

Analog Electronic Circuits
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Lecture – 48
Common Collector and Common Drain Amplifiers (Contd.):
Numerical Examples (Part B)

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Numerical example: CC amplifier

- $V_{BE(on)} \approx 0.6\text{ V}$
- $\beta = 100$
- $V_A = 50\text{ V}$
- $C_{\pi} = 10\text{ pF}$
- $C_{\mu} = 5\text{ pF}$

- $V_{DD} = 10\text{ V}$
- $V_{BB} = 6\text{ V}$
- $V_T = 26\text{ mV}$
- $C_L = 100\text{ pF}$
- $R_E = 9.8\text{ k}\Omega$
- $R_S \approx 100\text{ k}\Omega$

$V_C = 10\text{ V}$
 $V_E = 4.9\text{ V}$
 $V_B = 5.5\text{ V}$

$g_m = \frac{I_C}{V_T} = \frac{0.5\text{ mA}}{26\text{ mV}} = 19.2\text{ mA/V}$
 $r_{\pi} = \frac{\beta}{g_m} = \frac{100}{19.2} = 5.2\text{ k}\Omega$
 $r_o = \frac{V_A}{I_C} = \frac{50\text{ V}}{0.5\text{ mA}} = 100\text{ k}\Omega$

$(1 + \beta)I_B \approx \beta I_B$

$6\text{ V} = I_B \times 100\text{ k}\Omega + 0.6\text{ V} + 100 I_B \times R_E$

$I_B \{ 10^5 + 9.8 \times 10^5 \} = 5.4\text{ V}$

$I_B = \frac{5.4}{10^8 \times 10^5} = 5\text{ }\mu\text{A}$ → $I_C = \beta \times I_B = 0.5\text{ mA}$

Find:

- Opt. point
- Values of small signal pars.
- Voltage gain,
- Input Imp.
- Output Imp.
- Input Cap.
- Upper cutoff freq.

Welcome back after the short break. So, we do have here it is the third example. So, it is you can see that essentially, we are adding one resistance at the emitter instead of having ideal bias current and also we do have the R_S at the base node. We can say the source resistance. Let you consider this R_E 9.8 kilo ohms. So, let me change this one to 9.8 kilo ohms and let us try to analyze the circuit to find the operating point of the transistor.

So, to start with let me draw the DC loop here. So, we do have V_{dd} which is 6 volt and then we do have the R_S , which is 100 k and then we do have the V_{BE} on this diode drop and then we do have the resistance here R_E . So, that you consider the current flow here it is I_B . And then of course, we do have the beta times of this I_B current it is coming from the collector. So, we can say that this is beta into I_B . So, that is the I_C part.

So, the current flowing through this resistor on the other hand it is $1 + \beta$ into I_B . So, if I consider that this current it is approximately equals to beta into I_B and then if you analyze this circuit. Namely, if we consider the potential drop through this loop. So, what we can get it is in this loop. We do get 6 volt here and then we do have 0.6 volt here. So, 6 volt equals to we do have I_B into 100 k plus 0.6 volt and then roughly you can say that 100 times I_B into R_E ok. And R_E , we said 9.8. So, what we are getting here it is I_B multiplied by 100 k. So, that is 10 to the power 5 and then R_E we do have 9.8 k.

So, this is this plus. So, this is 9.8 into 10 to the power 5. So, this is equals to 5.4 volt. So, that is 5.4 volt is 6 minus 0.6. So, that gives us I_B equals to 5.4 divided by 10.8, yes 10.8 into 10 to the power 5. So, that gives us 5 micro ampere. So, just a make a note that we have intentionally have tuned it this resistance. So, that we can get the same value of this I_B , what we have obtained in our previous example of 5 micro ampere.

So, even if this resistance it is something else of course, the circuit it will be working fine, but it is just for making this circuit comparable with the previous circuit we are making this R_E equals to 9.8. So, once we obtain this I_B of say 5 micro ampere, so, that gives us the I_C equals to 100 into 5 micro ampere. So, then beta into this 5 micro ampere so, that is equals to 0.5 milliamperere right.

And then once we have the I_C equals to this one, then you can calculate what will be the voltage here. Similar to the previous case; the voltage here it will be 6 volt here minus this drop, drop across this R_S and this that drop it is 0.5. So, we can say the voltage here V_B equals to 6 minus 0.5. So, that is 5.5 let me use a different color.

So, the voltage at the base it is 5.5, the voltage coming here it is 5.5 minus 0.6. So, the voltage here it is emitter voltage equals to 4.9 volt. So, that is 5.5 minus 0.6 and of course, the collector voltage here it is 10 volt.

So, that gives us the operating point of the circuit. Now using this values of the quotient currents and voltages we can find the small signal parameter. And since the currents particularly, the collector current and base current they are same. So, we can see that the g_m value of the g_m remains the same. Namely, 1 by 52 ampere per volt μ and likewise r_{π} equals to 5.2 k and then r_{e} equals to 100 k right. So, we obtain the small signal parameter. Now then we can find what will be the voltage gain input impedance output impedance so and so.

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Numerical example: **CC amplifier**

- $V_{BE(on)} \approx 0.6\text{ V}$
- $\beta = 100$
- $V_A = 50\text{ V}$
- $C_{\pi} = 10\text{ pF}$
- $C_{\mu} = 5\text{ pF}$

- $V_{dd} = 10\text{ V}$
- $V_{BB} = 6\text{ V}$
- $V_T = 26\text{ mV}$
- $C_L = 100\text{ pF}$
- $R_E = 10.8\text{ k}\Omega$
- $R_S \approx 100\text{ k}\Omega$

Find:

- Opt. point
- Values of small signal pars.
- Voltage gain, ≈ 1
- Input Imp. $\approx 9\text{ k}\Omega$
- Output Imp. $\approx 9\text{ k}\Omega$
- Input Cap.
- Upper cutoff freq.

$$A_v = \frac{(g_m r_{\pi} + 1)(r_{\pi} \parallel R_E)}{(g_m r_{\pi} + 1)(r_{\pi} \parallel R_E) + r_{e}}$$

$$\approx \frac{(\beta + 1) 9.8\text{ k}}{(\beta + 1) 9.8\text{ k} + 5.2\text{ k}}$$

$$\approx \frac{914.2}{1014.2} \approx 0.9$$

$$R_{in} = r_{\pi} + (g_m r_{\pi} + 1) r_{e} \parallel R_E$$

$$= 5.2\text{ k}\Omega + (\beta + 1) \frac{100 \times 9.8 \times 10^3}{109.8}$$

$$= 5.2\text{ k}\Omega + 909\text{ k}\Omega = 914.2\text{ k}\Omega$$

$\approx 9\text{ k}\Omega$

So, let me use the same space and let me clear it and again this we are considering it is 9.8. Sorry for the correction here again and again. But, anyway we do have the voltage gain you may recall the voltage gain A_V , since we do have the R_E here earlier in our analysis we have considered this resistance as R_L with that. So, the voltage gain we obtain it is g_m into $r_{\pi} + 1$ into r_o in parallel with this R_E right.

So, that is because we are having this r_o coming here and this R_E and r_o they are coming in parallel because this terminal for signal it is AC ground. So, r_o and R_E they are coming in parallel. In the denominator on the other hand; we do have g_m into $r_{\pi} + 1$ into r_o in parallel with R_E plus r_{π} .

So, what are the changes we do have here it is; this is of course, $\beta + 1$. Now r_o it is 100 k and R_E it is 9.8 k right. So, close to this one, 9.8 k or to be more precise it will be close to 9.5 or something like that. But whatever it is say we approximate by this R_E , it is a 9.8 k. So, likewise in the denominator we do have $\beta + 1$ into whatever 9.8 k and then we do have the r_{π} . So, this r_{π} it is this is 5.2 k. Note that this voltage gain it is from this point to this point.

We do have R_S also to be considered, but attenuation for this circuit from this point to this point, it is expected to be very small even though R_S it is 100 k. Mainly because, you do have the resistance here, input resistance here it is very high. But anyway, we will see that, but for the time being let you consider voltage gain from precisely at the base terminal to the emitter terminal and even though this R_E it is coming in parallel with r_o because, this we do have $1 + \beta$ getting multiplied.

So, still this part it is dominating over this part. So, still and hence we can say that this is approximately 1. So, the voltage gain it is approximately 1. Now let us look into the input resistance. So, let you consider the input resistance. So, the input resistance on the other hand it is as we have discussed before. So, this will be $r_{\pi} + g_m$ into $r_{\pi} + 1$ into r_o coming in parallel with R_E . And again this is the input resistance looking into the base of this one, base of the transistor without considering this R_S .

So, we do have r_{pi} equals to 5.2 kilo ohms and then we do have $\beta + 1$ and then this resistance it is whatever 100 multiplied by 9.8 divided by 109.8 into 10 to the power 3 kilo right. And so, this part again either we can approximate by 9.8 or so, we can say that this is close to 9 . But, it will be very close to 9 this if you say that this is $10/11$. So, that will be close to this one, but whatever it is. It, we do have so if I approximate this part or this is equal to very close to 9 kilo ohm.

So, even then we do have 5.2 kilo ohm and then we do have 100 , one getting multiplied with and this 9 . So, that is giving us 909 kilo ohm. So, that is equals to 914.2 kilo ohm that is definitely it is higher than this resistance. So, the attenuation coming at this point, because the input resistance here it is given here. Attenuation due to this finite value of R_S which is I should say the voltage here with respect to this one or rather base voltage V_b with respect to V_{in} it is given by R_{in} divided by $R_S + R_{in}$. And R_S is 100 k R_{in} it is close to 900 k. So, accordingly you can say that this is 914.2 divided by this is 1014.2 .

So, it is very close to 0.9 . So, even if I consider this finite value of R_S then the voltage gain starting from the primary terminal to this point even though I do have R_S is quite high, still it is around 0.9 , considering this R_S high value of R_S right. So, that is about the voltage gain remaining close to 1 . Output resistance we have discussed before. So, again we can probably we can go through that the let me clear this and this is 9.8 k as we have taken.

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Numerical example: CC amplifier

Find:

- Opt. point
- Values of small signal pars.
- Voltage gain,
- Input Imp.
- Output Imp.
- Input Cap.
- Upper cutoff freq.

$V_{BE(on)} \approx 0.6\text{ V}$
 $\beta = 100$
 $V_A = 50\text{ V}$
 $C_{\pi} = 10\text{ pF}$
 $C_{\mu} = 5\text{ pF}$

$V_{dd} = 10\text{ V}$
 $V_{BB} = 6\text{ V}$
 $V_T = 26\text{ mV}$
 $C_L = 100\text{ pF}$
 $R_E = 10.8\text{ k}\Omega \approx 9\text{ k}\Omega$
 $R_S = 100\text{ k}\Omega$

$R_o \approx \frac{1}{g_m + \frac{1}{R_E}} \approx \frac{1}{g_m} = 52\ \Omega$
 $f_{U1} = \frac{1}{2\pi R_o C_L} \approx 30\text{ MHz}$
 $C_{in} \approx C_{\mu} \Rightarrow f_{U2} = \frac{1}{2\pi R_S C_{in}} \approx \frac{1}{3}\text{ MHz}$

So, the output impedance it is if I consider this part this is giving us the output impedance very close to 1 by gm. So, R O it is very close to 1 by g m and then we also have this 1 by R E and R E since it is quite high compared to 1 by g m. So, this is remaining close to 1 by gm which is 52 ohms.

So, the upper cutoff frequency considering the C L and the output resistance if I consider. So, this upper cutoff frequency coming from the output node, if I say that f U 1. So, that is equal to 1 by 2 pi R o into C L. So, this is remaining very close to thirty mega Hertz. And then if I consider the input capacitance; again C in it is still we will approximated by C mu and hence f U 2, the second option for the upper cutoff frequency which is 1 by 2 pi R S and C in.

So, that part it is I should say I do have the R in also, but yeah R in is much higher than RS. In fact, to be more precise I should rather consider the R in also. So, we should consider R S in

parallel with R_{in} and then C_{in} . And of course, here this resistance it is coming close to and this close to 100 kilo Hertz as kilo ohm. So, again this frequency it is very close to 1 by 3 mega Hertz.

So, the conclusion here it is what we can say that even if you consider R_E and R_S still we do have the overall performance of the circuit even with R_S is very high overall performance of the circuit or the qualitative performance of the circuit. Namely, the voltage gain approximately one and then input resistance is very high, output resistance is very small, input capacitance is low and then the upper cutoff frequency it remaining high only right.

Now, if I consider the other resistance also R_C then of course, there will be a change. So, we will see that, but before that let you consider the most counterpart also, namely common drain amplifier. So, in the next slide we will be going for common drain amplifier yeah. So, here we do have the common drain amplifier.

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Numerical example: CD amplifier

Find:

- Opt. point
- Values of small signal pars.
- Voltage gain,
- Output Imp.
- Input Cap.
- Upper cutoff freq.

$V_{th} \approx 1V$
 $KW/L = 2 \text{ mA/V}^2$
 $\lambda = 0.01 /V$
 $C_{gs} = 10 \text{ pF}$
 $C_{gd} = 2 \text{ pF}$

$V_{dd} = 10V$
 $V_{GG} = 6V$
 $C_L = 100\text{pF}$
 $I_{BIAS} = 1 \text{ mA}$
 $R_S \approx 10 \text{ k}\Omega$

$V_S = V_{GG} = V_{GS} = 6 - 2 = 4V$
 $I_{DS} = I_{BIAS} = \frac{KW}{2L} (V_{GS} - V_{th})^2 (1 + \lambda V_{DS}) \approx 1$

$V_{GS} = V_{th} + \sqrt{\frac{2I_{BIAS}}{KW/L}}$
 $= 1V + \sqrt{\frac{2 \times 1 \text{ mA}}{2 \text{ mA/V}^2}}$
 $= 1 + 1 = 2V$

$g_m = \frac{KW}{L} (V_{GS} - V_{th})$
 $= 2 \times 1 \text{ mA/V}$
 $r_{ds} = \frac{1}{\lambda I_{DS}}$
 $= \frac{1}{0.01 \times 10^{-3}} = 10^5 \Omega$

Again for this circuit also to find the performance parameters, we need to follow the same procedure. Namely, we need to find the operating point then we need to find the small signal performance then as parameters values and then we can find the corresponding voltage gain output resistance in then input capacitance in so and so.

So, here of course, the circuit it is different slightly different. So, let us try to see with this example, how do we find the operating point of the transistor. Remaining things it will be similar to the common collector circuit. So, let us try to see that. So, to get the DC operating point, let we consider this circuit. So, what we have here it is in DC condition; VG if I say that R S it is even though it is say 10 k or 100 k since the current flow here it is 0, DC wise. So, the drop across this R S is 0. So, we can say that V GG it is directly coming to the gate node.

So, if I say that V_{GG} equals to, I do have the V_{GS} of the transistor and then we do have the current flowing here right. And this current flow of course, it is we do have say 1 milli ampere of current. So, we are expecting that to find the voltage here which is basically the V_{GG} minus this 1 sorry, I should say that the V_S voltage or V_{out} voltage it is V_{GG} minus V_{GS} .

Now, to find the V_{GS} what you have to do this is now I_{DS} . So, we can say that I_{DS} equals to I_{BIAS} equals to the expression of the current which is $K_n W/L$ by $(V_{GS} - V_{th})^2$. And we may drop this $(1 + \lambda V_{DS})$ factor. We can approximate this is may be equals to 1. So, if I equate this part; what we can get here it is V_{GS} equals to V_{th} plus 2 times I_{BIAS} and then divided by $K_n W/L$ and then square root.

So, here we do have V_{th} of the transistor it is given here which is 1 volt plus 2 times I_{bias} it is 1 milliampere and then the device parameter it is given here it is $K_n W/L$ equals to 2 milli ampere per volt. So, 2 milli ampere per, I should say this is volt square. So, what we have here it is this 2 and this 2 it is getting cancelled. We do have milliampere it is also getting canceled. So, this part, this part as a result it is we do you have 1. So, the V_{GS} it is 1 plus 1 equals to 2 volt right. So, that is the V_{GS} .

So, from that we can say that the voltage at the source it is 6 minus 2, that is 4 volt. So, the voltage here it is 4 volt and of course, the drain voltage here it is 10 volt and gate voltage here it is 6 volt. So, that gives us the operating point of the transistor of course, it ensures the transistor it is in saturation region of operation which is of course, required. And then we can calculate the small signal parameter. So, let us try to see what will be the small signal parameter values. Let me use this space here.

So, the g_m particularly the g_m it is $K_n W/L$ into $V_{GS} - V_{th}$. So, what we have it is 2 milli ampere per volt square and this is 1 volt. So, 2 into 1 milli ampere per volt, on the other hand the r_{ds} which is 1 divided by λ into I_{DS} . Now λ it is given here it is 0.01 0.01. So, that is 1 divided by 0.01 which is 10 power minus 2 and then I_{DS} it is 1 milliampere which is 10 power minus 3.

So, that gives us 10 power 5 ohms. So, that is the; that is the impedance we are getting for this r_{ds} and this is the g_m part. So, using that we can find now we can find the voltage gain. So, you can probably for the to calculate the voltage gain, let you try to remember the value of this V_{GS} and sorry, the g_m and the corresponding value of the r_{ds} .

So, again let me use the space and clean it. So, what we are looking for it is the voltage gain A_v .

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Numerical example: CD amplifier

Find:

- Opt. point
- Values of small signal pars.
- Voltage gain, ≈ 1
- Output Imp.
- Input Cap.
- Upper cutoff freq.

• $V_{th} \approx 1\text{ V}$

• $KW/L = 2\text{ mA/V}$

• $\lambda = 0.01\text{ /V}$

• $C_{gs} = 10\text{ pF}$

• $C_{gd} = 2\text{ pF}$

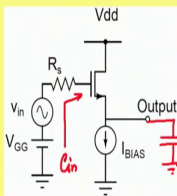
• $V_{dd} = 10\text{ V}$

• $V_{GG} = 6\text{ V}$

• $C_L = 100\text{ pF}$

• $I_{BIAS} = 1\text{ mA}$

• $R_s \approx 10\text{ k}\Omega$



$$A_v = \frac{g_m r_{ds}}{(g_m r_{ds} + 1)}$$

$$= \frac{2 \times 10^{-3} \times 10^5}{(2 \times 10^{-3} \times 10^5 + 1)}$$

$$= \frac{200}{201} \approx 1$$

$$R_o = \frac{1}{g_m + \frac{1}{r_{ds}}}$$

$$= \frac{1}{2 \times 10^{-3} + 10^{-5}} \approx \frac{10^3}{2} = 500\ \Omega$$

$$C_{in} = C_{gs} \left(\frac{1}{g_m r_{ds} + 1} \right) + C_{gd}$$

$$= \frac{10\text{ pF}}{201} + 2\text{ pF}$$

$$\approx 2\text{ pF}$$

Handwritten notes:

- $A_v = \frac{g_m r_{ds}}{(g_m r_{ds} + 1)}$
- $= \frac{2 \times 10^{-3} \times 10^5}{(2 \times 10^{-3} \times 10^5 + 1)}$
- $= \frac{200}{201} \approx 1$
- $R_o = \frac{1}{g_m + \frac{1}{r_{ds}}}$
- $= \frac{1}{2 \times 10^{-3} + 10^{-5}} \approx \frac{10^3}{2} = 500\ \Omega$
- $C_{in} = C_{gs} \left(\frac{1}{g_m r_{ds} + 1} \right) + C_{gd}$
- $= \frac{10\text{ pF}}{201} + 2\text{ pF}$
- $\approx 2\text{ pF}$

So, what is the voltage gain of this circuit? The g_m into r_{ds} divided by g_m into r_{ds} plus 1 and g_m it is 2 milli, 2 into 10 to the power minus 3 and r_{ds} it is 10 to the power 5 ohms. So, likewise here also 2 into 10 to the power minus 5 into 10 to the power sorry, minus 3 and 10 to the power 5 plus 1.

So, here in the numerator we do have 200 and in the denominator we do have 201. So, we can approximate this by 1. So, the voltage gain it is 1. And then the output impedance if you see the output impedance R_{out} equals to 1 divided by g_m plus 1 by r_{ds} . So, what we have here it is 1 divided by g_m it is 2 milli, 2 into 10 to the power minus 3 and then 1 by r_{ds} . So, that is 10 to the power minus 5 right.

So, again this is this part it is dominating over this. So, we can approximate this by so, 10 to the power 3 by 2 which is 500 ohms. Of course, it is not as small as the previous case; namely as small as R_{out} of common collector stage, but still it is low and then if you consider we do have the capacitance coming here of say 100 pico Farad.

So, from that we can calculate the upper cutoff frequency. But before that we can find what will be the C_{in} . So, let me use different color for C_{in} . So, now, we are going to calculate C_{in} which is C_{gs} . So, we do have the C_{gs} part multiplied by 1 by $g_m r_{ds}$ plus 1 , you may recall this expression plus C_{gd} .

So, this part of course, we do have here it is 201 . So, we may drop this part or rather I should say C_{gs} we do have the 10 pico Farad divided by 201 and C_{gd} it is 2 pico Farad. So, this part we can say it is closed to we can approximate this 2 by 2 pico Farad only. Because, how much is it, this is $10, 5, 5$ and it is just right. It is it is very small we can ignore this part definitely we can ignore. So, this is what the input capacitance.

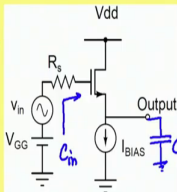
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Numerical example: *CD amplifier*

- $V_{th} \approx 1 \text{ V}$
- $KW/L = 2 \text{ mA/V}$
- $\lambda = 0.01 \text{ /V}$
- $C_{gs} = 10 \text{ pF}$
- $C_{gd} = 2 \text{ pF}$

- $V_{dd} = 10 \text{ V}$
- $V_{GG} = 6 \text{ V}$
- $C_L = 100 \text{ pF}$
- $I_{BIAS} = 1 \text{ mA}$
- $R_s \approx 10 \text{ k}\Omega$



$$f_{U1} = \frac{1}{2\pi \times 500 \times 10^{-10}} \text{ Hz}$$

$$= \frac{10^7}{\pi} \approx \frac{10}{3} \text{ MHz}$$

$$\approx 3 \text{ MHz}$$

$$f_{U2} = \frac{1}{2\pi \times 10^4 \times 2 \times 10^{-12}}$$

$$= \frac{10^8}{4\pi} = \frac{25}{\pi} \text{ MHz}$$

$$\approx 8 \text{ MHz}$$

• **Find:**

- Opt. point
- Values of small signal pars.
- Voltage gain,
- Output Imp.
- Input Cap.
- Upper cutoff freq.

Now, if I say the upper cutoff frequency let me again clear it and use the space here. So, upper cutoff frequency coming from C L. f_{u1} equals to 1 by 2π output resistance it is 500 and C L it is 10 to the power minus 10 Hertz.

So, we can multiply this 2 with 500 to get 1000 here. So, what you are getting it is 10 to the power 7 divided by π . So, approximately equals to 10 divided by 3 mega Hertz or we can say that this is close to 3 mega Hertz of course. And then the other candidate to define the upper cutoff frequency which is coming from this R S and C in. So, f_{u2} equals to 1 by 2π into R S, we are taking 100 k 10 to the power 4 and then C in it is 2 pico Farad so, 2 into 10 to the power minus 12 .

So, this 4 and this minus 12, if you see we do have minus 8 here. So, we can see it is 10 to the power 8 divided by 4 pi or we can say this is 25, 25 by pi mega Hertz. Or we can further simplify if I consider this is 3. So, roughly it is 8 mega Hertz.

So, that gives us the upper cutoff frequency it is defined by this only. So, that is the upper cutoff frequency. So, that is how you can analyze this circuit.

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Numerical example: *CD amplifier*

- $V_{th} \approx 1 \text{ V}$
- $KW/L = 2 \text{ mA/V}$
- $\lambda = 0.01 \text{ /V}$
- $C_{gs} = 10 \text{ pF}$
- $C_{gd} = 2 \text{ pF}$

- $V_{dd} = 10 \text{ V}$
- $V_{GG} = 6 \text{ V}$
- $C_L = 100 \text{ pF}$
- $I_{BIAS} = 1 \text{ mA}$
- $R_s \approx 10 \text{ k}\Omega$

• **Find:**

- Opt. point
- Values of small signal pars.
- Voltage gain,
- Output Imp.
- Input Cap.
- Upper cutoff freq.

So, similarly, if I consider the common drain circuit with say resistance here R_L instead of I_{BIAS} , then we can get the similar kind of performance probably you can work it out.

(Refer Slide Time: 36:32)

Numerical example: CD amplifier

Find:

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- Input Cap.
- Upper cutoff freq.

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 $KW/L = 2\text{ mA/V}$
 $\lambda = 0.01\text{ /V}$
 $C_{gs} = 10\text{ pF}$
 $C_{gd} = 2\text{ pF}$

$V_{dd} = 10\text{ V}$
 $V_{GG} = 6\text{ V}$
 $C_L = 100\text{ pF}$
 $R_L = 4\text{ k}\Omega$
 $R_S \approx 10\text{ k}\Omega$

$V_S = \frac{K \cdot W}{2L} R_L (V_{GG} - V_{th} - V_S)^2$
 $V_S = 1 \times 10^{-3} \times 4 \times 10^3 (5 - V_S)^2$
 $(V_S - 5)^2 = \frac{V_S}{4}$
 $V_S - 10V_S + 25 - \frac{V_S}{4} = 0$
 $(V_{GG} - V_{GS}) = I_{DS} R_L = V_S \rightarrow V_{GS} = V_{GG} - V_S$
 $I_{DS} = \frac{2 \cdot m}{2} (V_{GS} - V_{th})^2 = 1\text{ mA}$
 $V_{GS} = V_{GG} - V_O$
 $R_L I_{DS} = \frac{K \cdot W}{2L} \cdot (V_{GS} - V_{th})^2 \cdot R_L = V_{GG} - V_{GS}$
 $V_S = \frac{41 \pm 9}{8} \rightarrow \frac{4V}{80V} \times \frac{4V}{8} = \frac{41 \pm \sqrt{41}}{8} = \frac{41 \pm 6.4}{8}$

So, let us see what is the circuit I do have for you yes. So, here we do have same common drain amplifier, but we do have R_L having a value of 4 k. R_S , we do have same 10 k. So, instead of having ideal BIAS circuit if we put say R_L of say 4 k and then V_{GS} of say 6 volt with whatever the parameter it is given here, then how do you find the operating point.

So, this part since it is tricky. So, let me explain to you, rest of the things probably you can do it yourself. So, again if I consider this loop; what we can get here it is the drop across this R_S is 0. So, we can say that gate voltage it is directly coming here DC wise and then we do have the V_{GS} here and then we do have the ir drop. So, if I call this is V_O output voltage, then V_{GG} , V_{GG} minus V_O it is essentially V_{GS} of the transistor right.

So, we can say that the voltage here on the other hand, if the current flow here it is say I_{DS} , the voltage here it is R_L multiplied by I_{DS} . So, in other words we can say that the V_{GG}

minus this V_{GS} . So, that is equal to. So, this voltage that is equal to I_{DS} multiplied by R_L . Now this V_{GG} if you on the other hand if I say that V_{GS} and the yeah. So, this is so I can say the other way also say I_{DS} equals to $K W$ by $2 L$ multiplied by $V_{GS} - V_{th}$ square.

And then if I multiply this by R_L . So, what we are getting it is R_L into I_{DS} , but that is equal to this one. So, we can say that, this is equal to $V_{GG} - V_{GS}$ right. So, probably, we can try to see what will be its expression of this I_{DS} from this or from how do we proceed the, maybe you can try to write. So, this in terms of V_S and so, this is V_S then, so this is V_S . So, from that we can say that V_{GS} equals to no V_{GS} sorry, so V_{GS} equals to $V_{GG} - V_S$.

Yes. So, now, we can say that V_S equals to this one. On the other hand V_{GS} , we can replace by this $V_{GG} - V_S$. So, we can let me use different color. So, using this part and this part along with this one, what we can say that V_S equals to $K W$ by $2 L$ into R_L multiplied by V_{GS} which is $V_{GG} - V_{th} - V_S$ square.

Now, let me put the value of different parameters here. So, we do have R_L equals to $4 k$ and this part it is 1 milliamperes per volt. So, we can say that V_S equals to 1 milliamperes; 1 into 10 to the power minus 3 . R_L equals to $4 k$, 4 into 10 to the power 3 and then we do have $V_{GG} - V_{th}$, that is $6 - 1$, so, that is $5 - V_S$ square. Or we can probably you can make it $V_S - 5$ square. So, $V_S - 5$ square into 4 equals to V_S right. Or we can say that we can take this 4 here.

So, we are getting V_S square minus $10 V_S$ plus 25 . Then minus V_S by 4 equals to 0 . Now if you solve this second order equation; what will be getting is that one solution you will be getting for V_S is V_S equals to. So, the coefficient of V_S here it is 41 by 4 with a minus sign. So, 41 by 4 plus or minus square root of 41 by 4 square minus 4 into whatever it is.

So, we do have A into C . So, we do have 4 into 25 , so, that is 100 divided by 2 . So, if you take 4 outside what we will be having here it is 41 divided plus minus. So, here we do have 41 square and here you do have 16 yes so, 4 square. So, basically you will be getting 81 square root divided by 4 into 2.8 .

So, this gives you this is 9. So, we can say that V_S , I am using this space sorry for clumsy here, clumsy arrangement 41 ± 9 divided by 8. So, one solution if I consider minus, one solution it is 4 volt and the other solution if I consider this is plus that is 50 divided by 8.

Now, this is not possible that because, the transistor enters into cutoff. So, we are not considering this one, we need to consider this one. So, if I consider V_S the voltage here actually. So, this is same as the source voltage V_S if the V_S it is 4 volt; we do have 6 volt. So, the voltage drop here it is 2 volt.

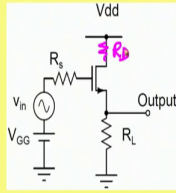
So, that gives us V_{GS} is equal to 2 volt. If the V_{GS} is equal to 2 volt, then we can say that the corresponding I_{DS} equals to $K \cdot W/L$, that is 2 milli and then divided by 2 into V_{GS} is 2 volt minus V_{th} square so, that gives us 1 milliamper. So, again we are making this R_L is equal to 4 k. So, that the current flow I_{DS} it is consistent with the previous example right.

So, let you consider that that much of current and it is consistent to the previous case and once you obtain the value of this I_{DS} . So, then we can find the corresponding value of the small signal parameters. So, let me calculate the small signal parameter.

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Numerical example: CD amplifier

- $V_{th} \approx 1 \text{ V}$
- $KW/L = 2 \text{ mA/V}$
- $\lambda = 0.01 / \text{V}$
- $C_{gs} = 10 \text{ pF}$
- $C_{gd} = 2 \text{ pF}$



$I_{DS} = 1 \text{ mA}$
 $g_m = 2 \text{ mA/V}$
 $r_{ds} = 100 \text{ k}\Omega$

- **Find:**
 - Opt. point
 - Values of small signal pars.
 - Voltage gain,
 - Output Imp.
 - Input Cap.
 - Upper cutoff freq.

• $V_{DD} = 10 \text{ V}$
• $V_{GG} = 6 \text{ V}$
• $C_L = 100 \text{ pF}$
• $R_L = 4 \text{ k}\Omega$
• $R_s \approx 10 \text{ k}\Omega$

So, I think we already have done that since I_{DS} equals to 2 milli ampere sorry, 1 milli ampere. The corresponding g_m , it was coming 2 milli ampere per volt and of course, the r_{ds} it is same as the previous case; 100 k. And rest of the parameters you can calculate yourself. So, I am not going to repeat that part now if you have say r_{ds} connected here then what will happen?

(Refer Slide Time: 48:49)

Numerical example: CD amplifier

- $V_{th} \approx 1 \text{ V}$
- $KW/L = 2 \text{ mA/V}$
- $\lambda = 0.01 / \text{V}$
- $C_{gs} = 10 \text{ pF}$
- $C_{gd} = 2 \text{ pF}$
- $V_{dd} = 10 \text{ V}$
- $V_{GG} = 6 \text{ V}$
- $C_L = 100 \text{ pF}$
- $R_D = 4 \text{ k}\Omega$
- $R_L = 4 \text{ k}\Omega$
- $R_S \approx 10 \text{ k}\Omega$

$I_{DS} = 1 \text{ mA}$

$r_{ds} = 100 \text{ k}\Omega$

$$R_0 = \left[\frac{R_D + r_{ds}}{(g_m r_{ds} + 1)} \right] \parallel R_L$$

$$\approx \frac{1}{g_m} \parallel R_L$$

$$\approx \frac{1}{g_m} = 500 \Omega$$

Find:

- Opt. point
- Values of small signal pars.
- Voltage gain, ≈ 1
- Output Imp. $\approx 500 \Omega$
- Input Cap.
- Upper cutoff freq.

So, let me see that part. So, we do have this R D also connected we do have the R D connected here. So, what we say that we do have RD which is 4 k and then R L also 4 k. Assuming this transistor it is in saturation earlier we already have analyze that for R L of 4 k, I DS equals to so, that is equal to 1 milliampere and if this is R D is equal to 4 k. So, the drop across this R D is 4 volt.

So, we do have 6 volt coming here. So, this is 6 volt and the source we do have 4 volt. So, the voltage coming here after subtracting 4 volt from 10 volt, it is 6 volt. So, we do have 6 volt here, we do have 6 volt here. So, that this transistor it is still in saturation region of operation. So, that makes the circuit it is still working as a good amplifier. And then you can use the this I DS current and the V GS to calculate the g m and this r d s it still remains high namely 100 k.

And so, what will happen is that the impedances; particularly, the output impedance it will be having little modification g_m the voltage gain since the g_m it is remaining same voltage gain again approximately it will be 1, output impedance it will be having slight change. In fact, if we see the R_{out} , if you look into this circuit; the R_{out} it will be R_D plus r_{ds} divided by g_m into r_{ds} plus 1. So, that you can calculate.

So, that is the resistance here and the total resistance looking into the circuit; it will be this part coming in parallel with R_L . Now here if you see the numerical value; this part it may be dominating over 1 and then r_{ds} it is also dominating. So, as a result this part it is becoming 1 by g_m only all practical purposes. And then, R_L even though R_L it is coming in parallel. So, it is since 1 by g_m it is 500 ohms. So, again this can be well approximated by 1 by g_m and it is 500 ohms.

So, even though we do have R_D it is there, but the if you see the output impedance it is remaining low quote and unquote low. And it is expected that upper cutoff frequency defined by output resistance and the C_L , it is almost remaining the same. Only another important thing you must be careful that voltage coming from this point to this point it is also prominent. So, as a result and that not only the C_{gd} , it will be contributing through Miller effect, but sorry, C_{gs} . But C_{gd} , it is also having Miller affected part. So, what is the voltage gain coming from the gate to drain that we need to see.

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Numerical example: *CD amplifier*

- $V_{th} \approx 1\text{ V}$
- $KW/L = 2\text{ mA/V}$
- $\lambda = 0.01\text{ /V}$
- $C_{gs} = 10\text{ pF}$
- $C_{gd} = 2\text{ pF}$
- $V_{dd} = 10\text{ V}$
- $V_{GG} = 6\text{ V}$
- $C_L = 100\text{ pF}$
- $R_D = 4\text{ k}\Omega$
- $R_L = 4\text{ k}\Omega$
- $R_s \approx 10\text{ k}\Omega$

• **Find:**

- Opt. point
- Values of small signal pars.
- Voltage gain, ≈ 1
- Output Imp.
- Input Cap.
- Upper cutoff freq.

So, if you see the voltage gain coming from gate to source that is approximately 1, that is what we said. But in addition to that, if you see the C_{gd} and the voltage coming here we call say V_d so $V_{small d}$. So, that is definitely it is nonzero and the voltage coming here it is V_{in} multiplied by approximately multiplied by R_D divided by the so, that is multiplied by $g_m R_D$ divided by $1 + g_m R_L$.

So, if I consider this resistance is very high compared to R_D . So, that is what I will be getting and this can be well approximated by R_D by R_L with a of course, a minus sign. So, now, in this example since we are taking both of them are equal. So, we can say that the voltage gain from here to here, it will be close to 1 with a minus sign. So, we can see that C_{in} ; its primary contributor is C_{gd} , but it is getting affected by this voltage gain, $1 - V_d$ divided by V_{in} and this part it is given here.

So, from this equation if you see this part it is C_{gd} multiplied by 1 and then minus 1 is also there. So, it becomes plus 1 R_D by R_L . So, I should say that this becomes practically 4 pico Farad. So, what is the conclusion here it is even though we do have R_D here and we do have the signal coming here since, C_{gd} it is small and then the input capacitance still it is remaining low.

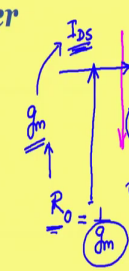
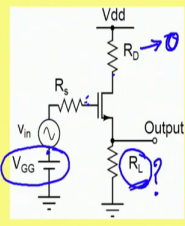
But, we need to be careful that R_D may be allowed to some extent, but if the R_D it is coming more and more then, the contribution of the C_{gd} to the input capacitance it will be large. And as a result the upper cutoff frequency defined by R_S and the C_{in} that may be a problem.

So, unnecessarily, we should not be putting this R_D . So, that is what the conclusion. So, let us see what is the design guidelines we can follow based on this knowledge? So, let me I think I do have a slide for that.

(Refer Slide Time: 56:47)

Design guidelines: CD amplifier

- $V_{th} \approx 1\text{ V}$
- $KW/L = 2\text{ mA/V}$
- $\lambda = 0.01\text{ /V}$
- $C_{gs} = 10\text{ pF}$
- $C_{gd} = 2\text{ pF}$
- $V_{dd} \approx 10\text{ V}$
- $C_L = 100\text{ pF}$
- $R_s \approx 10\text{ k}\Omega$
- $V_{GG} = ?$
- $R_D = ?$
- $R_L = ?$



- Opt. point
- Values of small signal pars.
- Voltage gain,
- Output Imp.
- Input Cap.
- Upper cutoff freq.

(Note: The slide includes a video feed of a presenter in the bottom right corner and a Windows taskbar at the bottom.)

So, with here it is the analysis the knowledge of the circuit analysis can be utilized where in the analysis part; we have started the calculation from top to bottom of this list. While these parameters it was given to us. So, that was the numerical analysis we have done for the common collector or common drain circuit.

Now, if we have to make a design, where in fact, these parameters it will be given to us. Voltage gain should be close to 1, then output impedance it will be given to us, then maybe for a given value of the load capacitance; the cutoff frequency may be given to us from that we need to calculate R O.

So, this output impedance we can find. So, the way we will be proceeding while we have to design the circuit it is basically from bottom to up. And so, from the requirement of the output impedance which we know that this output impedance is 1 by, roughly 1 by g_m and that gives

us the requirement here. So, then once you have the value of the g_m , from that we can calculate what will be the corresponding I_{DS} .

So, what is the sequence? From R_O we calculate g_m and then from that we calculate I_D or I_{DS} . And to achieve this I_{DS} , we can find what supposed to be the meaningful DC voltage and what will be the corresponding meaningful resistance of the source. And better, we should avoid this resistance and ideally we want this resistance should be 0. So, that unnecessarily we do not want to complicate the circuit and contribution of the C_{gd} , we do not want to take it to the input capacitance otherwise that will affect the upper cutoff frequency.

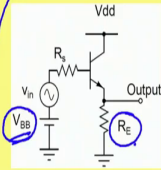
So, the summary of the design guidelines is that we start from output resistance particularly for common drain circuit then we calculate g_m , we calculate the required I_{DS} to achieve the required I_{DS} , then we can find what will be the value of this one and also the corresponding DC voltage here. In fact, this DC voltage it may be coming from the previous stage. So, in case if this is given to us; accordingly, then we can calculate the corresponding R_L . So, it boils down to the point that we need to calculate the corresponding R_L of the circuit.

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Design guidelines: *CC* amplifier

- $V_{BE(on)} \approx 0.6\text{ V}$
- $\beta = 100$
- $V_A = 50\text{ V}$
- $C_{\pi} = 10\text{ pF}$
- $C_{\mu} = 5\text{ pF}$




- $V_{DD} = 10\text{ V}$
- $V_T = 26\text{ mV}$
- $C_L = 100\text{ pF}$
- $R_S \approx 100\text{ k}\Omega$

- $R_E = ?$
- $V_{BB} = ?$

- Opt. point
- Values of small signal pars.
- Voltage gain,
- Input Imp.
- Output Imp.
- Input Cap.
- Upper cutoff freq.

I_C

R_O

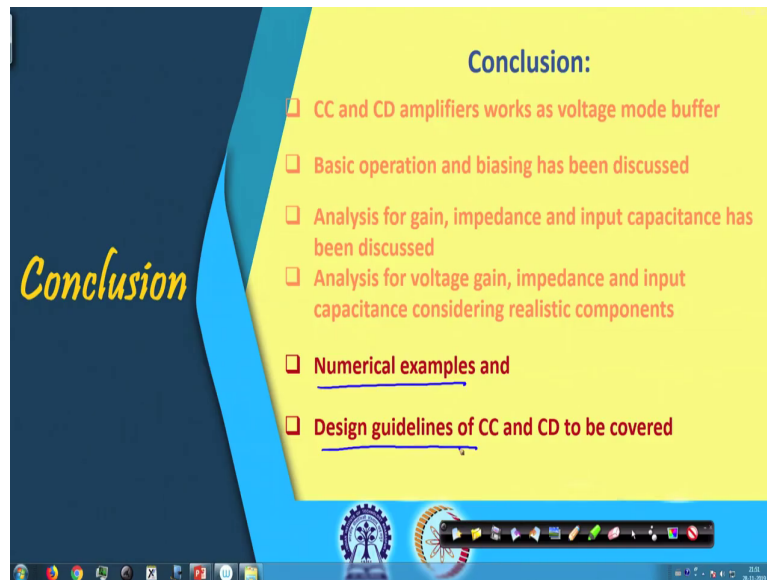


So, similar kind of guidelines it can be followed for the common collector circuit also. Where, again the information may be given or rather requirement it will be given for the upper cutoff frequency for a given load capacitance. So, from that we need to calculate what is the R_O . And this R_O , since it is predominantly defined by g_m from that we can find what is the corresponding trans conductance and from that we can find what will be the corresponding collector current. And if the collector current is known to us, then for a given value of V_{BB} , we can find what will be the corresponding R_E .

So, if V_{BB} , it is given to us then, the last thing it is we need to find the corresponding R_E . But whatever the calculation we will be doing. We are assuming that the remaining parameters are given to us. Namely, the device parameters particularly the early voltage and C_{π} C_{μ}

even though we do have so many parameters, but primarily we do have the main thing is the collector current and gm it is defining the circuit performance of this voltage buffer.

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Conclusion:

- ❑ CC and CD amplifiers works as voltage mode buffer
- ❑ Basic operation and biasing has been discussed
- ❑ Analysis for gain, impedance and input capacitance has been discussed
- ❑ Analysis for voltage gain, impedance and input capacitance considering realistic components
- ❑ Numerical examples and
- ❑ Design guidelines of CC and CD to be covered

I think we need to conclude now. So, what we have done today? It is we are we have concluded with numerical examples and exhaustive numerical examples it is giving us to understand how we proceed for designing a circuit. So, the design guidelines of the common collector and common drain, it is also covered and so, that is all about this second configuration. Now in the next class; we will be going for the other configuration namely the common base and common gate configuration.

Thank you for listening.