

Analog Electronic Circuits
Prof. Pradip Mandal
Department of Electronics and Electrical Communication Engineering
Indian Institute of Technology, Kharagpur

Lecture – 89
Numerical Examples on Current Mirror and its applications (Part-D)

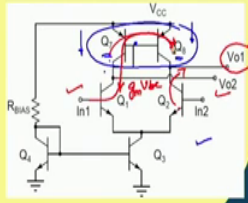
(Refer Slide Time: 00:28)


Numerical example on Differential amplifier having CM (using BJTs)

- **Example 10:**
- Assume that, $V_{BE(on)} = 0.6V$ and $V_A = 100V$, β 's are very high
- Q1 and Q2 are identical, Q3, Q4 and Q5 are identical,
- Q7 and Q8 are identical
- $R_{BIAS} = 11.4 k\Omega$, $V_{cc} = 12V$, $V_T = 26mV$

For a "meaningful" input common mode bias

(i) Find d.c. currents through all transistors of the circuit





Yeah. Welcome back to our next example. So here we do have the differential amplifier and the load of course, it is active load, but internally we do have current mirror. So, what we are expecting here it is transistor 7 DC wise it will be mirroring its own DC current into transistor 8 and that is good. In fact, we want this current should also be same as this 1 from balance point of view. So, we do not have to put any external circuit to bias here and in addition to that this transistors 7 it may also mirror signal current, in case if we have say gm into V b current it is coming here at the collector.

So, that current is also getting mirrored here. So it is expected that the signal it is whatever the differential signal or common mode signal, it will be arriving to this output through this transistor 2 as well as through transistor 1 and then through the current mirror. So, we will see the consequence in this numerical example I hope you recall the analysis we have done for this circuit.

So, in the numerical examples we will be reestablishing the same thing, to start with we do have to find the DC currents through all the transistors.

(Refer Slide Time: 02:12)

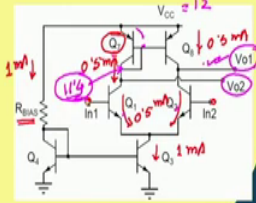
Numerical example on Differential amplifier having CM (using BJTs)

• Example 10:


- Assume that, $V_{BE(on)} \approx 0.6V$ and $V_A = 100V$, β 's are very high
- Q1 and Q2 are identical, Q3, Q4 and Q5 are identical,
- Q7 and Q8 are identical
- $R_{BIAS} = 11.4\text{ k}\Omega$, $V_{cc} = 12V$, $V_T = 26mV$

For a "meaningful" input common mode bias

(i) Find d.c. currents through all transistors of the circuit



$(1 + \frac{V_{CE}}{V_A}) \approx 1$



Again the value of this register it is 11.4 k, so that makes this current equals to 1 milliampere. So, the current flow here it is also 1 milliampere and if we are applying meaningful input common mode DC then half of the current is flowing here and remaining half it is here. So,

each one of them it is 0.5 milliampere so this 0.5 milliampere it is getting mirrored here. So, the current flow here it is 0.5 through transistor 7 as well as transistor 8.

Now yeah so it is now it is pretty straightforward so if you if you ignore this early voltage to calculate the nominal quiescent current, namely $I_{CQ} \approx I_{CQ} + V_{CE} / V_A$ if you consider it is approximately equal to 1 for DC condition DC current. Then the circuit analysis it becomes really simple and also we like to say that since this is transistor 7 it is diode connected.

So, the voltage here it is decided by the 12 volt minus 0.6 so the voltage here it is 11.4. In fact, it can be shown that the DC voltage at this point assuming Q1 Q2 identical Q7 Q8 identical it is also 11.4 volt. So, I should say DC voltage at output 1 and output 2 both are 11.4 volt, now with this information let us calculate the small signal gain namely differential mode gain and common mode gain in the next slide.

(Refer Slide Time: 04:30)

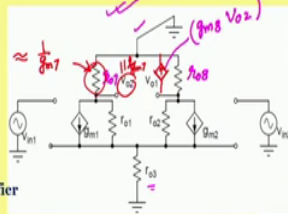
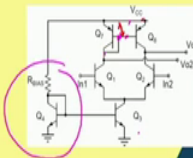
Numerical example on Differential amplifier having CM (using BJTs)

• Example 10 (contd.):

- Assume that, $V_{BE(on)} = 0.6V$ and $V_A = 100V$, β 's are very high
- Q1 and Q2 are identical, Q3, Q4 and Q5 are identical,
- Q7 and Q8 are identical
- $R_{BIAS} = 11.4\text{ k}\Omega$, $V_{cc} = 12V$, $V_T = 26mV$

For a "meaningful" input common mode bias

- Find d.c. currents through all transistors of the circuit
- Find the differential mode gain and common mode gain of the amplifier

So, yeah so now our next calculation it is we need to find differential mode gain and common mode gain. And here we do have most of the small signal model this part of course, we are in the small signal model we are removing we are keeping only r_{o3} and on the other hand for transistor 8 we do have r_{o8} and then r_{o7} . In fact, since it is diode connected we should also give this r_{o7} in parallel with $1/g_{m7}$.

So, the voltage coming here V_{o2} it is predominantly it will be defined by $1/g_{m7}$ and whatever the signal current is flowing through this. So, approximately we can say that this resistor it is $1/g_{m7}$, so then whatever the voltage it is producing here that voltage it is also deciding the V_b voltage of transistor 8.

So, through the transistor 8 there will be a current flow, signal current flow and this signal current flow. Of course, it will be it will be corresponding g_{m8} multiplied by the V_b here which is it is basically this is V_{o2} because this node it is ground.

So, the voltage V_{be} voltage it is g_{m8} multiplied by V_{o2} , so in in summary now to analyze this circuit we can just simplify and saying that this resistance it is $1/g_{m7}$ this is r_{o8} .

(Refer Slide Time: 06:34)

Numerical example on Differential amplifier having CM (using BJTs)

• Example 10 (contd.):

- Assume that, $V_{BE(on)} \approx 0.6V$ and $V_A = 100V$, β 's are very high
- Q1 and Q2 are identical, Q3, Q4 and Q5 are identical,
- Q7 and Q8 are identical
- $R_{BIAS} = 11.4\text{ k}\Omega$, $V_{ec} = 12V$, $V_T = 26mV$

For a "meaningful" input common mode bias

(i) Find d.c. currents through all transistors of the circuit

(ii) Find the differential mode gain and common mode gain of the amplifier

$$V_{o2} \approx -g_{m1} \frac{1}{g_{m7}} \left\{ \frac{V_{in,d}}{2} - V_{be} \right\}$$

$$V_{o1} = \left[\frac{g_{m8}}{g_{m7}} \left(\frac{g_{m1}}{g_{m7}} \right) \times \left\{ \frac{V_{in,d}}{2} - V_{be} \right\} + g_{m2} \left(\frac{V_{in,d}}{2} - V_{be} \right) \right] \parallel r_{o1} \parallel r_{o2}$$

$$= g_{m1,2} V_{in,d} \lambda \parallel r_{o1} \parallel r_{o2}, \quad \frac{V_{o1}}{V_{in,d}} = g_{m1,2} (r_{o1} \parallel r_{o2})$$

But in addition to that we do have a current flow here which is g_{m8} multiplied by V_{o2} and then we do have r_{o1} r_{o2} then we do have g_{m1} into V_{be1} , so this is V_{be1} across this r_{pi} so V_{be1} here.

So, likewise here we do have V_{be2} so V_{be2} multiplied g_{m2} it is giving the current here. And to get the differential mode gain what we can say we can make this voltage equals to $V_{in,d}/2$ and this voltage on the other hand it is minus $V_{in,d}/2$. And in fact, this is common node this is common node the impedance looking into this device and this device. If I ignore this part strictly speaking they are not same, the impedance looking into the source of transistor 1.

It is smaller primarily because at its collector we do have a smaller resistance compared to whatever the resistance we do have. In fact, there may be a detailed calculation by which you

can find that this voltage it is tilted towards V_{dd} $V_{in,d} / 2$ compared to minus $V_{in,d} / 2$. If the 2 resistances they are equal then only you can say this is ac ground, but whatever it is we may say that it is having V_s voltage that makes this V_{be} voltage which is this $V_{in,d} / 2$ minus V_s .

On the other hand the voltage here it is minus $V_{in,d} / 2$ and then minus this V_s and then that produces this current. And this current it is producing a voltage compared to this impedance we may ignore this r_{o1} even though it is connected to this node which is having the signal, but as the signal here it is very small. We may see that output voltage V_{o2} it is well approximated by g_{m1} multiplied by $1 / g_{m7}$.

So, that is the impedance at this node and then $V_{in,d} / 2$ minus I should not say s let it be V_e because this is common emitter voltage. So, that is the voltage you do have here so the current flow at this node on the other hand it will be g_{m8} multiplied by this voltage which is g_{m1} / g_{m7} with a minus sign multiplied by $V_{in,d} / 2$ minus V_e . So, this is the current at this point in addition to that we do have this current also, so we do have g_{m2} and then we do have minus $V_{in,d} / 2$ minus V_e .

So, this is the total current and if I multiply this current by the impedance at this node which is practically it is r_{o8} in parallel with r_{o2} , so that gives us the output voltage V_{o1} . In fact, if you see here g_{m7} and g_{m8} we may cancel it out and if I consider g_{m1} and g_{m2} they are equal then this we do have a minus sign here and minus sign here that makes it is plus and here you have minus sign so we can say even this part is also getting removed. So, with this approximation what you are getting here it is g_{m1} so we do have g_{m1} here and then of course, with a minus sign here because the current is departing this node.

So, we will be having a minus sign so this minus sign and this minus sign and this minus sign they are getting converted into plus. So, eventually g_{m1} or g_{m2} multiplied by this $V_{in,d}$, multiplied by this net output resistance which is practically r_{o8} and r_{o2} in parallel. So, if I say that final output voltage if I call this is the net output voltage V_{o1} by differential input

here which is equal to g_{m1} or g_{m2} multiplied by r_{o8} in parallel with r_{o2} on the other hand the voltage at this node V_{o2} .

So, V_{o2} on the other hand so this is equal to it is very small so whatever the voltage you do have that is getting multiplied by g_{m1} , but then that is again multiplied by $1/g_{m7}$. So, this is $V_{in,d}$ by 2 minus V_e , but whatever it is these two g_m s in the same order of magnitude as a result you may say that this voltage it is very small compared to V_{o1} . And if I say that output voltage differential output voltage V_{od} defined as V_{o1} minus V_{o2} .

So, all practical purposes it is equal to V_{o1} and then the expression of V_{o1} it is given here to find the gain differential mode gain A_d . So, that is equal to that is defined as V_{od} divided by $V_{in,d}$ and that is given by g_{m1} into r_{o8} into in parallel with r_{o2} . So, numerical value to calculate numerical value let we consider let we calculate g_{m1} and g_{m8} and r_{o2} .

(Refer Slide Time: 14:43)

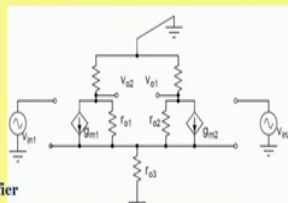
Numerical example on Differential amplifier having CM (using BJTs)

• Example 10 (contd.):

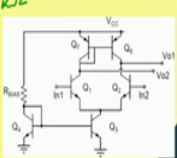

- Assume that, $V_{BE(on)} = 0.6V$ and $V_A = 100V$, β 's are very high
- Q_1 and Q_2 are identical, Q_3, Q_4 and Q_5 are identical,
- Q_7 and Q_8 are identical
- $R_{BIAS} = 11.4 k\Omega$, $V_{ec} = 12V$, $V_T = 26mV$

For a "meaningful" input common mode bias

- Find d.c. currents through all transistors of the circuit
- Find the differential mode gain and common mode gain of the amplifier



$$g_{m1} = \frac{0.5}{26} \text{ S}, \quad r_{o2} = 200 k\Omega, \quad r_{o8} = 200 k\Omega$$

$$A_d = \frac{0.5 \times 100}{26} \times 10^3 = \boxed{1923}$$



In fact, we already have done this calculation g_{m1} equals to 0.5 divided by 26. And so this is this much of more and r_{o2} equals to 200 k also r_{o8} equals to 200 k and that gives us the differential mode gain equals to 0.5 into 100 divided by 26. So, that is equal to so this into 1000 so this is equal to 50, I should say 50 divided by 26 multiplied by 1000 so that is 1923 to be more precise.

So, that is the differential mode gain, on the other hand the common mode gain. So, the common mode gain it is essentially it is a bit tricky.

(Refer Slide Time: 16:13)

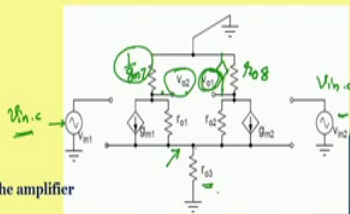
Numerical example on Differential amplifier having CM (using BJTs)

• Example 10 (contd.):

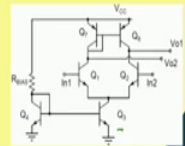

- Assume that, $V_{BE(sat)} \approx 0.6V$ and $V_A = 100V$, β 's are very high
- Q1 and Q2 are identical, Q3, Q4 and Q5 are identical,
- Q7 and Q8 are identical
- $R_{bias} = 11.4 k\Omega$, $V_{cc} = 12V$, $V_T = 26mV$

For a "meaningful" input common mode bias

- Find d.c. currents through all transistors of the circuit
- Find the differential mode gain and common mode gain of the amplifier



$$A_c = \frac{v_{o2}}{v_{in-c}} = -\frac{g_{m1}}{g_{m7}} \left(1 + \frac{g_{m1} r_{o3}}{g_{m7}} \right)$$

$$= -\frac{1}{2g_{m7} r_{o3}} = \frac{-26 \Omega}{2 \times 0.5 \times 100k \Omega} = -26 \times 10^{-5}$$



Here we do have this resistor it is practically 1 by g_{m7} , and if we apply same voltage here and same voltage here namely V_{in-c} . So, that makes this voltage and this voltage to be equal so, even though we do have r_{o8} connected here. But we do have voltage dependent current

source which depends on this voltage, making this node very insensitive or a smarter way to calculate their common mode voltage we can say that common mode gain.

Essentially, it is V_{o2} divided by V_{in} and in this circuit since we are applying same voltage here and here V_{in} with same polarity. In that case this node of course, it is remaining high impedance or rather I should say degenerated node. So, we do have this registered remaining there and it is degenerating the circuit and this gain as you have discussed before it will be the gain of this circuit which is getting degenerated by r_{o3} or if I split the circuit it will be rather 2 times of r_{o3} .

So, the corresponding gain here it is g_{m1} multiplied by 1 by g_{m7} so that is the impedance here divided by $1 + g_{m1} \times 2 \times r_{o3}$. In fact, this g_{m1} sorry after removing this 1 you can remove this g_{m1} also, so that gives us a common mode gain equals to 1 by $2 \times g_{m7}$ into r_{o3} . In fact, g_{m7} it is given to us and also yeah so it is becoming this is 26 divided by 2×0.5 milliamperes into 0.5 and then r_{o3} it is 100 k.

So, that gives us how much 26 into 10 to the power 5 minus 5 sorry. So, the common mode gain it is really very small, so that makes this circuit it is having differential mode gain it is good and then common mode gain it is quite low, the similar kind of circuit can also be constructed using MOSFET.

(Refer Slide Time: 19:38)

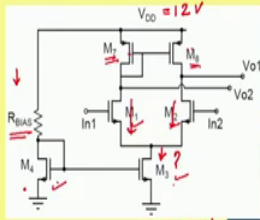
Numerical example on Differential amplifier having CM (using MOSFETs)

• Example 11:

- $(K_n, W1/L1) = (K_n, W2/L2) = 2 \text{ mA/V}^2$,
- $(K_n, W3/L3) = (K_n, W4/L4) = 4 \text{ mA/V}^2$,
- $(K_p, W7/L7) = (K_p, W8/L8) = 1 \text{ mA/V}^2$;
- $V_{th} = 1.5\text{V}$, λ 's = $0.01/\text{V}$, $V_{DD} = 12\text{V}$, $R_{BIAS} = 9.5 \text{ k}\Omega$,

For a "meaningful" input common mode bias

(i) Find d.c. currents through all transistors of the circuit



Handwritten equations and notes on the slide:

$$V_{DD} - V_{GS4} = R_{BIAS} \times I_{REF} = R_{BIAS} \times \frac{4\text{mA}}{2} \times (V_{GS4} - V_{th})^2$$

$$V_{DD} - V_{th} - (V_{GS4} - V_{th}) = 19(V_{GS4} - V_{th})^2$$

$$9.5 - x = 19x^2 \Rightarrow 19x^2 + x - 9.5 = 0 \rightarrow x = ?$$

Additional handwritten notes:

$$A_d = g_{m1} (R_{o2} || R_{o8})$$

$$A_c = \frac{1}{g_{m7} (2R_{o2})}$$

So, in the next slide we will be talking about that so here again we are assuming that these two transistors, these two transistors they are identical, these two transistors they are identical here and the load part also it is active current mirror load and they are also identical. And the supply voltage it is 12 volt bias register it is 9.5 k and let we consider all the lambdas are 0.01 per volt. Threshold voltage of all the transistors it is equal to 1.5 the analysis part it will be very similar to the other circuit.

We just now we have discussed having BJT implementation, but probably the DC operating point may be little different. So, let we calculate the DC operating point we do have 12 volt supply here and we do have the size of transistor 4, it is given here rather trans conductance factor it is 4 milliamperere per volt square. If we calculate it carefully what you can get here it is the current flow it is actually it is equal to 1 milliamperere.

So, 4 is it 1 milliampere this is 3 and 4 they are equal that is fine let me calculate this one. So, we do have the V_{DD} minus V_s or V_{GS} of transistor 4 and so that is equal to this R_{bias} , R_{bias} multiplied and this I and so this I reference.

So, this I reference on the other hand it can be defined by this transistor so we do have R_{bias} multiplied by 4 milliampere by 2 into V_{GS} minus V_{th} square. And so here what we can do we can yeah so we can add 1 V_{th} and then subtract 1 V_{th} . So, we can say V_{DD} minus V_{th} minus V_{GS} 4 minus V_{th} equals to we do have 9 here 9.5 here and then 2 here. So, that gives us 19 into 19 into V_{GS} 4 minus V_{th} square and this part it is it is 9.5 So, we can say this 9.5 minus let you consider this is x is equal to $19x$ square right.

So, from that we can find what will be the corresponding x so we do have $19x$ square plus x and then minus 9.5 equals to 0. So, from that we can find what is the x and then you can consider this two are having current mirror so; obviously, then you can find what will be the current flow here. And then half of the current it is flowing here, so then here also the corresponding current it will be half of that.

So, that is how we can proceed probably you can work it out and once you get the operating point then you can find the differential mode gain. Which is again g_m into r_o 2 in parallel with r_o 8 and the common mode gain on the other hand it is a_c equals to minus 1 by g_m 7 into 2 into r_o 3. Probably you can work it out so since it is similar kind of example so I will skip that part.

(Refer Slide Time: 25:18)

Numerical example on Differential amplifier having CM (using MOSFETs)


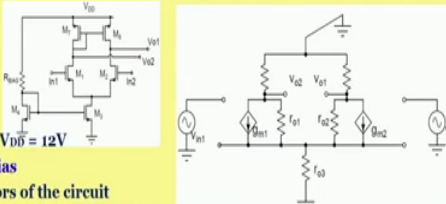
• **Example 11 (contd.):**

- $(K_n \cdot W1/L1) = (K_n \cdot W2/L2) = 2 \text{ mA/V}^2$,
- $(K_n \cdot W3/L3) = (K_n \cdot W4/L4) = 4 \text{ mA/V}^2$,
- $(K_p \cdot W7/L7) = (K_p \cdot W8/L8) = 1 \text{ mA/V}^2$
- $V_{th} = 1.5\text{V}$, $\lambda_i \approx 0.01/\text{V}$, $R_{BIAS} = 9.5 \text{ k}\Omega$, $V_{DD} = 12\text{V}$

For a "meaningful" input common mode bias

(i) Find d.c. currents through all transistors of the circuit

(ii) Find the differential mode gain and common mode gain of the amplifier



So, yeah so this is and then you can probably you can find what will be the numerical value.

(Refer Slide Time: 25:25)

Conclusion:

- ❑ **Numerical examples on simple current mirror**
 - Using MOSFETs
 - Using BJTs
- ❑ **Numerical examples on improvised CM**
 - Using BJTs
 - Using MOSFETs
- ❑ **Numerical examples on amplifiers having CM**
 - CE/CS amplifiers
 - ✓ Differential amplifiers

Now, coming to the conclusion of this entire session it is what we have talked about basically we started with numerical examples of simple current mirror. And we have calculated the different transistor current there and then we have talked about numerical examples of improvised current mirror namely the beta helper and then cascade current mirror.

And then we have talked about different numerical examples on amplifier starting with common emitter and common source amplifier, having current mirror as its load. And then we have talked about differential amplifier implemented by BJT as well as the MOSFET. And then there we have considered how to calculate the quiescent current of all the transistors and then we have calculated the differential mode gain and common mode gain, I think that is all to share with you thank you for listening.

