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Discrete Mathematics

Let Us Count

Catalan Numbers - Part 4

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So we have seen that the total number of paths without crossing the diagonal from $(0,0)$ to any (n,n) is given by $2nCn$ minus $2nCn$ plus one. This goes by the name the n th Catalan number denoted as C_n . This was given by the mathematician Catalan. So C_n is written by $2nCn$ minus $2nCn$ plus one. After simplification we get it as one by n plus one into $2nCn$. So let us see how the sequence C_n goes. C_0 is one. C_1 is one by two into $2C_1$ which is one. C_2 is one by three into $4C_2$ which is 2. C_3 is one by four into $6C_3$ which is 5 and C_4 is one by five into $8C_4$ which is 14 and so on. So the Catalan numbers sequence is 1, 1, 2, 5, 14, 42, 132 and so on. Let us see some interesting examples of Catalan numbers.

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