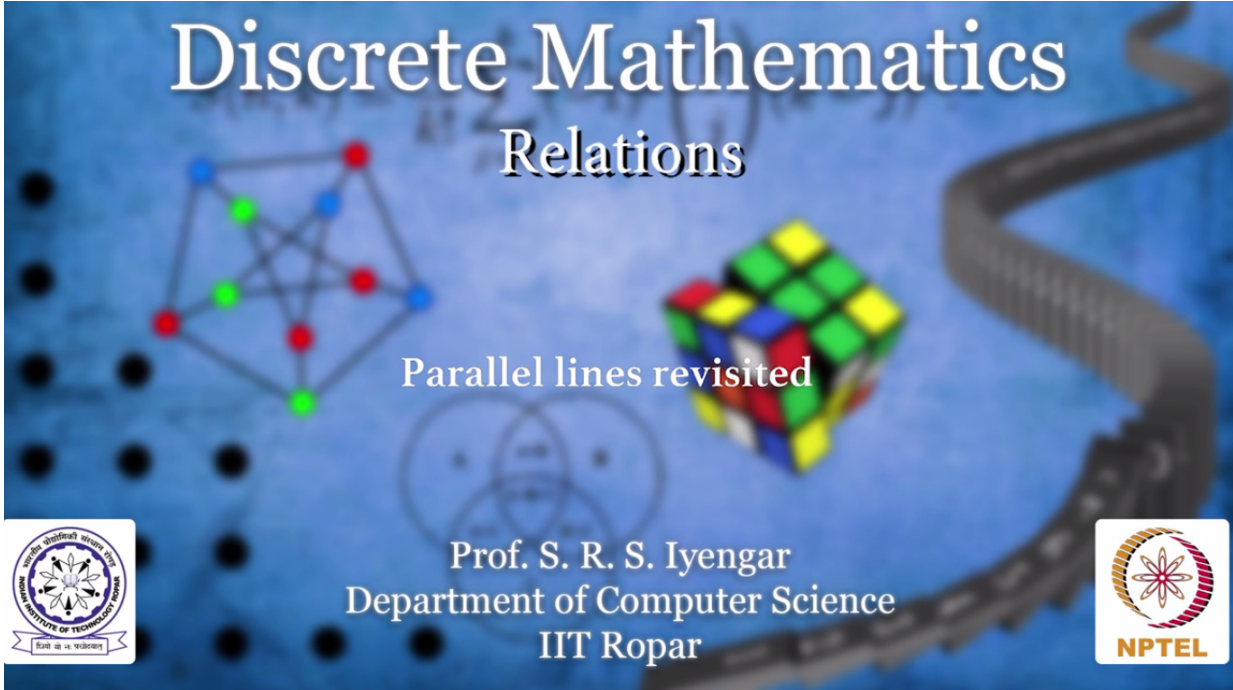




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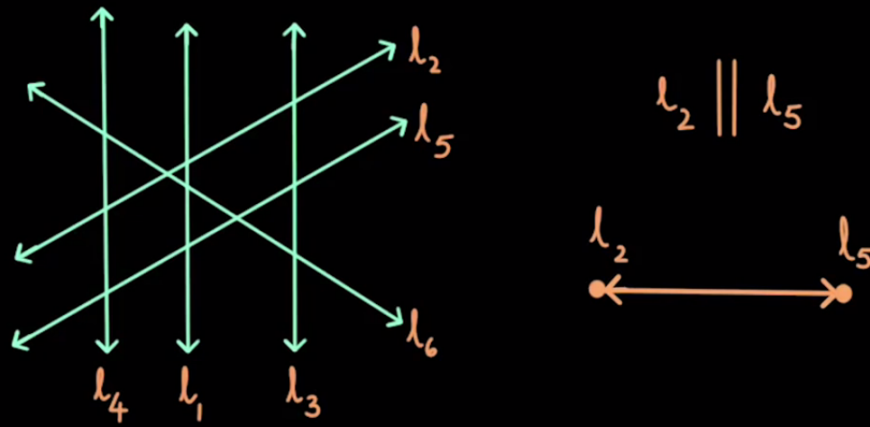
Parallel lines revisited

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Let me take an example now. Of these six lines  $l_1, l_2, l_3, l_4, l_5,$  and  $l_6$  as you can observe  $l_2$  is parallel to  $l_5$  so which means in the graph  $l_2$  will have a line arrow pointing towards  $l_5$  and  $l_5$  is also parallel to  $l_2$  obviously so there will be a symmetric arrows from  $l_2$  to  $l_5$  and  $l_5$  to  $l_2$  so on and so forth.



The graph will look like this and the corresponding matrix will, let me populate the corresponding matrix, there will be a 1, 1, 1, 1, 1, 1, 1 this way. You can pause the video and maybe check if I am right. I have put a 1 let's say in  $l_3$  and  $l_4$ ,  $l_3$ th column and  $l_4$ th column because  $l_3$  is parallel to  $l_4$  so is  $l_4$  with  $l_3$ .  $l_4$  is parallel to  $l_3$ . You see something very nice about this matrix of course the diagonals have 1 adding to that we observe the matrix is symmetric you see on the right side. You see below the diagonal on the left side both are exactly the same that is because  $l_i, l_j, l_j, l_i$ , both have either 1 or 0 that is because two lines are either parallel to each other or they are not parallel to each other.

	$l_1$	$l_2$	$l_3$	$l_4$	$l_5$	$l_6$
$l_1$	1	0	1	1	0	0
$l_2$	0	1	0	0	1	0
$l_3$	1	0	1	1	0	0
$l_4$	1	0	1	1	0	0
$l_5$	0	1	0	0	1	0
$l_6$	0	0	0	0	0	1



Anyways another small observation which I made just now that whenever a line is parallel to another line let us say here  $l_4$  is parallel to  $l_1$  and  $l_1$  is parallel to something else  $l_3$  then  $l_4$  will be parallel to  $l_3$ . Correct. This may not be true in real life where a person A is friends with person B and a person B is friends with person C. Person A needn't be friends with person C. This is not true in real life with the friendship relation but with parallel lines relation this seems to be true, correct.

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