

NPTEL

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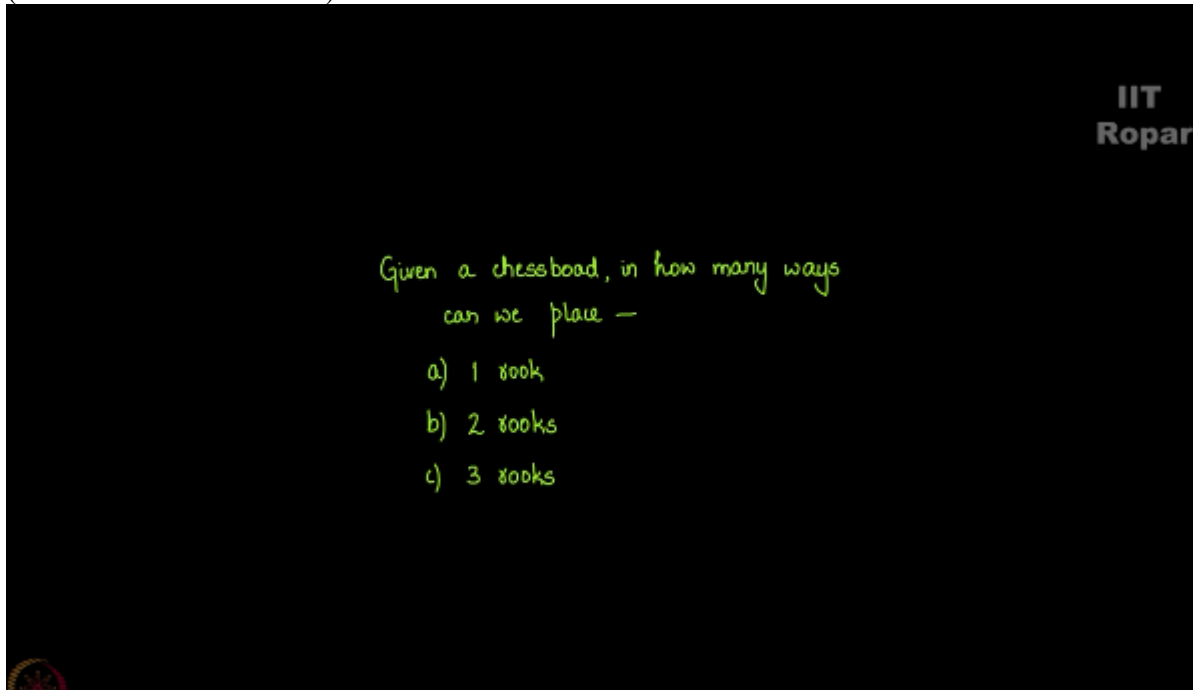
Discrete Mathematics
Principle of Inclusion and Exclusion

Rook Polynomial

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So given a chessboard we ask this question, in how many ways can we place 1 rook? In how many ways can we place 2 rooks, and in how many ways can we place 3 rooks?

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And then note down the numbers and write them as a polynomial like this, so we write it as a 0 rooks cannot be placed in anyway, so we simply write 1 here + 1 rook can be placed in 9 ways so we write down $9X$ + 2 rooks can be placed in 12 ways, so we write $12X^2$ square, and 3 rooks can be placed in 3 ways, so we write $3X^3$ cube, so this is called a rook polynomial of a given chessboard,

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Given a chessboard, in how many ways
can we place —

$$\left. \begin{array}{l} \text{a) 1 rook} \\ \text{b) 2 rooks} \\ \text{c) 3 rooks} \end{array} \right\} \boxed{1 + 9x + 12x^2 + 6x^3}$$

Rook polynomial



and this is how it is represented.

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