly, but later. So, these are a few things which we are able to obtain from the table that we obtained in the

last class ok. Now, there is a something on the AC side, say ideally on the AC side we should have voltages and currents that are sinusoidal on the DC side voltage and current should be constant.

Now, if you look at the AC side of the converter, the voltages are sinusoidal on the DC side current is constant, but the voltage on the DC side is not constant, I mean it is not a constant ok. As similarly what about the current on the AC side? The currents are not sinusoidal. So, on the AC side voltages are as required ideal, but currents are not sinusoidal. On the DC side current is ideal by our assumption it is constant, but voltage is not ideal.

So, when we say something is not equal to what is desire, then we want to find out by how much it is deviating from ideal. So, how do we do that? We want to quantify the amount by which the voltage on the DC side is deviating from ideal; from the ideal waveform and we want to quantify the amount by which the current on the AC side is deviating from what is desired. So, how do we do that?

Student: (Refer Time: 11:52).

Sorry.

Student: (Refer Time: 11:54).

Sorry.

Student: (Refer Time: 11:55).

Student: Ripple factor.

Ripple factor, yeah any other suggestion.

Student: DC side is ripple factor AC side is total (Refer Time: 12:09) discussed.

Yeah. So, finally, it is some frequency which is appearing and it should not be there say on the DC side we want only DC quantity, but there are other periodic waveforms. So, the point is there are other periodic waveforms that are appearing on the DC side in the in the case of voltage. On the AC side as well we want only fundamental, but we do not have DC on the AC side, but we have some other harmonic components.

So, a very nice way of trying to quantify this is using what is known as harmonic components and that we can do by the use of Fourier series ok. So, what I will do is, I will try to briefly give the results of Fourier series without we getting into any derivations. So, that you are familiar with the results and one can use directly ok.