

Analog Electronic Circuits
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Lecture - 25
Common Emitter Amplifier (Part B)

Welcome back after the short break.

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CE amplifier – Fixed bias (contd...)

• Small signal equivalent circuit(s)

The diagram shows a common emitter amplifier with a fixed bias network. The small signal equivalent circuit is shown with an AC voltage source V_s and a resistor R_B connected to the base. The emitter is grounded, and the collector is connected to a collector resistor R_C and a load resistor R_L . The output voltage V_{out} is taken across R_L . Handwritten annotations include: $V_{out}/V_s = -g_m R_o A_v$, $V_{out}/V_s = -R_C/g_m$, $V_{out}/V_s = -R_C \beta/g_m$, $V_{out}/V_s = -R_C \beta/g_m = A_v$, $i_c = \beta i_b$, $i_c = \beta V_{be}/g_m$, and $i_c = \beta V_{be}/g_m = g_m V_{be}$.

So, we are discussing about the CE amplifier, then we are close to the small signal equivalent circuit. So, large signal analysis we have done and based on the large signal analysis, what we said is the DC voltage here it is fixed.

So, whenever we are going for small signal, first thing is that we will be considering this DC part is 0. And so, we can say that this is AC ground; of course, we do have this ground. Then next thing is that these capacitors are working as a short and whatever the circuit will be having, it is now that we will call the equivalent circuit.

In addition to that base to emitter, we are also having one V_{be} on internal DC voltage that also need to be met 0. So, base to emitter what we have it is the r_{π} . We do have this r_{π} , then we do have the signal coming here. So, we do have the signal directly coming here.

Along with this r_{π} of course, we do have R_B , $R_{\text{capital B}}$ and this is connected to ac ground which means that this R_B and this r_{π} , they are coming in parallel and typically this resistance is very high compared to this one. So, we may ignore this part, we can simply consider this r_{π} .

And then on the other hand the collector side so, this is the base node, this is the collector side. At the collector side, we do have R_C which is connected to V_{cc} which is now ac ground. So, this is ac ground I am using red color ground here just to indicate that this is valid for ac signal only.

And then from collector to emitter we do have the current this I_C current, but here again, here it is having the DC part as well as the small signal part. So, we should say that DC part we are dropping it and what we have it is only the small signal part I_C .

So, this I_C equals to βi_b and the i_b it is whatever the current it is flowing from the signal source into the base. So, this i_b if you see here this i_b , it is this is V_s divided by r_{π} . So, this is what the i_b . Now that i_b it is after multiplying with β , βi_b it is giving us the on the small signal collector current.

That current is flowing through this resistance which is producing a voltage and for it may be noted that the signal here though it can go positive and negative, but for correct polarity and consistency of the input to output signal phases, we need to put a sign.

Say for example, here whenever you are talking about base to emitter voltage, this is signal voltage it can go plus and minus, but then we are putting plus sign here and minus sign here; same thing for polarity of the i_b . So, we are considering this is the positive direction of the base current.

Likewise whenever we do have the collector current, this is the positive direction of the collector current with respect to that if the collector current is flowing in this direction the developed voltage here it will be this will be minus and this is plus. So, the voltage coming at this point it is minus R_c multiplied by this i_c in. So, that is minus R_c into beta naught into i_b . Further to that we can write this as minus R_c beta naught into i_b it is v_s divided by r_{π} .

So, that is what the v_{out} . So, we can say that this v_{out} expression is this given here. So, this v_{out} expression it is given here. So, from that I can say that v_{out} , I should use this small v_{out} divided by v_s equals to minus R_c multiplied by beta naught divided by r_{π} . So in fact, this is nothing, but our voltage gain.

In small signal model, if we map this equivalent circuit into voltage amplifier small signal voltage amplifier, then this is representing as the voltage gain A_v . So, we will see that again this A_v , but its expression it is given here. Now this small signal equivalent circuit it may be having two ways of representing. The first one just now we are discussing, the other one it is again similar only difference is that let me use a different color to consider that this i_c instead of writing in terms of i_b . Let me use blue color.

So, instead of using i_b we can write i_c equals to. In fact, we can write beta naught i_b it is v be divided by r_{π} all right. And so, this v be divided by r_{π} this parameter, it is of course, it is a small signal parameter we already have discussed earlier. This is g_m trans conductance of the transistor multiplied by then this v_{be} . So, this part it is basically the trans conductance of

the amplifier. So, in this red color what you have done is that this current, we are writing in terms of i_b which means that this current source it is current dependent current source.

On the other hand if I you say, this model then this is voltage dependent current source right. So, this v_{be} it is defining this the current. And then the remaining things; however, it remain same namely the output voltage here, it is minus R_c into i_c and instead of writing beta into i_b naught, now I can write this as minus R_c into g_m into v_{be} and incidentally this v_{be} , it is same as v_s . So, we can write this as minus $R_c g_m$ into v_s .

Again this is representing the same v_{out} and with this we can say that v_{out} divided by v_s equals to minus g_m into R_c . This is again the expression of the voltage gain if we are representing this whole circuit as equivalent voltage amplifier.

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CE amplifier – Fixed bias (contd...)

• **Small signal equivalent circuit(s)**

The diagram illustrates the small signal equivalent circuit of a CE amplifier with fixed bias. It shows a signal source V_s with internal resistance r_{π} connected to the base of a BJT. The base is biased by a fixed bias network consisting of a resistor R_b connected to V_{cc} and the base. The collector is connected to V_{cc} through a resistor R_c . The output voltage V_{out} is taken from the collector. Handwritten annotations include: i_b at the base, $i_c = g_m v_{be}$ at the collector, and $A_v v_{be}$ at the output. A smaller inset circuit shows the full fixed-bias circuit with V_{cc} , R_b , R_c , and the BJT, with V_{be} and V_{out} labeled.

So, I should say that the this circuit we do have while we are mapping this circuit in the form of small signal equivalent circuit, there are so, this circuit whole circuit we are mapping in this form and it is having two ways of writing this small signal i_c here; one is in terms of $g_m v_{be}$ the other one it is βi_b .

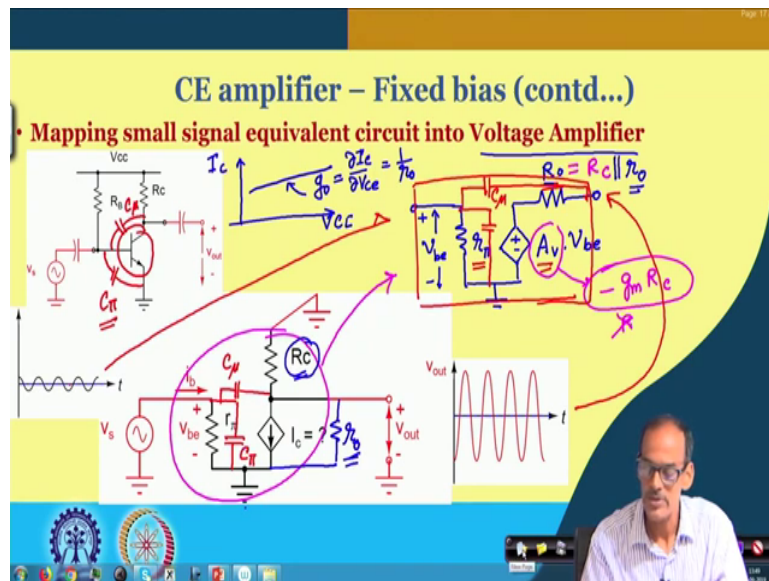
Now, if we are mapping this circuit in the form of voltage amplifier, we prefer this expression over this one that is because then input we are considering it is input signal we are considering as voltage rather than current. So, maybe in other model while we are considering say the same CE amplifier as current gain current amplifier or maybe impedance amplifier, then we may use say the other model here.

So, if I use say this current source as $g_m v_{be}$, whatever we will be getting it is equivalent I should say that will be the input signal it is the voltage. Now if I consider this output as voltage; obviously, then this current source along with this R_c , we need to translate this circuit in the form of Thevenin equivalent.

So, once we translate this into Thevenin equivalent model, then only we will be getting the output port as voltage source and we need to map into this normal model the known model which is $A v_{in}$ and in this case v_{in} it is basically the v_{be} . And then we do have the output resistance and incidentally this output resistance and this output resistance they are same ok.

So, now, if we map this small signal equivalent circuit into a voltage amplifier, what we are getting it is the following.

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So, we are discussing about the this small signal model. And now if we translate this model in the form of voltage amplifier, what is the voltage amplifier will be getting it is voltage dependent voltage source at the output port and then we do have the output resistance R_o . So, voltage dependent voltage source it is A_v times the input port voltage

In this case v_{in} it is v_{be} . So, this is plus and this is minus this is connected to ground and then at the input we do have the r_{π} . So, the input resistance is r_{π} of the transistor and at the across this r_{π} , we do have the v_{be} voltage. So, this is plus and this is minus indicating if this is plus and this is minus the corresponding voltage here this should be in phase.

However we already have discussed that expression of this A expression of the A , it is minus g_m into R_c or we also have said that in terms of current. So, for the timing let me stick to this one forget about this one and then output resistance it is same as the R_c .

So, this circuit whatever the circuit, we have discussed here small signal equivalent circuit we can map into this model the voltage amplifier model. Having this three important parameter A_v , output resistance and then input resistance here. So, this is input resistances r_{pi}

And at the input of course, we are giving the signal with a 0 voltage here and at the output we are getting the signal all right. So, that is about the how we are mapping the circuit into voltage amplifier. Note that this model, it is valid for low frequency as well as in the mid range frequency.

However, if you go to higher and higher frequency, then the this device may be having this device may be having its own parasitic capacitances from base to collector it may be having one capacitance and then base to collector it is having another capacitance. So, base to collector capacitance, it is referred as C_{pi} and then we do have the C_{mu} .

These are essentially small signal capacitance associated with the BJT. So, if we are considering small signal equivalent circuit and particularly in the high frequency range, then this capacitor and then this capacitor they are again popping up and we need to consider them. So, we need to consider this C_{pi} and then C_{mu} ok.

Then of course, we can consider their equivalent circuit here which is having the C_{pi} and then C_{mu} . Note that C_{mu} need to be connected to this point not this point ok. So, in addition to that I must say that so far, we are ignoring the early voltage effect namely the dependency of the collector current on the V_{ce} we are ignoring.

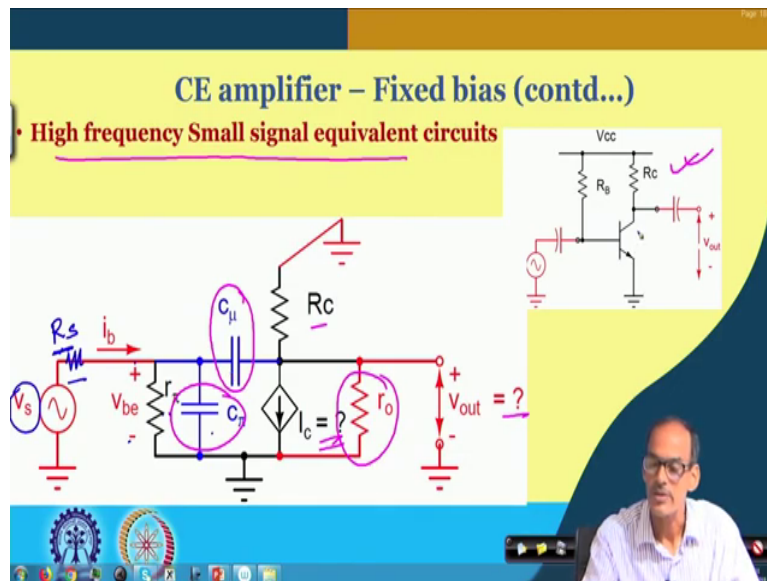
But in case if we want to consider whatever the dependency, it is having slight whatever positive slope in the active region and this slope will be represented by finite conductance called g_{naught} which is defined as change in I_c with respect to change in V_{ce} .

And this is called small signal reciprocal of small signal output resistance R_O . So, if you consider this resistance or this finite slope, what will be getting here it is that one resistance here which is either you can write in the form of conductance or resistance R_O and so, this resistance since it is coming in parallel with R_C .

And as this is connected to ground, this is also connected to ground. So, the output resistance R_O , it will be rather R_C in parallel with small R_o . So, this represents the complete model of the c_e amplifier small signal model of the CE amplifier which is valid for low frequency as well as high frequency. And of course, in the low frequency region ah, then the c_{pi} and c_{mu} they are effected to be very negligible and also this typically this r_{naught} it is quite high compared to R_c . So, we may still consider this is R_c .

But once we replace this passive element by active element which may be having output resistance comparable with this and then we must have to consider this r_{naught} .

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So, to avoid this so much of clumsy things, let me go to the next slide where I have the clear diagram of the small signal model. So, what we have as I said that the in the small signal model we do have r_{π} and then R_c which is the output resistance and so and so, and then we do have this resistance this capacitance and this capacitance, they are getting added up and also to take care of the early voltage effect we do have r_o .

So, this small signal model, it is referred as high frequency a small signal equivalent circuit of the CE amplifier. So, this derivation we already have said. So, nothing to discuss about that and in case I must say one thing, I must add one thing that this in case the source resistance is having source signal source is having source resistance R_s , then this voltage need not be same as this one.

So, then we may have to consider this R_s and then r_{pi} to consider this voltage and once you go to higher and higher frequency this R_s in combination with r_{pi} and then C_{pi} also effect of C_{mu} , you may call it as equivalent input capacitance all of them are going to contribute to define the cutoff frequency of the amplifier.

So, this capacitors are they will be playing important role to define the bandwidth of the circuit. So, whenever the situation comes, we will discuss that in detail. Now let us see or lest let me highlight one issue of this fixed bias CE amplifier is having particularly the operating point it is sensitive to beta of the transistor.


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Sensitivity of Operating point of CE Amp

- Operating point of Fixed bias CE amp is sensitive on β of the BJT

• A series Resistor R_E is added at the emitter terminal to de-sensitize the operating point



So, then to let me use a different slide to discuss that point. Sensitivity of operating point as I said sensitivity of operating point of the CE amplifier particularly if it is fixed bias. So, if it is

fixed bias namely the I_B , it if it is decided by this R_B and V_{be} one and V_{CC} then the collector current I_C which is β times I_B .

So, as a result if I fix this I_B and then if I replace this transistor by another one having different value of this β , definitely the corresponding I_C , it will be getting changed. So, what will be the consequence? To explain that, let me go back to our previous method of finding operating point of the circuit. So, where do we is to draw this I_C versus V_{CE} . So, we used to draw I_C versus V_{CE} characteristic curve for a given value of I_B .

So, I_B it is fixed and then also we do, we used to draw the load line. So, is to draw the load line defined by this R_C and V_{CC} . So, this node this point it is V_{CC} and so, these two together it was giving the operating point there.

Now typically we like to avoid of course, this point as well as the saturation point and whenever it is to give a signal here, we are adding the I_B as a result this total I_B , we are expecting that if the signal is present, then it will be going up and down like this one. And as a result this the crossing point of the device characteristic and the load line they used to, it is to move from here to here and as a result it was products in the output voltage.

So, if this operating point is properly set, then if the in presence of I_B the I_C maybe it is changing over this range and this the meeting point, it was shifting from this point to this point and as a result it was giving the output signal.

And to get a very good swing we want this operating point should be middle of this range. What is this range, which is defined by upper side it is defined by supply voltage V_{CC} and lower side it is defined by the limit of the active region which is referred as $V_{CE\ set}$; $V_{CE\ set}$ saturation.

So, we like to keep this operating point middle. So, that both the lower as well as the upper swing of the signal is to get a good one. Now if you see that in case suppose, we are fixing this R_B which is deciding this i_b and then if you replace this transistor having different β .

So, then what it be it would be happening is that this line for the same I_B because of different beta it may be getting shifted here.

So, this beta if it is say beta F2 from beta F1, then the q point, now it is getting shifted from here to here. And if the q point it is coming here; obviously, the signal swing if you see this side it will be very much limited. This side it may be getting extended, but since this lower side it is getting limited, then if you apply the signal the signal limit it will be decided by the lower one out of these two limits.

So, as a result if the beta is getting changed from the previous value to this new one, the I_C characteristic it is getting shifted here. And then the operating point since it is coming here so, that may create the signal and getting distorted towards the lower side. So, if you still continue giving the same amplitude signal for this operating point so, what we are expecting that, then the corresponding output signal let me draw here. It will be getting huge distortion and this side it may be like this.

So, this distortion of course, for analog circuit it is not acceptable. So, that creates the main problem the change of this beta, it may be due to various region. In case if you want to replace this transistor by another one and you do not know the beta, then it may create problem and to get the same value of the beta using which you have obtained this operating point may not be practically a good solution.

The other problem are which is the typical problem, it is that this beta it is a strong function of temperature. So, in case if the junction temperature of this BJT is increasing this beta, it may increase as a result this operating point it may be going up there. And that may affect the q point operating point of the circuit drastically which is referred as thermal runaway problem.

Why is it called runaway problem? If I_C it is increasing due to increase of beta maybe that is due to originally due to increase of temperature and if the I_C is increasing and then that may increase the power dissipation of the in the junction and that may further increase the temperature and then that may lead to again increase the beta. As a result it is having

cumulative effect to increase the beta and on this q point of the circuit it may it may go towards the saturation limit or active region limit.

So, this problem can be as I said that this is a problem which is referred as the thermal runaway problem for C E amplifier particularly if it is fixed bias. So, what is the solution for this is we can add a series resistor at the emitter. So, if you add one series resistor called R_E and then instead of fixing this current probably we can try to fix the voltage here by different means and then we can the we will be seeing that the operating point will be having a better stability.

So, that gives us something called from now voltage bias with emitter degenerated. So, this R_E it is referred as emitter degenerated which desensitize the operating point of the circuit, but of course, will be discussing the topic later. But since we are desensitizing the circuit by placing this R_E that will that also affect the gain of the circuit. Now to get back the gain, we need to connect one bypass capacitor.

So, this is this will be discussed in the next day, but just to give a hint that yes C E amplifier with fixed bias it is one good amplifier, but it is having this issue need to be addressed differently and we will see that how this node it will be biased in the form of voltage namely by using a potential divider, those things will be covered in the next class.

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Conclusion:

- ❑ Operation of CE Amplifier
- ❑ Biasing of CE amplifier:
 - ❑ Fixed bias ✓ R_B
 - ❑ D.C. decoupling capacitors C_c
- ❑ Analysis CE amplifier
 - ✓ Operating point and
 - ❑ Small (a.c.) signal → V. Amp
- ❑ Sensitivity problem in Fixed bias CE amplifier

So, what we have discussed today let me summarize. We have started with simple operation of the CE amplifier rather earlier whatever the knowledge we already have gathered that we have discussed. And then we have discussed the biasing of the CE amplifier namely how we define the operating point of the circuit by connecting a base resistor called fixed bias resistor R_B at the base.

And then we put a DC decoupling capacitor to feed the signal. So, in combination with R_B and a capacitor C_c called coupling capacitor C_c to feed the signal, we obtain the appropriate arrangement of the circuit. And then we have analyzed the operating point little detail by considering the input port situation and then output port situation for large signal and then we have discussed about the small signal equivalent circuit.

And then we map that equivalent circuit into a voltage amplifier. At least as I said that typically CE amplifier it is considered as a voltage amplifier. So, that is what we have done. We have mapped into voltage amplifier.

And then finally, we have discussed about the issue for which is existing for fixed by a CE amplifier namely the operating point is sensitive to beta of the transistor and that will be that need to be addressed by different means. So, that will be our next topic of our discussion. I think we are end of it.

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Thank you for listening.