

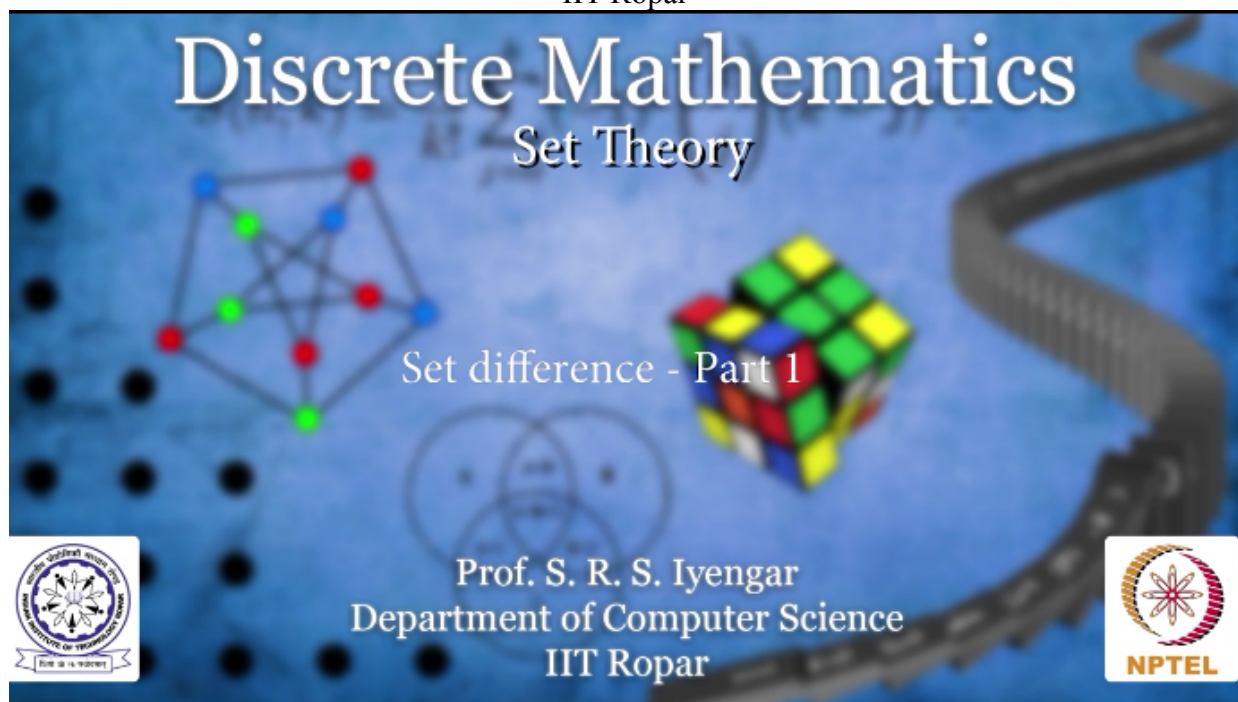
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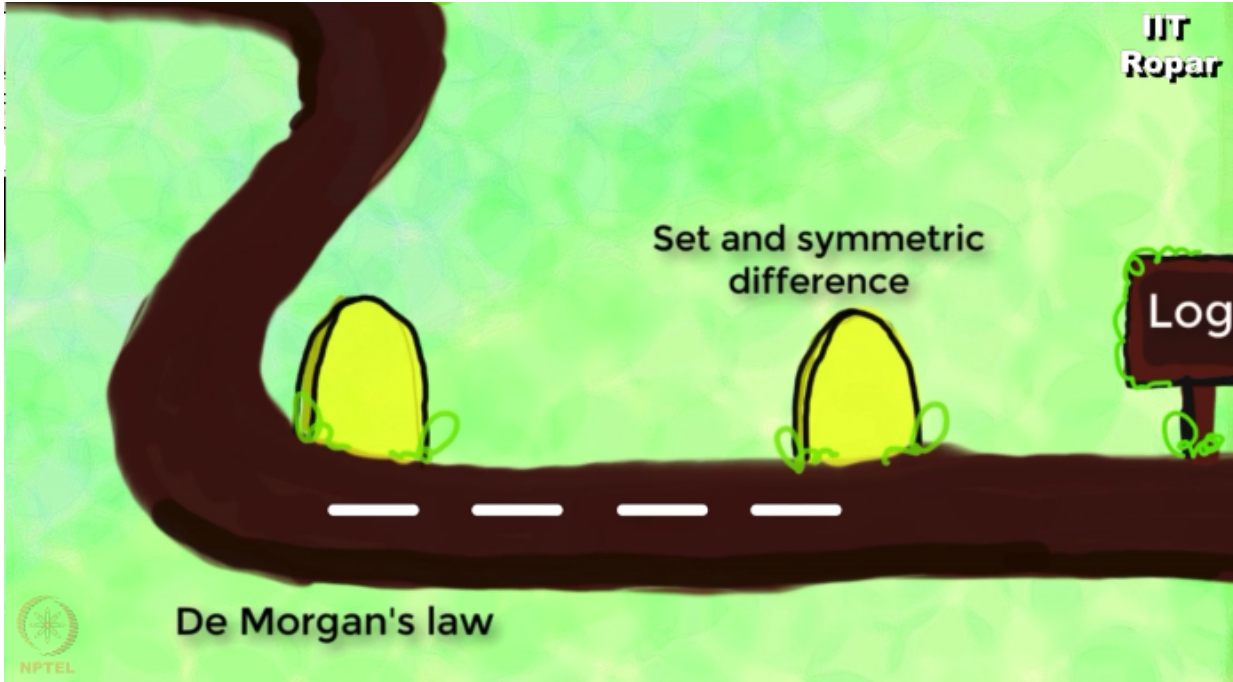
Discrete Mathematics
Set Theory

Set difference – Part 1

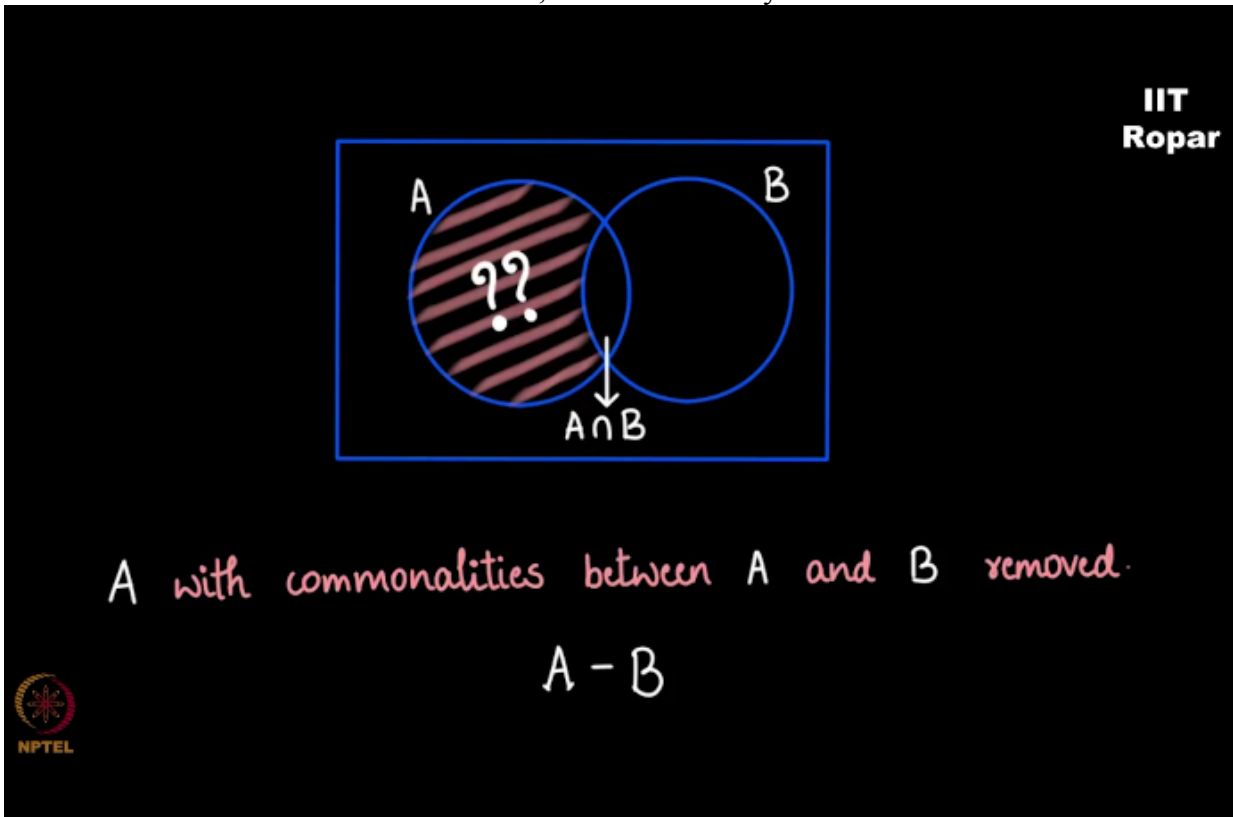
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We will now go ahead and understand what one means by the difference of two sets A and B , it is not the same but very similar to the difference of two numbers that we all are familiar already.



Look at this Venn diagram, you have a set A, you have a set B with some possible intersection, now look at the shaded region, what do you think this is? This is simply that part of A with commonalities between A and B removed, this is denoted by A minus of B.



Now this is not the typical $10 - 8 = 2$ that we now in arithmetic, it is slightly different from the typical subtraction, what you remove is not the whole of B from A, you only remove that part of B which is already in A, this is called the difference between two sets.

$$\cancel{10 - 8 - 2}$$

Whole of B is not removed from A.
Remove that part of B which is already in A.
Difference between two sets



Let me illustrate this with an example, let A be equal to 1, 2, 3, 4, 5, 6 and B be equal to 10, 5, 30, 6 and 100, so what is A-B? So in A you have 5, 6, it is also present in B 5, 6 the rest are not in A, 10, 30, and 100 they are not in A, so A-B will simply be 1, 2, 3, and 4, note that A-B need not be equal to B-A, isn't clear from the example we saw just now, A-B in our example in this Venn diagram happens to be 1, 2, 3, and 4, but B-A happens to be 10, 30, and 100, in fact

$$A = \{1, 2, 3, 4, \textcircled{5}, \textcircled{6}\} \quad B = \{10, \textcircled{5}, 30, \textcircled{6}, 100\}$$

$$A - B = \{1, 2, 3, 4\}$$

Note: $A - B$ need not be equal to $B - A$.

$$B - A = \{10, 30, 100\}$$

$A - B$ and $B - A$ are always disjoint.



they are disjoint, $A - B$ and $B - A$ are actually always disjoint you can observe this, you cannot have a common element in $A - A$ and $B - A$, in fact one can show that $A - B$ intersection $B - A$ is always an empty set, I'll leave that as an exercise problem for you all to explore.

One can show that $A - B \cap B - A = \emptyset$

TRY SOLVING



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