

Data Analytics with Python
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Lecture – 40
Linear Regressions Model VS Logistic Regression Model

In this class, we are going to compare logistic regression versus linear regression because it is very important to understand how this linear regression and logistic regressions are connected. If you understand the relationship between this linear and logistic regression, it is easy to interpret the meaning of logistic regression. So, agenda of this class is comparison of linear regression model and logistic regression model.

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Estimating the relationship

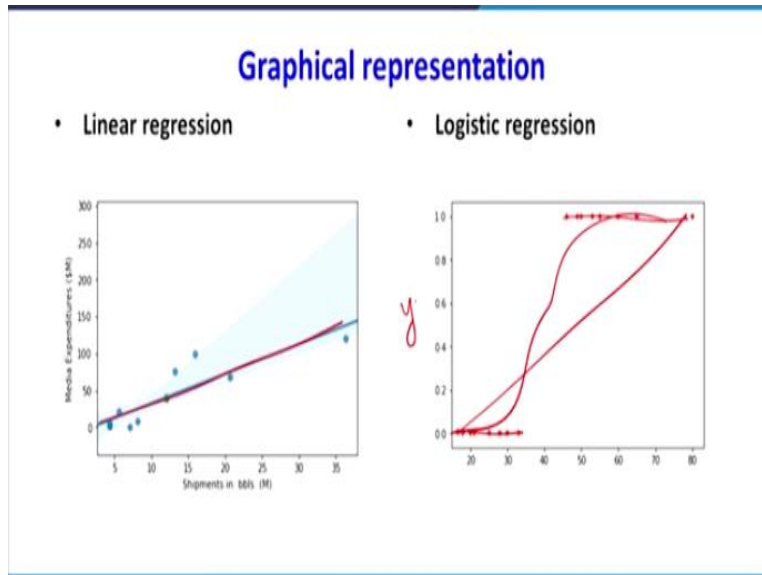
<p>Linear regression model</p> <ul style="list-style-type: none">• $Y_1 = X_1 + X_2 + \dots + X_n$• Where ,<ul style="list-style-type: none">- Y_1 = continuous data- Independent variables = nonmetric and metric	<p>Logistic regression model</p> <ul style="list-style-type: none">• $Y_1 = X_1 + X_2 + \dots + X_n$• Where ,<ul style="list-style-type: none">- Y_1 = Binary nonmetric- Independent variables = nonmetric and metric
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We will see the first relationship, first difference, estimating the relationship, when you look at the linear regression model, we used to write Y_1 equal to $X_1 + X_2 +$ and so on X_n , where Y_1 is a continuous data that is dependent variable, X_1, X_2 are independent variable, this independent variable it can be continuous we can call it as metric, otherwise it may be a discrete, we can call it as non-metric.

The linear regression model, if the independent variable is discrete variable, we can use the concept of dummy variable regression, whereas in logistic regression model, the general model is Y_1 equal to $X_1 + X_2$ to X_n , where the Y_1 is a binary variable, it is a nonmetric binary

variable. The independent variable can be continuous or discrete, we can call it other way; it may be a metric or nonmetric that it is a basic difference between linear regression model and logistic regression model.

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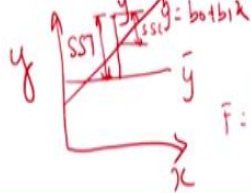
The another difference is if you plot a simple independent variable and the dependent variable for a linear regression, you may able to connect all the points this way but in logistic regression, value of Y can be only 2 possibilities may be 0 or 1, you may get this kind of relationship. What is a meaning here is you cannot form a linear relationship this way, you have to form a; a kind of an S shaped curve that is another difference between linear and logistic regression. What is that in the y axis, see 0 to 300 for linear for example, here you see that it is a possibility, not only that the y value is nothing but the probability but here their y value is the actual values.

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Correspondence of Primary Elements of Model Fit

Linear Regression

- Total sum of squares *SST*
- Error sum of squares *SSE*
- F test of model fit
- Coefficient of determination (R^2)
- Regression sum of squares *SSR*



$$F = \frac{MSR}{MSE} = \frac{SSR/k}{SSE/n-k-1} \quad R^2 = \frac{SSR}{SST}$$

Logistic Regression

- -2LL of base model
- -2LL of proposed model
- Chi-square test of -2LL difference (5)
- Pseudo R^2 measures
- Difference of -2LL for base and proposed models

Correspondence of primary elements of model fit between linear regressions, logistic regression, we used to write SST; total sum of square that is for linear regression, the equivalent term for logistic regression is $-2LL$ that is the log likelihood of base model. Here, we have to write SSE; error sum of square, the equivalent term in the logistic regression is $-2LL$ of proposed model. I have explained, what is the meaning of log likelihood in my previous lectures.

In this lecture also, I will show you the software output where we can get it this log likelihood value. We know that in a simple linear regression, the meaning of SST is like this, say this is \bar{y} , this is y , suppose a line goes like this, this is our predicted value $b_0 + b_1x$, this is our x value, this is our y value. So, this distance was our SST, the equivalent value in the logistic regression is $-2LL$.

Similarly, we have seen SSE, this unexplained this length, this length in the regression equation is SSE; error sum of square are unexplained variance portions, in the linear regression model to test the overall fit; model fit, we have used F test. There what was the F test in the linear regression model, F is MSR divided by MSE, what is MSR; MSR is SSR divided by k ; number of independent variable, divided by $SSE n - k - 1$.

Sometimes, some books they use k , some books they use p to explain the number of independent variables that is a F value. The equivalent test in logistic regression is chi square test of $-2LL$

difference that value is nothing but your G, in the linear regression to explain the model fit, the goodness of the model the term used is coefficient of determination, R square. So, what is R square?

R square is SSR divided by SST, regression sum of square divided by total sum of square, otherwise explained variance divided by total variance. The equivalent term in logistic regression is pseudo R square; I will explain what is the formula for finding pseudo R square in coming slides. Here, we use SSR; SSR is regression sum of square, the equivalent term for logistic regression is difference of $-2LL$ for base and proposed model.

I will explain the meaning of base and proposed model, base means when there is no independent variable corresponding log likelihood values called base value, when you introduce any 1 independent variable, after introduction of independent variable, the corresponding log likelihood values called model; model log likelihood, I will explain this detail in coming slides.

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Objective of logistic regression

- Logistic regression is identical to discriminant analysis in terms of the basic objectives it can address
- Logistic regression is best suited to address two research objectives:
 - Identifying the independent variables that impact group membership in the dependent variable
 - Establishing a classification system based on the logistic model for determining group membership

Then with respect to objective of logistic regression, how the linear and logistic regression differs. Logistic regression is identical to discriminant analysis in terms of basic objectives it can address. There is a one technique called discriminant analysis, the basic difference is in logistic regression, we had only 2 levels; 0 or 1 but in the discriminant analysis, we can have more than 1 level that case is called discriminant analysis.

This I did not cover it but this is the concept behind of discriminant analysis, so logistic regression is identical to discriminant analysis in terms of basic objective it can address; still we go for logistic regression. If there are 2 category, we can go for discriminant analysis also but still we prefer logistic regression because it is best suited to address 2 research objectives, one is identifying the independent variables that impact group membership in the dependent variable. Another one is establishing a classification system based on the logistic model for determining group membership.

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The fundamental difference

- Logistic regression differs from linear regression, in being specifically designed to predict the probability of an event occurring (ie., the probability of an observation being in the group coded 1)
- Although probability values are metric measures, there are fundamental differences between linear regression and logistic regression



There are some more reason is there, the fundamental difference between logistic and linear regression is; logistic regression differs from linear regression in being specifically designed to predict the probability of an event occurring, so the y value is nothing but the probability that is the probability of observation being group coded 1 or not, although the probability values are metric measures, there are fundamental differences between linear and logistic regression. Even though, we can say the probability value is metric, so there is a 2 possibility, it may be 0 or 1, so we may get different probability, when we go for logistic regression.

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Log likelihood

- Measure used in logistic regression to represent the lack of predictive fit
- Even though this method does not use the least squares procedure in model estimation, as is done in linear regression, the likelihood value is similar to the sum of squared error in regression analysis

SSE

Then, log likelihood; measures used to logistic regression to represent lack of predictive fit, so the log likelihood is used to measure how much lack of fit is there, even though this method does not use in least square procedure in model estimation as is done in linear regression, the likelihood value is similar to sum of squared error. If the log likelihood value is lesser, it is better because in the regression, we try to have sum of squared error SSE lesser it is better. Similar to that in logistic regression, if you are getting smaller value of log likelihood it is better that is a good model.

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Logistic vs discriminant

- Logistic regression may be preferred for two reasons
- First, discriminant analysis relies on strictly meeting the assumptions of
 - Multivariate normality and equal variance
 - Covariance matrices across groups
 - Assumptions that are not met in many situations
- Logistic regression does not face these strict assumptions and is much more robust when these assumptions are not met, making its application appropriate in many situations

Now, we will compare when should we go for logistic regression, when should we go for discriminant analysis, even 2 slides before also, I have explained comparison between logistic

and discriminant analysis. Discriminant analysis we can have more than 2 levels, 3 levels or 4 levels. The problem related to logistic regression can be solved with the help of discriminant analysis, where there are 2 levels.

We can say logistic regression is a special case of discriminant analysis but we would not go for discriminant analysis, we will go for logistic regression, there are some reason is there. See that the logistic regression may be preferred for 2 reasons. First; discriminant analysis relies on strictly meeting the assumption of multivariate normality and equal variance that is the first assumption for the discriminant analysis.

That means, the data has to follow normality and it has to have equal variance and the covariance matrices across groups is necessary, when we go for discriminant analysis. Assumptions that are not met in many situations, a real time problems we cannot have this assumptions, in that situation whenever there is a 2 level in the dependent variable instead of going for discriminant analysis, we can go for logistic regression.

Because these assumptions are not required for logistic regression otherwise, we can say logistic regression is more robust than discriminant analysis when there is an only 2 category in the dependent variable. The next point; the logistic regression does not face these strict assumption and is much more robust when these assumptions are not met, making its application appropriate in many situations, that is why we are going for logistic regression over discriminant analysis.

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Logistic vs discriminant

- Second, even if the assumptions are met, many researchers prefer logistic regression because it is similar to multiple regression
- It has straightforward statistical tests, similar approaches to incorporating metric and nonmetric variables and nonlinear effects, and a wide range of diagnostics
- Logistic regression is equivalent to two-group discriminant analysis and may be more suitable in many situations

Another point is even though, the assumptions are met, many researchers prefer logistic regression because it is similar to multiple regression, many possibility to interpret the result, it has straightforward statistical test, similar approaches to incorporating metric and nonmetric variables and nonlinear effects and a wide range of diagnostics. Logistic regression is equivalent to 2 groups; this point which I am trying to say, 2 group discriminant analysis may be more suitable in many situations.

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Logistic vs discriminant : Sample size

- One factor that distinguishes logistic regression from the other techniques is its use of maximum likelihood (MLE) as the estimation technique
- MLE requires larger samples such that, all things being equal, logistic regression will require a larger sample size than multiple regression
- As for discriminant analysis, there are considerations on the minimum group size as well

With respect to sample size which is better; logistic or discriminant analysis, one factor that distinguishes logistic regression from the other techniques is its use of maximum likelihood as the estimation technique. Maximum likelihood estimation requires larger sample such that all

things being equal, logistic regression will require a larger sample size than multiple regression, as of discriminant analysis there are considerations on minimum group size as well.

The another when we go for logistic regression, one point is that you need to have large sample size because it follow maximum likelihood estimate because the value of maximum likelihood estimate is sensitive to the sample size or degrees of freedom.

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Logistic vs discriminant : Sample size

- The recommended sample size for each group is at least 10 observations per estimated parameter 3 -
- This is much greater than multiple regression, which had a minimum of five observations per parameter, and that was for the overall sample, not the sample size for each group, as seen with logistic regression

Regression: 1-5
L. R : 1:10

The recommended sample size for each group is at least 10 observations per estimated parameter, when we go for logistic regression that means, if you are capturing 1 variable, you need to have 20 observations. If you are capturing 3 variables, you have to have 30 observations, this is the thumb rule; this is much greater than multiple regressions which had minimum 5 observations per parameter.

That was for the overall sample not the sample size of each group as seen in the logistic regression, so what the point here is if it is multiple regression for 1 variable, you need to have, you can have 5 respondent rated this regression when you go for logistic regression in to help for one variable in the top 10 respondent where it is regression. When you go for logistic regression, you need to have, for 1 variable, you need to have 10 respondent.

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Determination of coefficients

Linear regression

• R^2

- $r^2 = SSR/SST$

where:

SSR = sum of squares due to regression

SST = total sum of squares

Logistic regression

$$R^2_{Logit} = \frac{-2LL_{null} - (-2LL_{model})}{-2LL_{null}}$$

Where:

LL = Loglikelihood

$-2LL_{null}$ = -2LL of base model

$-2LL_{model}$ = -2LL of proposed model

Then the goodness of fit of the both linear and logistic regression, as I told you the linear regression, the R square that is a coefficient of determination is measured by SSR divided by SST, regression sum of square divided by total sum of square. The equivalent term in logistic regression is pseudo R square, otherwise R square logit equal to $-2LL$ for null model, $-2 \log$ likelihood minus of $-2LL$ log likelihood for model divided by $-2 \log$ likelihood for null.

This value I will show what is the null LL and model LL, so LL is likelihood, if I say $-2LL$ of log likelihood of base model without any independent variable, $-2LL$ model is meaning here is for model means, it is a proposed model, when you bring a new dependent variable into the logistic regression model that time what was the corresponding log likelihood value that is called this model value for log likelihood.

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Determination of coefficients

Linear regression

OLS Regression Results

Dep. Variable:	Media Expenditures (M)	R-squared:	0.783
Model:	OLS	Adj. R-squared:	0.756
Method:	Least Squares	F-statistic:	28.83
Date:	Wed 10 Oct 2018	Prob of nonlinearity:	0.000063
Time:	18:18:28	Log Likelihood:	-44.255
No. Observations:	10	AIC:	82.71
Df Residuals:	8	BIC:	83.32
Df Model:	1		
Covariance Type:	nonrobust		

coef	std err	t	Prob	[0.025	0.975]
intercept	7.6277	11.485	0.004	0.525	14.132
Spending in \$MM (M)	4.0205	0.745	5.379	0.001	2.289

Statistics: F=28.831 Durbin-Watson: 1.473
 Prob(Collinearity): 0.113 Jarque-Bera (skew): 2.129
 Skew: 1.129 Prob(KMO): 0.345
 Kurtosis: 2.925 Cond. No.: 24.8

Logistic regression

Results: Logit

Model:	Logit	Pseudo R-squared:	0.192
Dependent Variable:	Coupon	AIC:	12.8864
Date:	2019-09-08 11:07	BIC:	12.8916
No. Observations:	10	Log-likelihood:	-4.0432
Df Model:	1	LL(Null):	-5.0040
Df Residuals:	8	(LR p-value):	0.16560
Converged:	1.0000	Scale:	1.0000
No. Iterations:	7.0000		

coef.	Std. Err.	z	P> z	[0.025	0.975]
Spending	-0.6318	0.4366	-1.3838	0.1664	-1.5267
Card	-0.0029	1.4887	-0.0020	0.9984	-2.9287

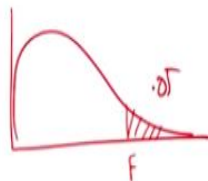
As I told you, you see that when you go for I have run this one previously, see here it is R square 0.783, here it is pseudo R square and as I told you in the previous class, you see that here there is a LL null, when there is no independent variable corresponding the value of likelihood is this much, this is null model, this is the base model, so this is your model likelihood, so we have to find the difference of these 2 to get the R square.

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Testing for overall significance

Linear regression

- F-test of model fit
- $F = MSR/MSE$



Logistic Regression

- G-test of model fit

$$G = -2 \ln \left[\frac{\text{likelihood without the variable}}{\text{likelihood with variable}} \right]$$

$$= -2 [-5 - (-4)]$$

$$= -2 [-1] = 2$$



Now, we will see how to test the overall significance of linear regression and logistic regression, to test the overall significance of a linear regression we know that the F value is nothing but MSR divided by MSE, mean regression sum of square divided by mean error sum of square, then

what we will do; we will, the error of distribution will follow like this, we will find out what is the say, suppose this is 0.05, we will get corresponding F value, this is our calculated F value.

With the calculated F value is lying on that side will reject null hypothesis, if it is lying on acceptance say, you will accept it but for logistic regression, the formula is $-2LL$ likelihood without the variable divided by likelihood with variable, this value can be find out, see -2 , when we say log value, it is division is nothing but subtraction, so likelihood without the variable is -5 minus; this minus for the log of division, likelihood with variable is your -4 . When we simplify $-5 + 4$, so we will get -1 , so $+2$.

This G also follow chi square distribution; this square is a right skewed distribution, this is your G value, G value is 2 for the degrees of freedom is number of independent variable in a logistical regression, that number of independent variable is nothing but the degrees of freedom for the G value, this value you can get it from this is output of Python of logistic regression and the linear regression, this was the comparison.

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Testing for significance

<p style="color: red; font-weight: bold;">Linear regression</p> <ul style="list-style-type: none"> • t-test <div style="border: 1px solid orange; padding: 10px; margin-top: 10px;"> $t = \frac{b_1 - \beta_1}{S_{b_1}}$ <p style="font-size: small;">where: $S_{b_1} = \frac{S_e}{\sqrt{SS_{xx}}}$</p> $S_e = \sqrt{\frac{SSE}{n-2}}$ $SS_{xx} = \sum X^2 - \frac{(\sum X)^2}{n}$ <p style="font-size: x-small;">β_1 = the hypothesized slope df = n - 2</p> </div>	<p style="color: red; font-weight: bold;">Logistic regression</p> <ul style="list-style-type: none"> • Wald-test <div style="border: 1px solid yellow; padding: 10px; margin-top: 10px; display: inline-block;"> $W = \frac{\hat{\beta}_1}{SE(\hat{\beta}_1)} = \frac{-0.0029}{1.4887}$ </div>
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The another point here is to test the significance of each independent variable in a linear regression model, will use t test, the t test; the calculated t test is $b_1 - \beta_1$, here the assumption was β_1 equal to 0 that was our null hypothesis, H_1 is β_1 not equal to 0, then we will find

out t value, then we look for see $n - 2$ degrees of freedom, $n - k - 2$ degrees of freedom, then we will compare it, whether it lying on the acceptance in the rejection site.

The equivalent test in the logistic regression to test the individual significance of each independent variable we should go for this test called Wald test, this Wald test is nothing but estimated beta 1 divided by standard error of a beta 1, so here you go back, see here the for example, the card; the estimated beta 1 is - 0.0029, the standard error is this value is standard error 1.4887, so this is equivalent to your z value.

So, this z value will be used to test whether the model is the individual independent variable is significant or not, this z value. This z value you got it, this dividing $- 0.0027$ by 1.480, this value is nothing but your Wald statistic.

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Model Estimation fit

- The basic measure of how well the maximum likelihood estimation procedure fits is the likelihood value, similar to the sums of squares values used in multiple regression **SSE**
- Logistic regression measures model estimation fit with the value of -2 times the log of the likelihood value, referred to as -2LL or -2 log likelihood
- The minimum value for -2LL is 0, which corresponds to a perfect fit (likelihood = 1 and -2LL is then 0)

Model estimation fit; the basic measure of how well the maximum likelihood estimation procedure fits is the likelihood value, similar to the sum of square value used in the multiple regressions, it is equivalent to your SSE. What will happen in multiple regression if the value of SSE is low, it is a good model, the same way logistic regression measures model estimation fit with the value of $- 2$ times log of likelihood value referred to as $- 2LL$.

The minimum value of $-2LL$ is 0, the similar to the SSE equal to 0, which corresponds to a perfect fit, so in the linear regression it is SSE, in the logistic regression it is $-2LL$, always we prefer lower is better.

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Model Estimation fit

- The lower the $-2LL$ value, the better the fit of the model
- The $-2LL$ value can be used to compare equations for the change in fit

The lower the $-2LL$ value, the better fit the model is, the $-2LL$ value can be used to compare equations for change in fit. So, what will happen; first we have to run this model without any independent variable, we have to get what is $-2LL$, then we have to introduce another independent variable, then we have to compare how much error term is there. If it is lesser, then the variable which have included is explaining the model in better way that is a meaning of comparing equations for change in fit.

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Between Model Comparison

- The likelihood value can be compared between equations to assess the difference in predictive fit from one equation to another, with statistical tests for the significance of these differences
- The basic approach follows three steps:

As I told you between model comparison, the likelihood value can be compared between equations to assess the difference in predictive fit from one equation to another with a statistical test for significance of these differences. There are 3 steps there that to assess whether the model is fit or not after introducing a new variable.

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Step 1 : Estimate a null model

- The first step is to calculate a null model, which acts as the baseline for making comparisons of improvement in model fit.
- The most common null model is one without any independent variables, which is similar to calculating the total sum of squares using only the mean in linear regression. \bar{y}
- The logic behind this form of null model is that it can act as a baseline against which any model containing independent variables can be compared.

The first step is; we have to estimate the null model, what is null model? The first step is to calculate a null model, which act as a baseline for making comparison of improvement in the model fit. The most common null model is one without any independent variables which is similar to calculating the total sum of square using only the mean linear regression, it is like you

know \bar{y} . The logic behind this form of null model is that it can act as a baseline against which any model containing independent variable can be compared.

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Step 2: Estimate the proposed model

- This model contains the independent variables to be included in the logistic regression model.
- This model fit will improve from the null model and result in a lower -2LL value.
- Any number of proposed models can be estimated

Step 2 is estimate the proposed model, this model contains the independent variables to be included in the logistic regression model, this model fit will improve from the null model and result in lower – 2LL value, if the after including a new independent variable, if the value of – 2LL low, then the model is good model, any number of proposed model can be estimated this way.

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Step 3: Assess -2LL difference:

- The final step is to assess the statistical significance of the -2LL value between the two models (null model versus proposed model).
- If the statistical tests support significant differences, then we can state that the set of independent variable(s) in the proposed model is significant in improving model estimation fit.

The third step is assessing the $-2LL$ difference, the final step is to assess the statistical significance of the $-2LL$ value between 2 models that is null model versus proposed model, if the statistical tests support significant differences, then we can state that the set of independent variables in the proposed model is significant in improving the model estimation fit.

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Between model comparison

<p>Linear regression</p> <ul style="list-style-type: none"> • <u>SSE</u> • $= \sum (y_i - \hat{y}_i)^2$ 	<p>Logistic Regression</p> <ul style="list-style-type: none"> • <u>$-2LL$ of proposed model</u>
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The another difference between logistic and linear regression is SSE, this also I have explained in my previous slide. In linear regression we say SSE, in logistic regression we say $-2LL$ of a proposed model, if it is lesser then model is good.

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Between model comparison

<p>Linear Regression</p> <ul style="list-style-type: none"> • $SSR = \sum (y_i - \bar{y}_i)^2$ • SST-SSE 	<p>Logistic regression</p> <ul style="list-style-type: none"> • Difference between log likelihood • $= 2LL_{null} - (2LL_{model})$
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In the linear regression we say SSR; in the logistic regression we say difference between log likelihood of null model and the model after introducing the 1 independent variable.

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Normality of Residual (Error)

Linear regression	Logistic regression
<ul style="list-style-type: none">• Normally distributed• Linear regression assumes that residuals are approximately equal for all predicted dependent variable values	<ul style="list-style-type: none">• Binomially distributed• Logistic regression does not need residuals to be equal for each level of the predicted dependent variable values

Another important assumption between linear and logistic regression is we can say difference with respect to error is; a linear regression model the error term follow normal distribution but in a logistic regression, the error term follow binomial distribution. Linear regression assumes that the residuals are approximately equal for all predicted dependent variable values. Logistic regression does not need residuals to be equal for each level of predicted dependent variables.

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Estimation Methods

<ul style="list-style-type: none">• Linear regression is based on <u>least square estimation</u>• Regression coefficients should be chosen in such a way that it minimizes the sum of the squared distances of each observed response to its fitted value	<ul style="list-style-type: none">• logistic regression is based on <u>Maximum Likelihood Estimation</u>• Coefficients should be chosen in such a way that it maximizes the Probability of Y given X (likelihood)• With MLE, the computer uses different "iterations" in which it tries different solutions until it gets the maximum likelihood estimates
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Another important difference is linear regression is based on the least square estimation via less but the logistic regression is based on the maximum likelihood estimation, this should be our first point. Regression coefficient should be chosen in such a way that it minimises the sum of the square distance of each observed responses to its fitted value, nothing but the error sum of square has to be minimised.

But here, the coefficient should be chosen in such a way that it maximises the probability of y given x, with the maximum likelihood estimation, the computer uses different iterations in which it tries to different solutions until it gets the maximum likelihood estimations, that is how many time solving logistic regression with the help of hand is very difficult.

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Interpretation

<p>Coefficients of linear regression is interpreted as:</p> <ul style="list-style-type: none">• Keeping all other independent variables constant, how much the dependent variable is expected to increase/decrease with an unit increase in the independent variable	<p>In logistic regression, we interpret odd ratios as:</p> <ul style="list-style-type: none">• The effect of a one unit of change in X in the predicted odds ratio with the other variables in the model held constant <p style="text-align: right; color: red; font-size: 2em;">3</p>
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The another difference between logistic and linear regression is the way we interpret the coefficient; this is a very important difference. In logistic regression keeping all other independent variable constant, how much the dependent variable is expected to increase or decrease with an unit increase in the independent variable, this is the way we interpret the meaning of coefficient of each independent variable in a linear regression model.

But in a logistic regression model, the effect of 1 unit change in the X in the predicted odd ratio with respect to other variables in the model held constant, the point here is that the coefficient in the logistic regression is explained with the help of odd ratio, suppose the odd ratio is 3, if the

odd ratio is 3, if there is a 1 unit increase in the independent variable, there is a 3 times more chance, the probability will be increased.

This is the way to interpret the coefficient of logistic regression, in this class I have explained the difference between logistic regression and linear regression model, there are many parameters I have compared the equivalent term for logistic regression, equivalent means with respect to linear regression. If you are so thorough on interpreting the linear regression model after listening to this lecture, you can interpret the logistic regression model in a very easy manner. Thank you very much.