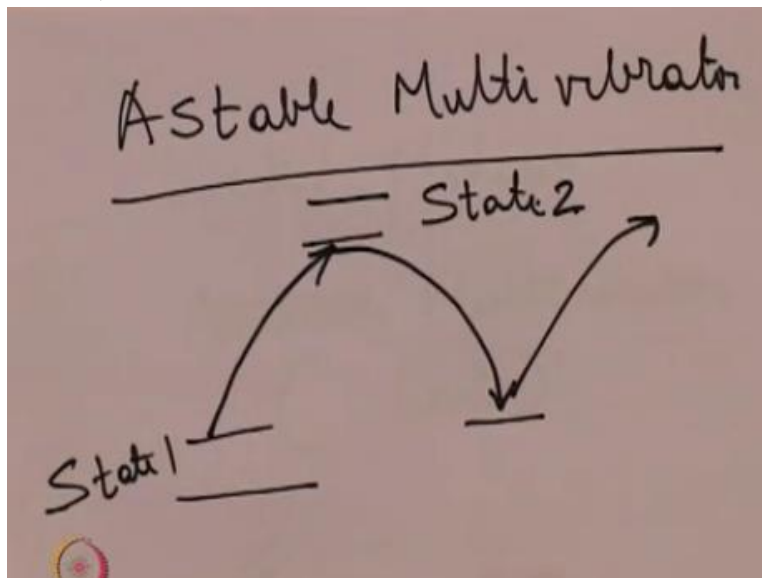


**Analog Circuits**  
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**Week 07**  
**Module 04**  
**Multi vibrators (Contd..)**

Hello, welcome to another module of this course analog circuits, so in the previous module we had talked about bi-stable multi vibrator in this module we shall be discussing about the other type of multi vibrator that I mention which is the Astable multi vibrator.

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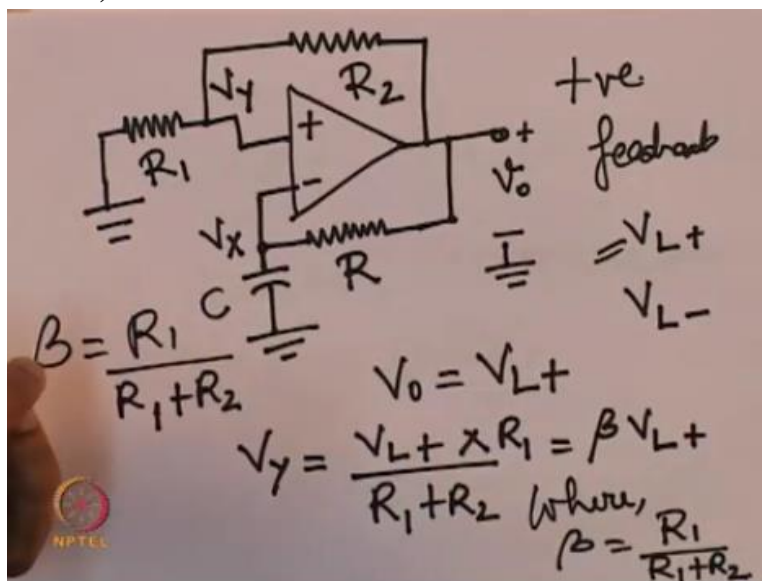
So as I had discussed in the previous modules that multi vibrators are special classes of analog circuits they are non linear analog circuits, because they do not their output is not always proportional to the input or there might be some abrupt changes in the output they might be acting linear in some regions but not in all regions of the input signal, so Astable multi vibrator and which I mention is that if this is state 1 and this state 2 then as time passes the system will transition from state 1 to state 2 and then come back to state 1 and then again go to state 2.

So it is never in any stable state in the bi-stable for the bi-stable multi vibrator, I had mentioned that there are 2 stable states that is if the system is in state 1 then it will continue to be in state 1, if the system is in state 2 if you continue to be in state 2 but for Astable multi vibrator that is not the case if the system is in state 1 it will inevitably transition to state 2 after some time it may

stay stable in state 1 for some time but not for all this again benefit is if the system is in state 2 it will stay in that state for some time and then inevitably come back to state 1 so this is the theory behind the Astable multi vibrator.

Let us see how to implement such a circuit so we are discussing about circuits Astable multi vibrator using opamps there are also other ways to implement Astable multi vibrator is using MOSFET's but here for this course we will be restricting our discussions to those circuits which are based on opamps only.

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So the circuit for an Astable multi vibrator is like this, this is the circuit again we see the feedback from the output is fed to the non inverting input not to the inverting input so the feedback is positive that is the first thing to know and now in addition to the resistances we also have a capacitance C as you know capacitance is a charge storage element.

So the voltage across this capacitance is not constant it will charge or discharge depending on the voltage difference across its terminals and the voltage that it is connected to and essential this capacitance is the element that provides the necessary timing that is the timing for transition from one state to another.

So let us analyze this circuit, so the output of the opamp as we had discussed earlier it can be in one of the 2 saturation states suppose one saturation state is  $V_{L+}$  and the other saturation state is

$V_{L-}$  and say initially the output of the opamp is at  $V_{L+}$  then the voltage at  $V_y$ , so initially  $V_0$  is  $= V_{L+}$  for this value of  $V_0$   $V_y$  will be  $= V_{L+}$  upon  $R_1 + R_2$  multiplied by  $R_1$  and let us call this value beta this  $R_1$  upon  $R_1 + R_2$  as beta so I can write  $V_y$  like this where beta is = okay and let me write it more clearly here ok what about this voltage  $V_x$ .

Now see when  $V_0$  is at the upper saturation voltage and say the voltage across C does not is a 0 or much less than that upper saturation voltage then due to this voltage difference this C will start charging and what is the equation for the voltage across this capacitance when it is charging so can I write the voltage value across the capacitance or this  $V_x$  value if we can go here.

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$$V_x = V_{L+} - (V_{L+} - \beta V_{L-}) \times e^{-t/\tau}$$

for  $t=0$ ,  
 $V_x = \beta V_{L-}$

for  $t \rightarrow \infty$   
 $V_x = V_{L+}$

So this  $V_x$  value I can write it like this  $V_x$  is  $= V_{L+} -$  of  $V_{L+} -$  beta  $V_{L-}$  e raise to  $- t$  upon tau, so according to this equation when time is 0,  $V_x$  will simply be  $=$  beta  $V_{L-}$  so initially the voltage across the capacitance is beta  $V_{L-}$  the lower where  $V_{L-}$  is the lower saturation voltage at the output but when  $T$  tends to 0 for a beg your pardon when  $T$  tends to infinity  $V_x$  will be  $=$  it will be  $= V_{L+}$ .

So had we allowed this capacitor to charge forever then the voltage across the capacitance would eventually be  $= V_{L+}$  the upper saturation voltage at the output but that will not happen that will not happen because this capacitor will keep on charging this till the time  $V_x$  is lesser than  $V_y$  once  $V_x$  exceeds  $V_y$  then however because of the property of this opamp that whenever the inverting input voltage exceeds the voltage at the non inverting input the output will get reversed

so the moment  $V_x$  crosses  $V_y$  the output will go from  $V_{L+}$  to  $V_{L-}$  so what is the time that it will take for  $V_x$  to reach  $V_y$  value.

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When  $V_0 = V_{L+}$   
 $V_y = \beta V_{L+}$   
 $V_x = V_{L+} - (V_{L+} - \beta V_{L-}) e^{-t/\tau}$   
 Say at  $t = T_1$ ,  $V_x = \beta V_{L+}$   
 $\beta V_{L+} = V_{L+} - (V_{L+} - \beta V_{L-}) e^{-T_1/\tau}$   
 $T_1 = \tau \ln \left[ \frac{1 - \beta \left( \frac{V_{L-}}{V_{L+}} \right)}{1 - \beta} \right]$   
 Time constant

So our if we write it on a fresh sheet  $V_y$  is given by  $V_x$  is given by ok say at time  $T_1$   $T = T_1$   $V_x$  becomes  $= \beta V_{L+}$  so then let me substitute that  $\beta V_{L+} = V_{L+} - (V_{L+} - \beta V_{L-}) e^{-T_1/\tau}$  upon  $\tau$  and the value of  $T_1$  if we solve this equation that we should get is like this like this, now here I did not mention what this  $\tau$ ,  $\tau$  is called the time constant for an RC based circuit.

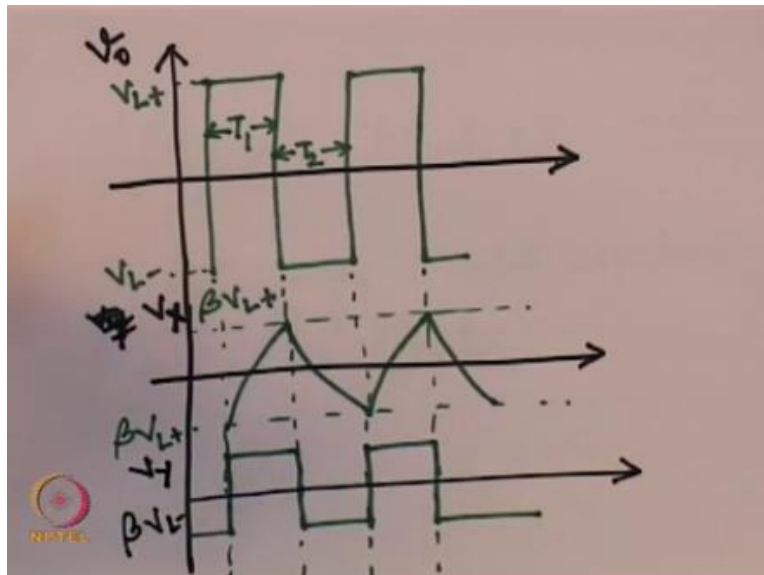
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For an RC based circuit,  $\tau = RC$ .  
 For a LR based circuit,  $\tau = L/R$ .

As we have in our case, tau is given by RC for LR or an inductor resistive resistance circuit tau is = L upon R so now that we have this our time constant which is = RC so let us go back to our circuit (Refer Slide Time: 12:59).

So let us come back to our circuit once again this is the circuit which we were discussing and we say that when  $V_0$  is = the upper saturation voltage  $V_{L+}$   $V_x$  will keep on increasing or in other words this capacitor will keep on charging till the point where  $V_x$  exceeds  $V_y$  and then once that happens the output  $V_0$  will change from  $V_{L+}$  to  $V_{L-}$  and that transition or the time taken for the capacitance to charge to  $V_y$  is given by T time capital T1 so if we plot this on a graph how will it look like.

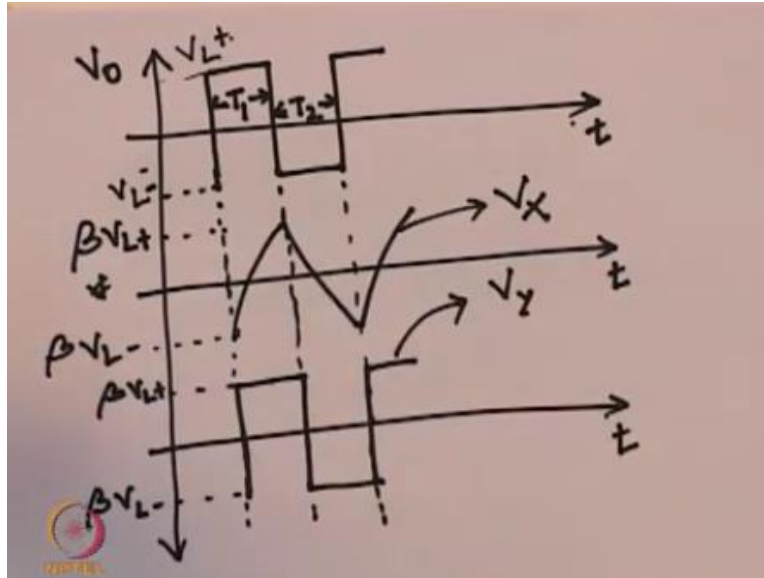
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So I have my  $V_0$  I use the green pen so initially when  $V_L$  is at state 1 at the upper saturation voltage or sorry I should say the  $V_0$  is at the upper saturation voltage  $V_{L+}$  it will remain in that state for time  $T_1$  after which it will transition to the lower saturation voltage and the corresponding  $V_y$  response will be something like this sorry this will be  $V_x$  please note this correction this will be  $V_x$  and this is  $V_y$  please note this correction this voltage that I showed here is  $V_x$  and this is  $V_y$  okay, we will come to the description of time  $T_2$  later on but for now let us see that is this  $V_x$  how  $V_x$   $V_y$  and  $V_0$  are changing with time.

So we were discussing about the properties of this Astable multi vibrator, we saw that by this voltage when the  $V_0$  is at the upper saturation voltage the  $V_x$  or the voltage across the capacitor keeps on increasing till the point where  $V_x$  exceeds  $V_y$  and then once  $V_x$  exceeds  $V_y$  the voltage  $V_0$  goes from the upper saturation voltage to the lower saturation voltage and the time take for the  $V_x$  to reach that  $V_y$  value where the transition takes place is given by capital  $T_1$  and let us see graphically how this looks like.

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So the top graph is  $V_0$  the middle graph is for  $V_x$  and the bottom most graph is for  $V_y$  so this graph kind of shows you know the what we were discussing mathematically say initially the voltage  $V_x$  or the voltage across the capacitor is  $V \beta V_L^-$  and you must be asking me a question why did I consider the initial voltage as  $\beta V_L^-$  isn't it?

I mean initial voltage would have been 0 but then what happens is yet it is true that initially at the very beginning of operation the voltage across the capacitor will indeed  $V_0$  but then once it is operating it will be bounded between  $V_x$  will be bounded between  $\beta V_L^+ + \beta V_L^-$  because in the same way that we saw that there is transition occurring when  $V_x$  reaches  $\beta V_L^+$  we shall also be seen that there will be another transition occurring when  $V_x$  reaches  $\beta V_L^-$ .

So  $V_x$  can never go below  $\beta V_L^-$  or it can never exceed  $\beta V_L^+$  because whenever say it goes below  $\beta V_L^-$  the transition will happen in  $V_0$  here and it will from the state of charging or discharging it might go to a state of discharging and charging respective.

So  $V_0$  stays at this value  $V_{L+}$  for a total time of  $T_1$  once  $V_x$  reaches  $\beta V_{L+}$   $V_0$  undergoes a transition from the upper saturation voltage to the lower saturation voltage  $V_y$  also simultaneously with  $V_0$  undergoes a transition from  $\beta V_{L+}$  to  $\beta V_{L-}$ , once  $V_0$  reaches  $V_{L-}$  - the supplied voltage to the capacitor is actually lesser than the voltage across the capacitor which is  $\beta V_{L+}$ , so once this transition happens the capacitor is subjected to an input voltage of  $V_{L-}$  whereas its voltage across the capacitor is  $\beta V_{L+}$ .

So the capacitor actually starts discharging so what is the equation when the capacitor starts discharging, so in this phase for time  $T_1$  charges and then once the transition happens it discharges and that discharging as we shall see happens also for a certain time which we shall call  $T_2$  okay, so what is the equation for the of the capacitor during the discharging phase?

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Handwritten equations on a whiteboard:

$$V_x = V_{L-} - (V_{L-} - \beta V_{L+}) e^{-t/\tau}$$

at  $t = T_2$

$$V_x = \beta V_{L-} = V_y$$

$$T_2 = \tau \ln \frac{1 - \beta \left( \frac{V_{L+}}{V_{L-}} \right)}{1 - \beta}$$

Time period,

$$T = T_1 + T_2 = 2\tau \frac{1 + \beta}{1 - \beta}$$

for  $V_{L+} = -V_{L-}$

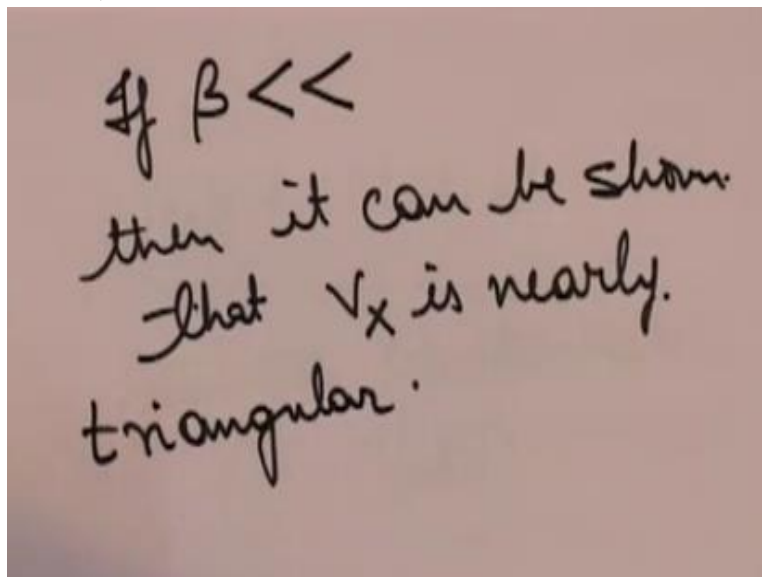
The equation across the capacitor or  $V_x$  is given by ok say at  $T = T_2$   $V_x$  becomes  $= \beta V_{L-}$  if you go back to the circuit once again, so now  $V_y$  is  $= \beta V_{L-}$  - ok the where  $V_{L-}$  is the lower lower threshold voltage or I beg your pardon where  $V_{L-}$  the lower saturation voltage  $V_x$  this capacitor is discharging so  $V_x$  is going down it will go down till the point again when  $V_x$  becomes lesser than  $V_y$  when there will again be a transition ok.

So we this capacitor will keep on discharging till  $V_x$  reaches  $V_y$  given by  $\beta V_{L-}$ , once that happens  $V_0$  will undergo a transition from the lower saturation voltage to the upper saturation voltage, so say at time  $T = \text{Capital } T_2$   $V_x$  is  $= \beta V_{L-}$  which is  $= V_y$  then that  $T_2$  if you substitute  $T = \text{capital } T_2$  in this equation and then solve for capital  $T_2$  will get the value of capital  $T_2$  as.

So then what is the time period or in other words what is the total time taken for this multi vibrator to start from a certain state and come back to the certain state the time period is this time for this for the charging phase capital  $T_1$  and for the discharging phase capital  $T_2$  so the time period  $T$  capital  $T$  is given by which is given by so when  $V_{L+}$  is  $= -$  of  $V_{L-}$  and the upper and lower saturation voltages and the output are the negative of each other for this condition the total time period is given by  $2\tau \frac{1 + \beta}{1 - \beta}$ .

Now usually this condition is satisfied sometimes for example if the saturation voltage is same as the supply voltages and say the supply voltages are  $+$  and  $- V_{ss}$  then usually this condition will be satisfied that is the upper saturation voltage will indeed be the negative of the lower saturation voltage.

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If  $\beta \ll$   
then it can be shown  
that  $V_x$  is nearly  
triangular.

Now there is a particular condition when beta is very less, say if beta is very small then it can be shown that that  $V_x$  is nearly triangular of course it may not be perfect triangle for getting a perfect triangular waveform we need some special techniques we shall we shall discuss in a



subsequent module but if beta is quite small then you know we can indeed achieve a nearly triangular output at  $V_x$ , so in that case  $V_x$  itself can also be treated as an output.

So in this module we covered the topic of Astable multi vibrator and saw that this Astable multi vibrator just the bi-stable multi vibrator has two states but unlike the bi-stable multi vibrator the 2 states are not stable that is one state if the circuit is in one state or as in our case if  $V_0$  is at the upper saturation voltage after time  $T_1$  it will go to the lower saturation voltage and thereby enforcing the state change and then once it is  $V_0$  is at  $V_{L-}$  or the lower saturation voltage again after time  $T_2$  it will move on to the upper saturation voltage  $V_{L+}$  does  $V_0$  keeps shifting from  $V_{L+}$  to  $V_{L-}$  and this is periodic.

So after time  $T_1$   $V_0$  will go from  $V_{L+}$  to  $V_{L-}$  and after time  $T_2$  it will go from  $V_{L-}$  to  $V_{L+}$  and the total time period will be the sum of these 2 time periods, in the next module we shall be covering the mono stable multi vibrator which is different from both bi-stable multi vibrator and the Astable multi vibrator in that it has only a mono stable multi vibrator has one only one stables.

So say state 1 is the stable state then if it is in the state 1 it will continue to be in that state until it is unless it is disturbed if it is disturbed it will go to the other state, state 2 but that state 2 is not a stable state that is if it is in state 2 it will come back to state 1, so that is what we will discuss in the next module, thank you.