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NPTEL ONLINE CERTIFICATION COURSE

Discrete Mathematics  
Recurrence Relation

A note on the proof

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The proof involves some symbolic manipulations that is mostly not very intuitive, but the idea behind the proof is just this, we will show that whenever you have a recurrence relation of the form  $a_n = c_1 a_{n-1} + c_2 a_{n-2}$  that is Nth term is defined by some constant times the previous term and constant times the previous to previous term, the solution will always be of the form  $a_n = \alpha_1 x_1^n + \alpha_2 x_2^n$ , the proof goes in a way where we plug in this  $a_n$ 's formula in the recurrence relation and show that it is actually satisfying it.

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Proof  $\rightarrow$  Symbolic Manipulations.

Idea :  $a_n = c_1 a_{n-1} + c_2 a_{n-2}$

Solution -  $a_n = \alpha_1 x_1^n + \alpha_2 x_2^n$

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Now in my humble opinion I feel whenever we go ahead and teach such complicated, this proof is slightly complicated non intuitive, okay, so whenever we go ahead and teach proofs you will

miss out on the big picture, the big picture here is a recurrence relation, okay, so let's say  $A_3$  is  $A_2 + A_1$ ,  $A_i$  is  $A_{i-1} + A_{i-2}$ , a Fibonacci sequence,  
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Proof  $\longrightarrow$  Symbolic Manipulations.

Idea:  $a_n = c_1 a_{n-1} + c_2 a_{n-2}$

Solution -  $a_n = \alpha_1 x_1^n + \alpha_2 x_2^n$

$a_3 = a_2 + a_1$

$a_i = a_{i-1} + a_{i-2}$   $\rightarrow$  FIBONACCI SEQUENCE

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if it starts with 0 and 1 as you can see, right, so a recurrence relation the spirit of which is actually captured by computational problems, if he spend a lot of time proving all the cases you will not see the most important point that a computer science student is supposed to see, so what we'll do is in the interest of not demotivating you all we will not get into the proof of this theorem right now, however we will look at the proper proof at the fag end of this chapter, as of now I'll assume this result and go ahead, solve a few problems and connect this idea to computer science.

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