

Analog Electronic Circuits
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Lecture – 88
Numerical Examples on Current Mirror and its Application (Part-C)

(Refer Slide Time: 00:28)

Numerical example on CE amplifier using CM (using BJTs)

Example 8:

- Assume that, $V_{BE(on)} \approx 0.6V$ and $V_A = 100V$, $V_T = 26mV$
- $\beta_1 = \beta_2 = 100$, Q_1 and Q_2 are identical and Q_3 and Q_4 are identical
- $R_1 = R_2$, $V_{cc} = 12V$

CASE – I: β_3 and β_4 are very high

(i) Find the value of R_1 so that nominal value of I_{C1} is equal to 2 mA.
 Use this value of R_1 for the subsequent parts of this question.

(ii) Find the values small signal output resistance and voltage gain of the amplifier.

(iii) Find the d.c. output voltage

$R_1 = \frac{12 - 0.6}{20\mu A} = \frac{11.4}{20} = 570 \text{ k}\Omega$
 $R_{out} = r_{o1} \parallel r_{o4} = 25 \text{ k}\Omega$
 $r_{o1} = \frac{V_A}{I_C} = \frac{100}{2 \text{ mA}} = 50 \text{ k}\Omega$
 $r_{o4} = 50 \text{ k}\Omega$
 $g_{m1} = \frac{2 \text{ mA}}{26 \text{ mV}} = \frac{1}{13}$
 $\text{Voltage Gain} = -g_{m1} R_{out} = -\frac{25 \text{ k}}{13} = -1923$

Dear students, welcome back after the break. So, we are going through different numerical examples and now we are going to talk about one common emitter amplifier which is using current mirror and particularly to bias the active load say Q 4. We are using current mirror and transistor 1; it is the amplifying device then we are assuming that Q 1 and Q 2 they are identical and also we are assuming that whatever the this Q 3 and Q 4 are also identical.

So, to get the I_C current of transistor 1 and collector current or transistor 4 equal. We want the current flow through transistor 2 should be equal to current flow through transistor 1. And

since, Q 1 and Q 2 are identical having the same beta value of 100. So, then the value of this resistance bias resistance, based biased resistance R 1 should be identical to this transistor the register R 2.

So, that the base current here and base current here, DC base current they should be equal. So, also we do have othered information namely all the devices are having early voltage 100 volt and with this information let we try to find what will be the value of this resistance to get the collector current I C 1 equals to 2 milli ampere.

So, since the beta is 100 so, the I B it is should be equal to 20 microampere. So, to get the value of this R 1 to get 20 microampere, the R 1 should be equals to V cc, that is 12 volt minus V BE point 6 volt divided by 20 micro ampere. So, this is 11.4 divided by 20 yeah. So, that is equal to you know 570 kilo ohm. So, the value of this resistance as well as this resistance they are equal to 570 kilo ohm.

So, with that we do have this current is also 2 milli ampere and if we assume that the base current loss it is ignorable, then you can say that collector current of transistor 3 it is also 2 milli ampere which is getting mirrored to transistor 4, so, that is making this current also 2 milli ampere. So, that is how these 2 currents; currents of transistor 1 and transistor 4 they are getting matched.

Now, with this information let us try to find the small signal output resistance and voltage gain of the amplifier. So, we are assuming both the devices are in active region. So, the output resistance R out equals to parallel connection of r o 1 and r o 4. Whereas, this r o 1, r o 1 equals to V A divided by this I C. So, that is equal to 100 divided by 2 milli ampere. So, that is giving us 50 kilo ohm.

So, same thing we can get for transistor 4, r o 4 equals to 50 kilo ohm and that gives us 25 kilo ohm. So, the output resistance it is 25 kilo. Now we like to get what will be the gain of this amplifier. So, the gain of the amplifier of course, the voltage gain of this amplifier it is g

m_1 multiplied by this R_{out} with a minus sign. So, what is the value of the g_{m1} ? Now g_{m1} equals to I_C .

So, that is 2 milli ampere divided by 26 milli volt, that is the V_T given there. So, this is equal to 1 by 13 mho. So, the voltage gain so, the voltage gain it is 50, 25 kilo divided by 13. So, that is coming how much this is 25, almost 200 or to be more precise rather 25 k divided by, no not 200, it is close to 2000 rather yeah.

So, the gain it is coming 1923. So, that is the voltage gain we are getting. So, as it is expected that since we do have active load. So, the gain it is expected to be very high and the output resistance is also high. Now, next part of this question it is to find DC output voltage we need to consider this V_A , the early voltage very carefully ok. Now let me clear the board and then again we will talk about the DC voltage.

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Numerical example on CE amplifier using CM (using BJTs)

Example 8:

- Assume that, $V_{BE(on)} \approx 0.6V$ and $V_A = 100V$, $V_T = 26mV$
- $\beta_1 = \beta_2 = 100$, Q_1 and Q_2 are identical and Q_3 and Q_4 are identical
- $R_1 = R_2$, $V_{CC} = 12V$

CASE - If β_3 and β_4 are very high

(i) Find the value of R_1 so that nominal value of I_{C1} is equal to 2 mA.
Use this value of R_1 for the subsequent parts of this question.

(ii) Find the values small signal output resistance and voltage gain of the amplifier.

(iii) Find the d.c. output voltage

$V_{OUT} = 11.4V$

As I said that the current flow current flow here and here should be equal and if you see it carefully the DC voltage here it is defined by this V_{cc} minus V_{BE} drop. So, I should say the voltage here it is. So, this is 12 volt. So, the voltage here it is 12 minus 0.6 so, that is 11.4 volt.

Now, with this 11.4 volt here we can say that whatever the current we do have. So, that may be 2 milli which is of course, 1 approximation that we are assuming $1 + \lambda V_{ds}$ part equals to 1 please stop here.

Student: (Refer Time: 08:10) sir.

[FL]

Student: [FL]

[FL].

Student: [FL]

[FL]

Student: [FL] ok.

[FL].

Student: [FL] sir

[FL]

Student: [FL]

[FL]

Student: [FL] start sir.

So, the current flow here it is to be more precise it is 2 milli ampere multiplied by $1 + \frac{V_A}{V_{CE}}$ divided by sorry, this is V_{CE} of transistor 2 divided by V_A . So, the current here it is 2 multiplied by V_{CE} it is 11.4 divided by $100 + 1$. So, whatever the current. Now if you see this current is getting mirrored here ignoring the base current loss here, because for transistor 3 and transistor 4, we have considered their betas are very high.

So, they are identical, this information it is also given. So, we can assume that the collector current of transistor 4 it is same as collector current of transistor 3. So, I_{C4} equals to I_{C3} . So, this I_{C3} as I said that this current is also equal to this and on the other hand this current the collector current of transistor 1 it is also 2 milli ampere multiplied by this kind of factor $1 + \frac{V_A}{V_{CE}}$ divided by V_A .

So, if this voltage here it is say 11.4, then you can say that this current and this current they are becoming equal. In intuitively also you can say that if this voltage it is 11.4. So, that makes the current here and current here, they are equal and also the current flow in transistor 3 and transistor 4 they are equal. So, that makes everything is consistent.

So, that gives us the DC output voltage V_{OUT} should be equal to 11.4 volt right. But of course, if the value of early voltage or in case we cannot ignore say this base current and then of course, the corresponding the current here and here there will be a mismatch and the DC voltage here it will deviate from here. So, in the next numerical example it is continuation of this, the same example, but considering finite value of this beta of transistor 3 and 4 will be giving us a situation where we need to consider mismatch of the 2 current and then we can try to find what will be the change of this output voltage right.

(Refer Slide Time: 12:13)

Numerical example on CE amplifier using CM (using BJTs)

• Example 8 (contd.):

- Assume that, $V_{BE(on)} = 0.6V$ and $V_A = 100V$, $V_T = 26mV$
- $\beta_1 = \beta_2 = 100$, Q_1 and Q_2 are identical and Q_3 and Q_4 are identical
- $R_1 = R_2$, $V_{cc} = 12V$

CASE - II: $\beta_3 = \beta_4 = 250$

(i) Find the precise value of I_{C1} and I_{C2} for $V_{CE1} = 11.4V$ and $V_{CE2} = 11.4V$
 Find the precise value of I_{C3} and I_{C4} for $V_{CE1} = 11.4V$ and $V_{CE2} = 11.4V$

(ii) Find the non-ideality factor due to base current loss in the current mirror

(iii) Find the d.c. output voltage

$I_{REF} = I_{C1} = 20\mu A \times 100 \times \left(1 + \frac{V_{CE}}{V_A}\right) = 2 \times 1.114 = 2.228\text{ mA}$, $I_{C2} = 2.228\text{ mA}$

$I_{C3} = I_{C4} = \frac{I_{REF}}{\left(1 + \frac{1}{\beta_3} + \frac{1}{\beta_4}\right)} = 2.228 \times \frac{1}{\left(1 + \frac{2}{250}\right)} = \frac{2.228}{1.008} = 2.210\text{ mA}$

So, in the next slide we are going to talk about that yeah. So, as I said that the problem here it is very similar, except that transistor 3 and transistor 4 they do have beta equals to 250. Now, here we can try to find what will be the current I_{C1} and I_{C2} at V_{CE} equals to 11.4. Why 11.4? As I say that is the voltage here it is 11.4 and suppose if we make this voltage also 11.4, then we know this current and this current they will be equal. And just now we have calculated that I_{C1} equals to 2 milli ampere. In fact, that is the base current 20 micro ampere multiplied by beta that is 100 multiplied by 1 plus V_{CE} , which is 11.4 divided by V_A .

In fact, if you do the calculation here what you will get it is the 2 into 1.114. In other words, this is 2.228 milli ampere. In fact, this is same for I_{C2} also. So, I_{C2} also equals to 2.228. Assuming that V_{CE2} it is 11.4. We can also try to find what will be the corresponding current here in transistor 3 and a transistor 4. If we ignore the if we ignore the base current loss, then we are expecting that this current and this current it will be same. But we do have

some loss here so, to get the I_{C3} what you can say that I_{C2} now it is working as the reference current for this current mirror I_{REF} .

So, I_{REF} equals to I_{C1} and its value is given here. So, I_{C3} equals to this I_{REF} and also we have to consider the non ideality factor due to the base current loss and that is $1 + \frac{1}{\beta}$ by $1 + \frac{1}{\beta}$ plus I_{C1} ratio, so, that is $1 + \frac{1}{\beta}$ multiplied by $1 + \frac{1}{\beta}$. So, we do have 2.228 is the I_{REF} reference current multiplied by $1 + \frac{1}{\beta}$ divided by $1 + \frac{1}{\beta}$ plus $1 + \frac{1}{\beta}$ by 250. In fact, both of them are 250s. So, we can simply say this is 2 divided by 250 and so, this is equal to 2.228 divided by 1.008 right. So, 2 divided by 250 right. So, this is 2 divided by 250 yeah. So, this is becoming 2.228 divided by 1.008. So, that is equal to now 2.228 divided by 1.008. So, that is equal to 2.210 milli ampere.

Now, the same current, same current it is also flowing through transistor 4 as they are identical. So, now, you can see that if we try to hold this voltage at 11.4, then the current flow here it is 2.228. On the other hand, the current coming from transistor 4 it is 2 on the other it is 2.210. So, we do have some excess current requirement and so, that current it is point so, we do have additional requirement here. So, that current is 2.228 minus 2.21. So, additional 0.018 milli ampere of current we are looking from this node.

Now where this current it will be coming from. So, of course, we do have in the small signal equivalent circuit we do have r_{o4} which is connected to the supply. And then also we do have r_{o1} . In fact, these 2 together you may say that it is providing R_{OUT} and the other end of the R_{OUT} , it is connected to 11.4 volt. So, as we are looking for this excess current, there will be a change of this voltage with respect to 11.4 volt by an amount of so, if I say ΔV_{OUT} . So, this ΔV_{OUT} it will be 0.018 milli ampere multiplied by whatever the output resistance.

And we have calculated the output resistance it was 25 k. So, that gives us a voltage difference or voltage variation which is equal to 25 multiplied by 1 point so 0.018. So, that is equal to 0.45 volt. So, the voltage here at the output the DC voltage it will be equal to V_{OUT}

equals to 11.4 minus 0.45. So, that is equal to 9.95 volt. Why it is minus? That is because we are demanding more current here so, naturally the voltage it will be coming down.

In case if this current it is higher than the current flow through transistor 1 for 11.4 volt DC, then the corresponding voltage here it would be higher positive. So, in this case since the current flow here it is more. So, we do have reduction of the voltage and it is finally, going to this one. So, yeah so, we have calculated these 2 currents and then also we have calculated this non ideality factor. In fact, this is the non ideality factor which is 1 divided by. So, this non ideality factor is 1 divided by 1.008. And then the corresponding DC voltage it is given here yeah. So, that is how you can approach. So, here what we have seen that precision level or these 2 currents are important, otherwise this voltage it may be having a big change. See suppose this the early voltage here and early voltage of the other transistor if they are having mismatch then also it is expected to have mismatch of these 2 current leading to significant amount of variation of this output voltage.

This may be a case when the output node it is high impedance node. So, even a small mismatch of the current may lead to significant amount of voltage variation. In this case though this variation it is not much, but there may be a situation in practical situations this difference it may be so large, probably 1 of the transistor may be pushed towards the saturated condition or saturation region of operation. So, we need to be little careful. Now let us go into different types of examples or application circuit of current mirror namely. differential amplifier. So, in the next example, example 9; we will be talking about differential amplifier where we are using current mirror yeah.

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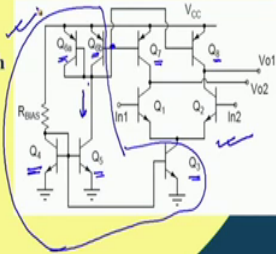
Numerical example on Differential amplifier having CM (using BJTs)

• Example 9:

- Assume that, $V_{BE(on)} \approx 0.6V$ and $V_A = 100V$, β 's are very high
- Q_1 and Q_2 are identical, Q_3, Q_4 and Q_5 are identical,
- Q_{6a}, Q_{6b}, Q_7 and Q_8 are identical
- $R_{BIAS} = 11.4 k\Omega$, $V_{cc} = 12V$, $V_T = 26mV$

For a "meaningful" input common mode bias

(i) Find d.c. currents through all transistors of the circuit



The circuit diagram shows a differential amplifier with two input transistors, Q1 and Q2, and two output transistors, Q3 and Q4. The inputs are labeled In1 and In2, and the outputs are labeled Vo1 and Vo2. The circuit is powered by Vcc and ground. A resistor R_BIAS is connected to the base of Q1 and Q2. The biasing circuit includes transistors Q5, Q6a, Q6b, Q7, and Q8. The circuit is designed to provide a meaningful input common mode bias.

So, here is the circuit first of all we do have the main differential amplifier and then we do have the bias circuit here. In fact, if you see here the bias circuit it is having number of current mirror. So, Q_4 and Q_5 they are forming a current mirror, Q_4 and Q_3 they are also forming a current mirror and whatever the current is flowing here that is again getting mirror to transistor 7 as well as transistor 8 and the corresponding diode connected transistors Q_{6a} and Q_{6b} together it is mirroring the current. In fact, this circuit we have discussed in a while we have analyzed the circuit. Now let us go into it is numerical calculation. What we have the information given here it is transistor yeah.

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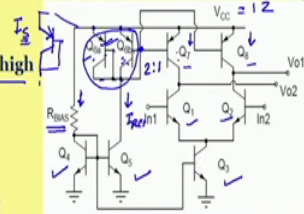
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- $R_{BIAS} = 11.4 k\Omega$, $V_{CC} = 12V$, $V_T = 26mV$

For a "meaningful" input common mode bias

(i) Find d.c. currents through all transistors of the circuit



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So, transistor 1 and 2, they are well matched. So, since it is differential amplifier so, we are looking for that. And then Q_3, Q_4 and Q_5 they are also identical. So, they are also matched NPN transistor. On the other hand Q_7, Q_8 , they need to be identical for differential amplifier of performance point of view. In addition to that Q_{6a} and Q_{6b} individually they are also identical to Q_7 and Q_8 . So, I should say all the 4 transistors they are identical.

Now, the moment we make transistor 6 and 6 a and 6 b parallelly connected, namely they are collectors they are connected together emitters are connected together and base also they are connected together. So, you may equivalently say that we do have 1 transistor which is say Q_6 which is similar to or it is identical to a parallel connection of this BJT transistor, assuming that the I_s of this transistor it is 2 times of I_s of individual Q_{6a} and Q_{6b} .

So, we may say that this current mirror it is mirroring the current with a ratio of 2 is to 1 rather whatever the current we do have here $I_{\text{reference}}$ current. So, half of that current it will be flowing here and another half it will be flowing there. So, that is that is what we have to keep in mind.

Now, here in this circuit the bias registered it is given to us that is 11.4 k and then supply voltage of course, this is 12 volt and thermal equivalent voltage it is 26 milli volt and V_{BE1} as usual we are taking point 6, early voltage it is 100 volt and let me assume that beta of all transistors they are quite high. So, we can ignore the base current loss.

In fact, many of the bias circuits we may not be looking for precision level of the current we like to get nominal value of the current and to get that we can many a times we do ignore the effect of beta. Anyway, so, this is given to us and let we calculate the reference current here and then let we calculate the current through all the other transistors. So, how do we proceed? First of all, the current flow through this R BIAS.

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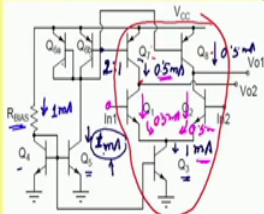
Numerical example on Differential amplifier having CM (using BJTs)

• Example 9:

- Assume that, $V_{BE(on)} \approx 0.6V$ and $V_A = 100V$, β 's are very high
- Q1 and Q2 are identical, Q3, Q4 and Q5 are identical,
- Q6a, Q6b, Q7 and Q8 are identical
- RBIAS = 11.4 k Ω , Vcc = 12V, $V_T = 26mV$

For a "meaningful" input common mode bias

(i) Find d.c. currents through all transistors of the circuit



$$I_{REF} = \frac{12 - 0.6}{11.4} = 1 \text{ mA} \Rightarrow I_{C3} = I_{C5} = 1 \text{ mA}$$

$$I_{C7} = I_{C8} = I_{C1} = I_{C2} \approx 0.5 \text{ mA}$$

$$I_{C6a} = I_{C6b} = 0.5 \text{ mA}$$

So, R BIAS it is we may call I reference, I reference equals to 12 volt supply minus V BE on of transistor 4 divided by R BIAS so, that is 11.4; so, that is equal to 1 milli ampere. For simplicity that why I have picked up the value here. So, that the reference current here it is 1 milli ampere. Now we do have transistor 5 and transistor 3 they are well matched with transistor 4. So, we can see that this current is 1 milli ampere same thing here also.

Now, you may consider this early voltage and then you can precisely get the value of this current, but many a times we may rather ignore that precision level. So, we can consider this nominal current of 1 milli ampere it is flowing through both these transistors. And as I said that this diode connected transistor it is mirroring the current in the ratio of 2 is to 1. So, half of this 1 milli ampere. So, that is 0.5 milli ampere. It is flowing through transistor 7 and likewise 0.5 milli ampere current is flowing through transistor 8.

Now if I say that we do have meaningful DC voltage here and here. So, that is what we said meaningful input common mode bias you do have then current flow here and current flow here they are identical. So, I should say half of this current is coming through transistor 1 and the other half it is coming through transistor 2.

So, current flow here it is 0.5 and here also it is 0.5 milli ampere. In fact, this 0.5 milliamperes it is consistent with the current flow through 7 and 8 respectively. So, that makes the current flow through transistor 5 and transistor 3 equal to 1 milli ampere. On the other hand current flow through transistor 7 then I_{C8} equals to I_{C1} equals to I_{C2} , all of them are approximately 0.5 milli ampere.

In fact, current flow through transistor 6 a and 6 b, they are also equal to 0.5 milli ampere. With this information now we can try to say that we can calculate what will be the gain and since the nominal currents they are consistent we can assume that all the transistors namely Q 1, Q 2, Q 7, Q 8 and Q 3 are in active region of operation. So, in the main circuit, we are keeping all the devices in proper region of operation then we can calculate the small signal gain.

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Numerical example on Differential amplifier having CM (using BJTs)

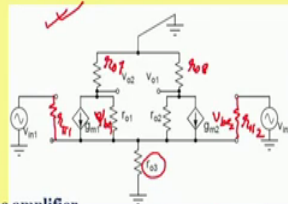
• Example 9 (contd.):

- Assume that, $V_{BE(on)} \approx 0.6V$ and $V_A = 100V$, β 's are very high
- Q1 and Q2 are identical, Q3, Q4 and Q5 are identical,
- Q6a, Q6b, Q7 and Q8 are identical
- $R_{BIAS} = 11.4\ k\Omega$, $V_{cc} = 12V$, $V_T = 26mV$

For a "meaningful" input common mode bias

(i) Find d.c. currents through all transistors of the circuit

(ii) Find the differential mode gain and common mode gain of the amplifier



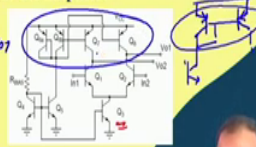

$$A_d = g_{m1}(r_{o1} || r_{o7})$$

$$= \frac{0.5}{26} \times 100\ k \approx 1.9 \times 10^3$$

$$A_c = \frac{-r_{o7}}{2r_{o3}} = \frac{-200k}{200k} = -1$$

$$r_{o1} = \frac{100}{0.5\ mA} = 200\ k = r_{o7}$$

$$r_{o3} = \frac{100}{1} = 100\ k$$

So, in the in the next slide as you have done before, once you know the operating point then we can calculate the small signal gain. So, the second so, this part we already have done. So, in the second part; we need to find the differential mode gain and common mode gain. Here we do have the small signal equivalent circuit where we do have yeah of course, we are not showing this $r_{\pi 1}$ and $r_{\pi 2}$ and transistor 7 and 8, they are giving $r_{o 7}$ and $r_{o 8}$.

We do have $r_{o 1}$ and $r_{o 2}$ and a current flow here it is $g_{m 1}$ into $V_{BE 1}$ and $V_{BE 2}$ here. And then transistor 3, it is having resistance of $r_{o 3}$ and as we have discussed before for this circuit the volt differential mode gain ad equals to $g_{m 1}$ into $r_{o 1}$ in parallel with $r_{o 7}$. And $g_{m 1}$ it is I_c so, that is 0.5 milli ampere divided by 26 milli volt multiplied by these 2 resistances. So, what is the value of this resistance $r_{o 1}$? $r_{o 1}$ equals to early voltage of 100

divided by current of 0.5 milli ampere. So, that is equal to 200 k. So, likewise r_{o7} . So, this 2 together it is giving 100 k. So, the gain here it is. So, this 2 both of them are in milli.

So, roughly we do have 2000. So, if it is 50 by 26 we are making close to 2 or 1.9 something, 1.9 something something 1000, 10^{10} to the power 3. So, that is the gain, differential mode gain. On the other hand the common mode gain it is the expression it is r_{o7} divided by 2 times of r_{o3} and r_{o7} , it is 200 k on the other hand r_{o3} .

So, r_{o7} , it is also like this. r_{o3} it is 100 that is early voltage divided by 1 milli ampere of current. So, that is equal to 100 k and so, that gives us 200 by 200 k equals to 1 of course, with a minus sign. So, that is how we can get the common mode gain and differential mode gain of this circuit. We can also work out on differential amplifier having current mirrored using MOSFET, probably I do have that in the next slide.

But before that instead of using the load connected through a current mirror, we may have current mirror load within the circuit itself. Namely, M_7 can be made diode connected and it is corresponding current it may be coming to the output. So, in the next example, what we have it is the circuit where transistor 7, it is diode connected and that current it is getting mirrored to transistor 8.

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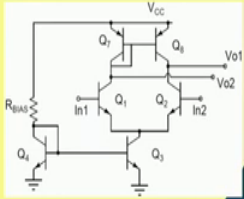
Numerical example on Differential amplifier having CM (using BJTs)

• **Example 10:**

- Assume that, $V_{BE(on)} \approx 0.6V$ and $V_A = 100V$, β 's are very high
- Q_1 and Q_2 are identical, Q_3 , Q_4 and Q_5 are identical,
- Q_7 and Q_8 are identical
- $R_{BIAS} = 11.4\text{ k}\Omega$, $V_{cc} = 12V$, $V_T = 26mV$

For a "meaningful" input common mode bias

(i) Find d.c. currents through all transistors of the circuit



The circuit diagram shows a differential amplifier with common mode biasing. It consists of a differential pair of BJTs (Q1, Q2) with inputs In1 and In2, and outputs Vo1 and Vo2. The emitters of Q1 and Q2 are connected to a common emitter node, which is biased by a current source formed by BJTs Q3, Q4, and Q5. A resistor R_BIAS is connected between the positive supply Vcc and the common emitter node. BJTs Q6 and Q7 are also shown in the circuit.

So, yeah so, here it is the circuit. Let me take a short break and then again will be resuming here.